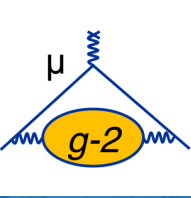
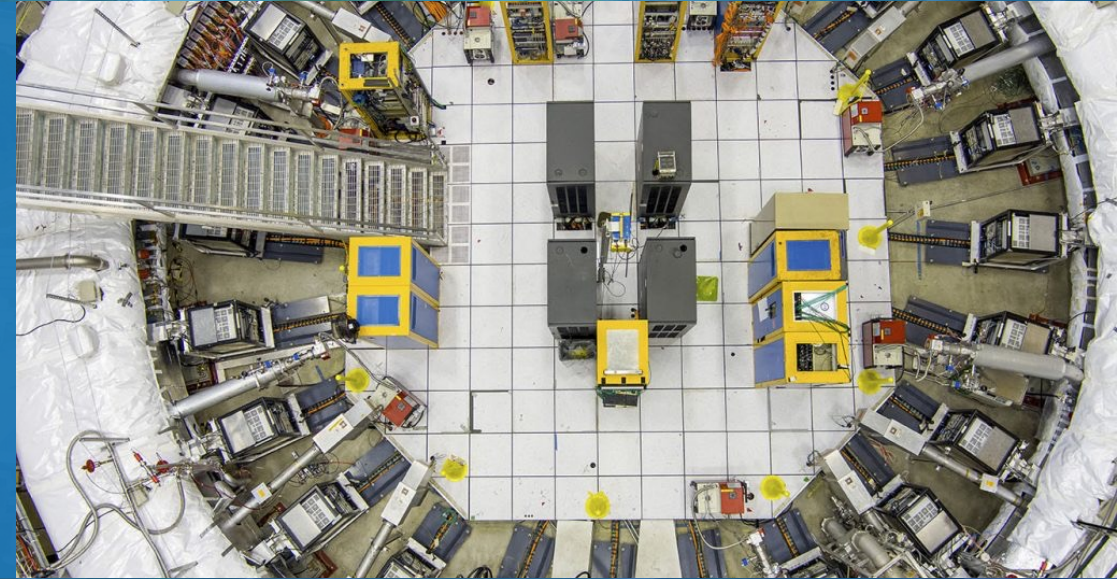


JANUARY 27<sup>TH</sup>, 2026



# The Muon's Wobble: Measuring Muon $g-2$ to Test the Standard Model



**SIMON CORRODI**  
Argonne National Laboratory

Stony Brook University  
Colloquium



# April 2021 – Muons made News

## A Particle's Tiny Wobble Could Upend the Known Laws of Physics

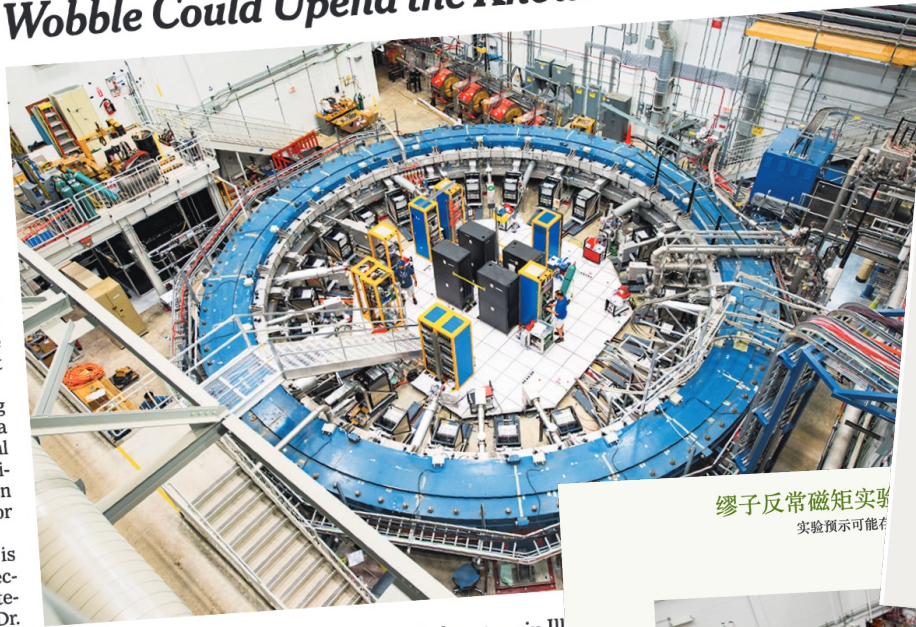
By DENNIS OVERBYE

Evidence is mounting that a tiny subatomic particle seems to be disobeying the known laws of physics, scientists announced on Wednesday, a finding that would open a vast and tantalizing hole in our understanding of the universe.

The result, physicists say, suggests that there are forms of matter and energy vital to the nature and evolution of the cosmos that are not yet known to science.

"This is our Mars rover landing moment," said Chris Polly, a physicist at the Fermi National Accelerator Laboratory, or Fermilab, in Batavia, Ill., who has been working toward this finding for most of his career.

The particle under scrutiny is the muon, which is akin to an electron but far heavier, and is an integral element of the cosmos. Dr. Polly and his colleagues — an international team of 200 physicists from seven countries — found that muons did not behave as pre-



A ring at the Fermi National Accelerator Laboratory in Ill.

缪子反常磁矩实验  
实验预示可能在



缪子反常磁矩实验

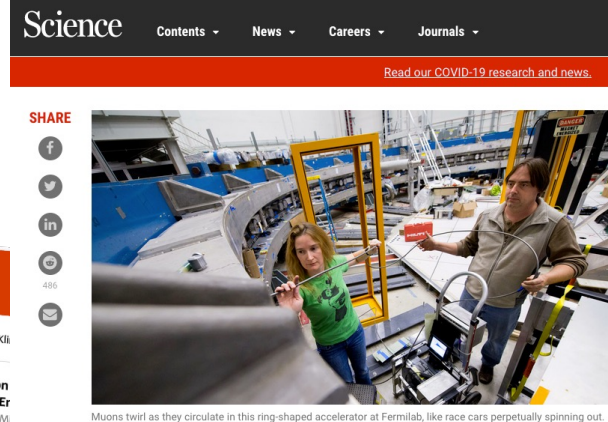
近日，在美国费米国家实验室进行的缪子反常磁矩实验结果与标准模型理论预言不相符，该结果与早期美国布鲁克海文实验室的未知粒子或者作用力。

“这意味着原本经历了多次考验，堪称完美的标准模型理论更完美的理论等待人类去发现。”缪子反常磁矩实验组在《中国科学报》。



### Neue Erkenntnisse in der Teilchenphysik Kundschafter ins Unbekannte

Seit 50 Jahren ersehnen Forscher Einblicke in die Welt jenseits der bekannten Naturgesetze. Mit den Erkenntnissen aus dem Muon-g-2-Experiment könnte sich das Tor zu einer neuen Physik öffnen. Von Johann Grollie



Particle mystery deepens, as physicists confirm that the muon is more magnetic than predicted

By Adrian Cho | Apr. 7, 2021, 11:00 AM

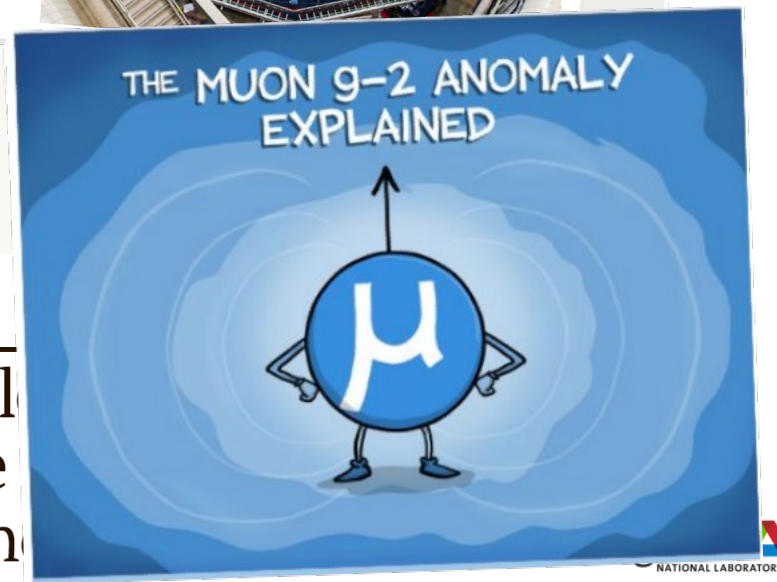


Muons twirl as they circulate in this ring-shaped accelerator at Fermilab, like race cars perpetually spinning out.



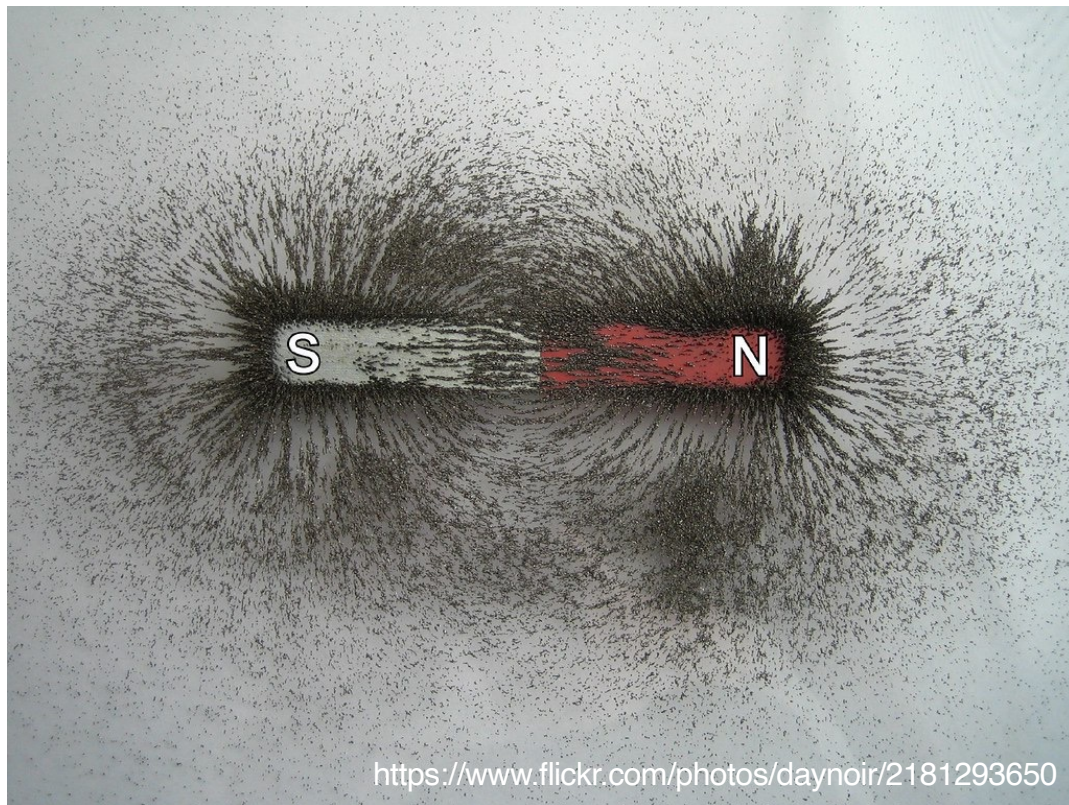
Le Monde  
VENDREDI 9 AVRIL 2021

Une particule élémentaire polarise le modèle de la physique





# ⚙️ Why is this magnetic?



## Classical

Is it full of tiny, circulating currents?  
Ampère's molecular currents



Magnetic Moment:  $\mu = I \cdot A = \frac{evr}{2}$

Angular Momentum:  $L = mvr$

$$\frac{\mu}{L} = \frac{e}{2m}$$

$$\mu = g \frac{e}{2m} L$$

Current loop:  $g = 1$



# ⚙️ Why is this magnetic?

Einstein measured  $g=1$  at 10%-level!

**Physics.** — “*Experimental proof of the existence of Ampère’s molecular currents.*” By Prof. A. EINSTEIN and Dr. W. J. DE HAAS.  
(Communicated by Prof. H. A. LORENTZ),

(Communicated in the meeting of April 23, 1915).

They “knew” that  $g=1$ , and measured it...  
... but this turns out to be false!

## Classical

Is it full of tiny, circulating currents?  
Ampère's molecular currents



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Current loop:  $g = 1$



# ⚙️ Why is this magnetic? Spin!

Later experimental work showed  $g_e \approx 2$

## Quantum Concept

Elementary particles are point-like:  $r \rightarrow 0, A \rightarrow 0, L \rightarrow 0$ , but there is magnetism

1928: Dirac's theory introduces an **intrinsic spin** for electrons

- Magnetism is an intrinsic property of elementary particle

**The g-factor** connects the spin ( $\vec{s}$ ) of a particle to its intrinsic **magnetic moment** ( $\vec{\mu}$ )

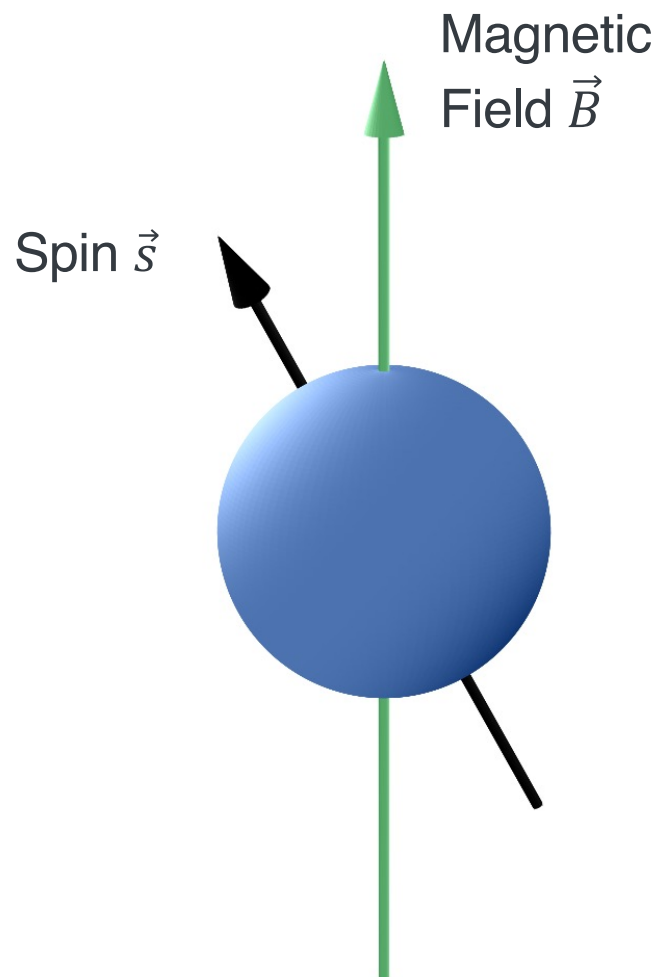
$$\vec{\mu} = g \frac{e}{2m} \vec{s}$$





# The **g**-factor

connects the spin ( $\vec{s}$ ) of a particle to its intrinsic **magnetic moment** ( $\vec{\mu}$ )

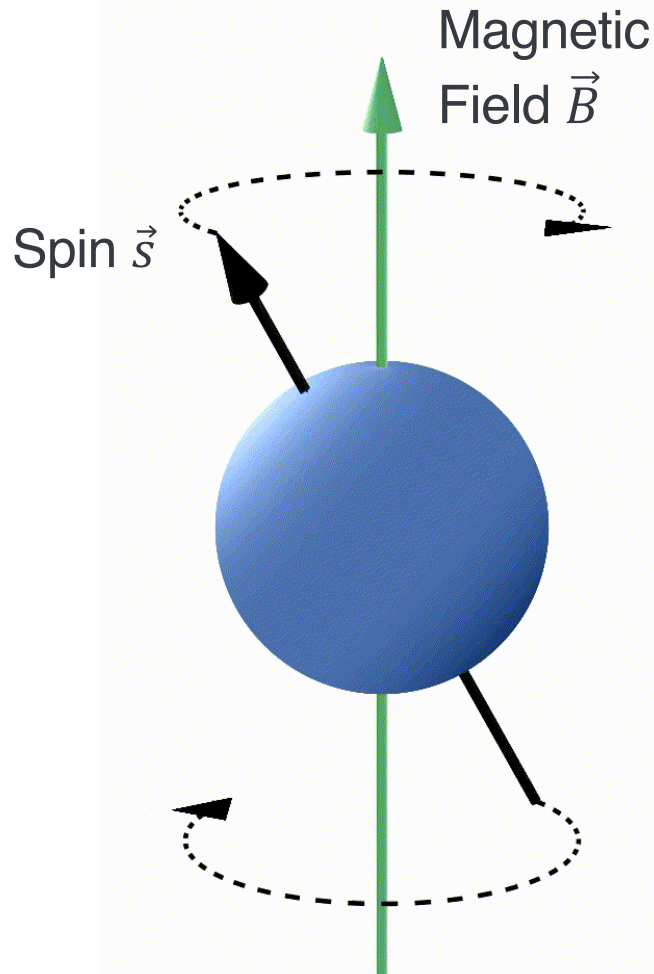






# The **g**-factor

connects the spin ( $\vec{s}$ ) of a particle to its intrinsic **magnetic moment** ( $\vec{\mu}$ )



The **spin precession frequency**  $\omega_s$  in a magnetic field  $\vec{B}$  is proportional to the **g-factor**

$$\vec{\omega}_s = \frac{g}{2} \frac{q}{mc} \vec{B}$$





# Magnetic Moments of Charged Leptons

A long history

## Classical $g = 1$

From classical current loop  $g = 1$ .

*Stern-Gerlach and atomic spectroscopy found  $g_e \approx 2$*

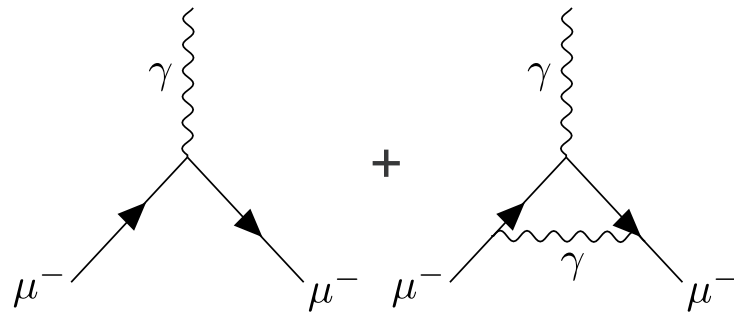
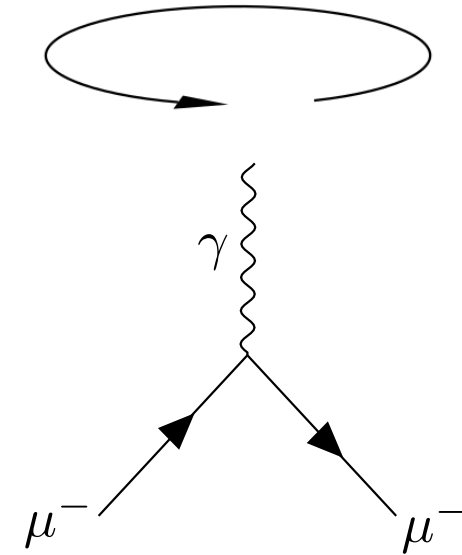
## Dirac (1928) theory $g = 2$

For a pure Dirac spin- $\frac{1}{2}$  charged fermion,  $g = 2$ .

## Schwinger (1948) and beyond $g > 2$

Interactions with **virtual particles** alter  $g$

*$g_e \approx 2 + \alpha/\pi$  prediction, foundation for the Standard Model*



## Feynman Diagrams

- "Bookkeeping" and "visualization" of particle interactions
- Expansion in "number of loops"



# The Standard Model

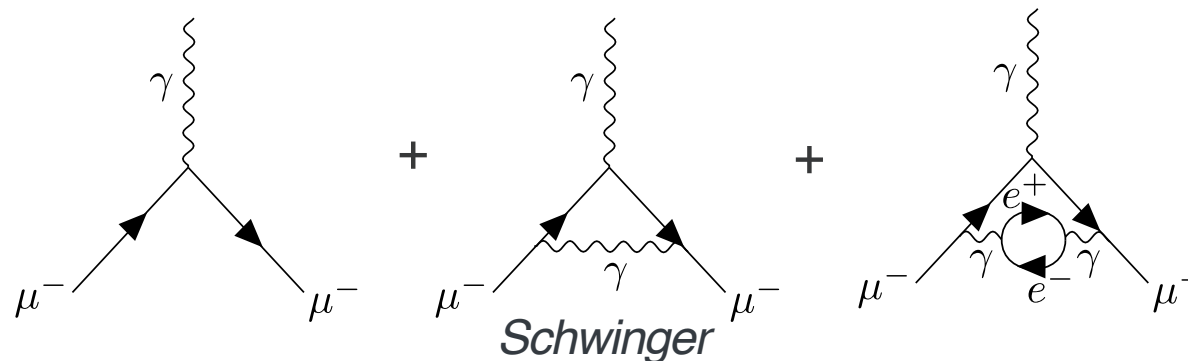
Encodes all known particles and interactions

	I	II	III
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	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino

Interactions with **virtual particles** alter **g**

Dirac-Term (2)

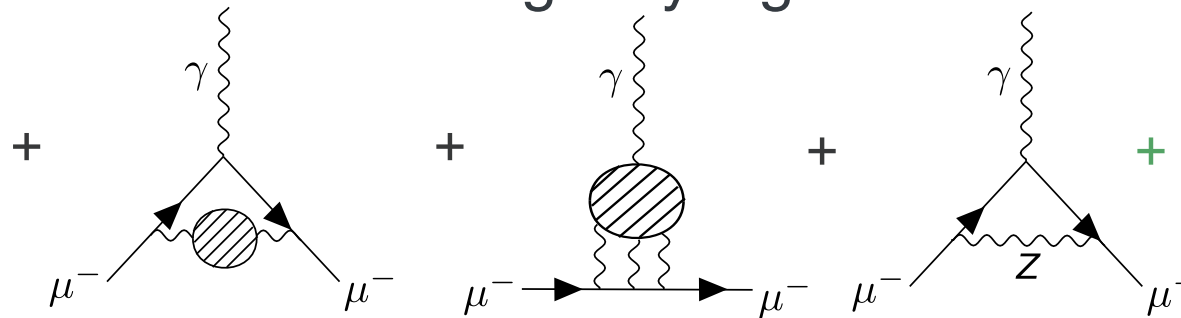
QED



Hadronic Vacuum Polarization

Hadronic Light-by-Light

Electroweak





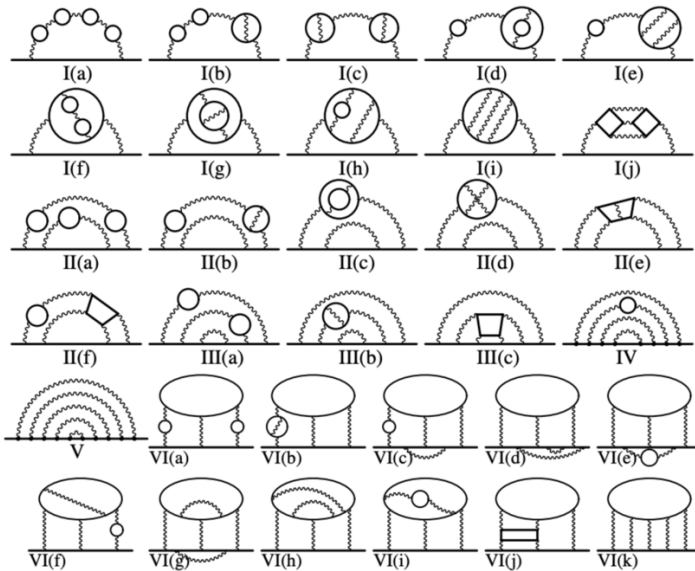


# The Standard Model

Encodes all known particles and interactions

## Quantum Electrodynamics QED

Over 12'000 QED diagrams (5 loops) calculated, extraordinary precision

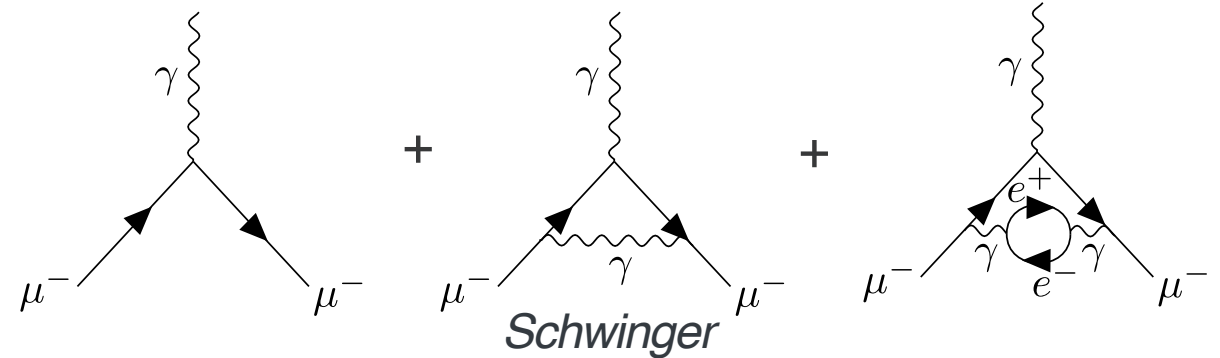


<https://arxiv.org/abs/1205.5370>

Interactions with **virtual particles** alter **g**

### Dirac-Term (2)

### QED

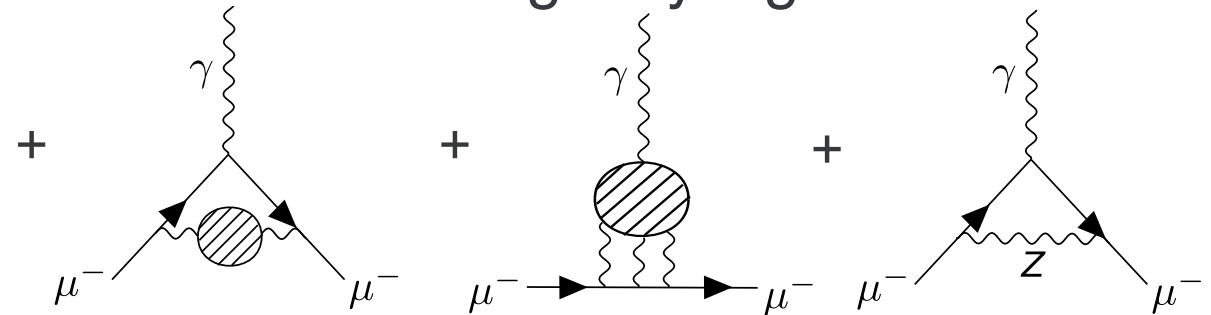


### Hadronic Vacuum Polarization

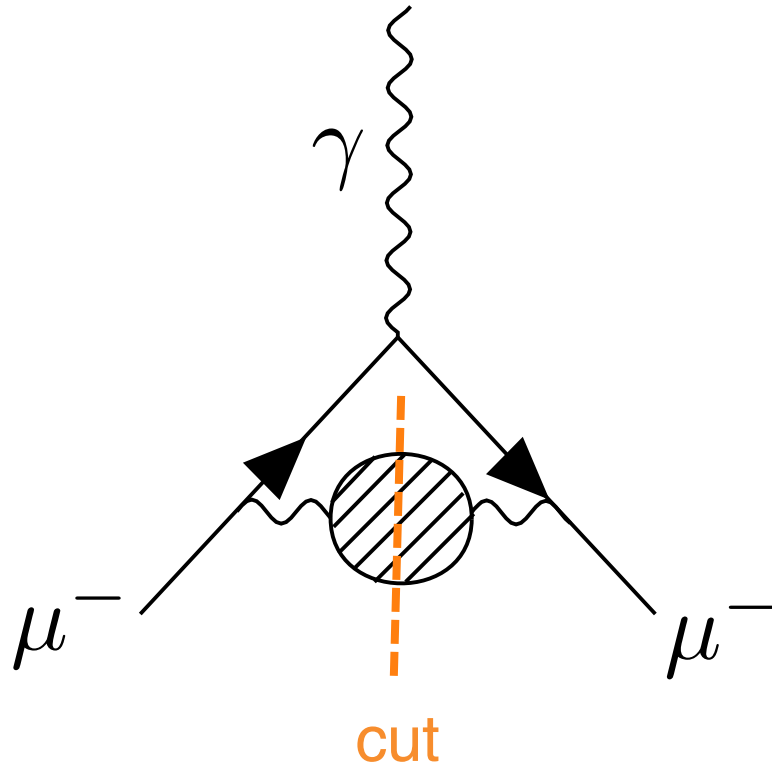
### Hadronic

### Light-by-Light

### Electroweak



# Hadronic Vacuum Polarization: HVP Data-driven Dispersive Approach





# Hadronic Vacuum Polarization: HVP Data-driven Dispersive Approach

Dispersion relation connects  $e^+e^- \rightarrow \text{hadrons}$  to leading order HVP contribution

$$a_\mu^{\text{HVP,LO}} = \frac{\alpha^2}{3\pi^2} \int_{s_{th}}^{\infty} \frac{K(s)}{s} R(s) ds$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \text{muons})}$$

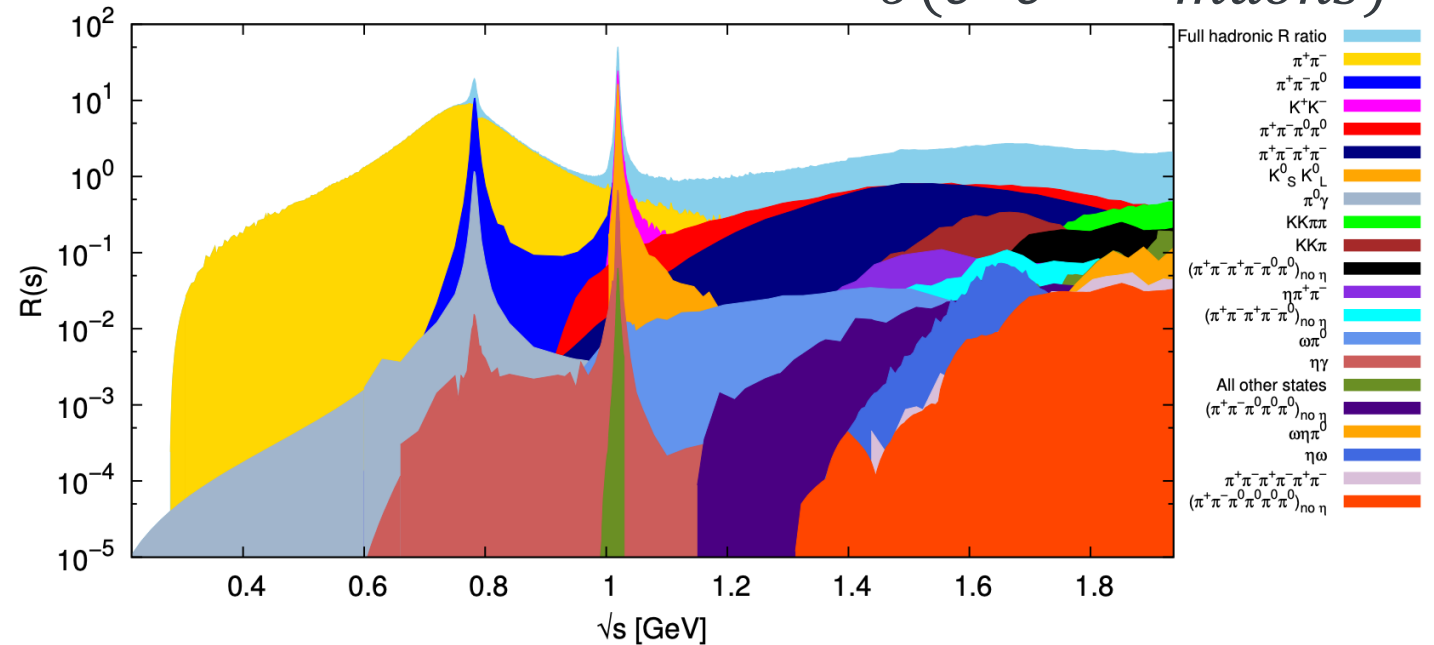
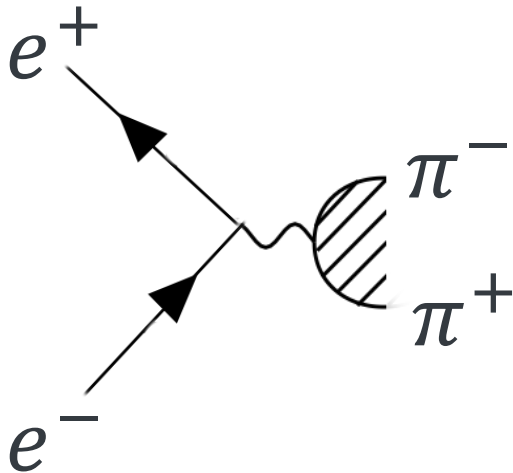
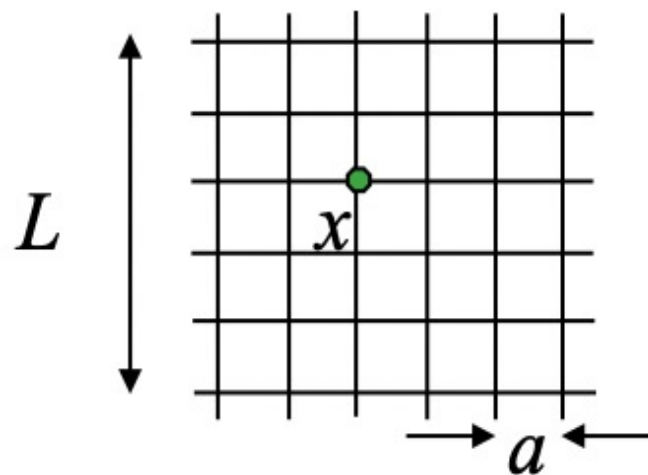


Figure 16: Contributions to the KNT data compilation of the total hadronic  $R$ -ratio from the different hadronic final states below 1.937 GeV [30, 265]. The full  $R$ -ratio is shown in light blue. Each final state is included as a new layer on top in decreasing order of the size of its contribution to  $a_\mu^{\text{HVP,LO}}$ .

# Hadronic Vacuum Polarization: HVP Lattice QCD

Ab-initio calculation with massive computing power



4D grid!



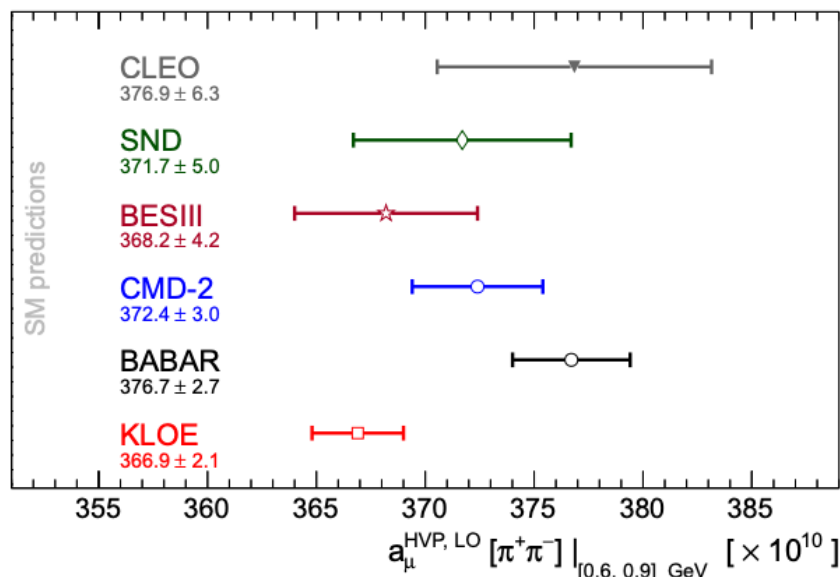
Calculated at supercomputers like  
Aurora at Argonne



# Hadronic Vacuum Polarization: HVP

## The pre-2021 view

data-driven dispersive



a flurry of experiments,  
different technique, some  
inconsistencies

lattice QCD

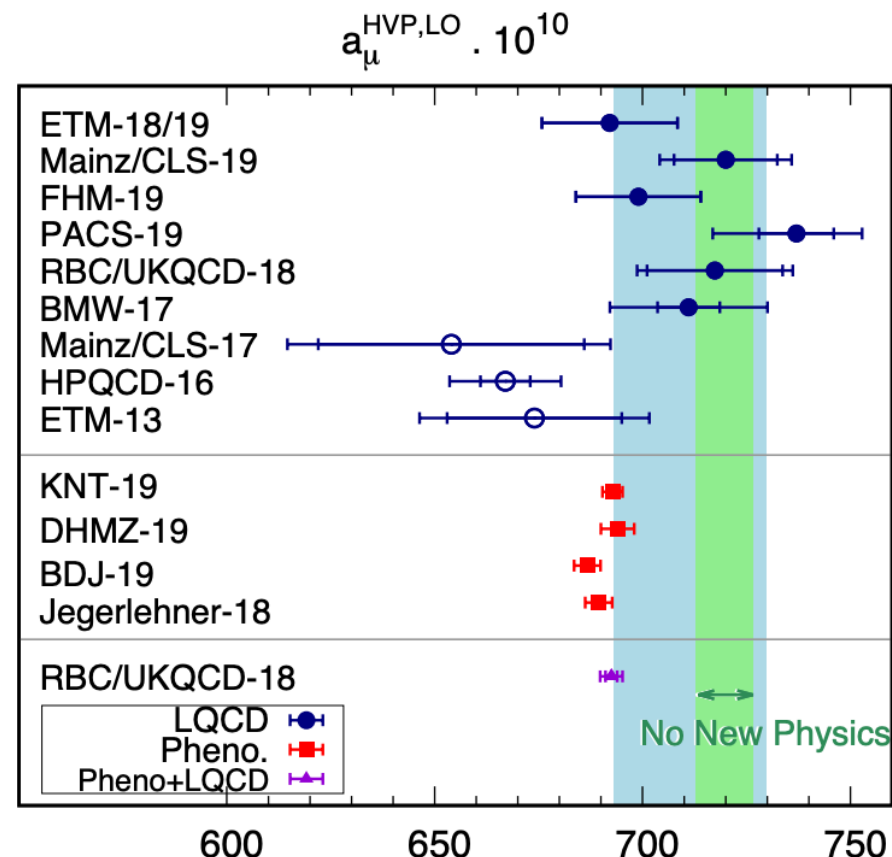


Figure 44: Compilation of recent results for  $a_\mu^{\text{HVP,LO}}$  in units of  $10^{-10}$ . The filled dark blue circles are lattice results that are included in the “lattice world average”. The average, which is obtained from a conservative averaging procedure in Sec. 3.5.1, is indicated by a light blue band, while the light-green band indicates the “no new physics” scenario, where  $a_\mu^{\text{HVP,LO}}$  results are large enough to bring the SM prediction of  $a_\mu$  into agreement with experiment. The unfilled dark blue circles are lattice results that are older or superseded by more recent calculations. The red squares indicate results obtained from the data-driven methods reviewed in Sec. 2. See Table 8 for more information on the results included in the plot. Adapted from Ref. [443].

<https://arxiv.org/pdf/2006.04822>

<https://arxiv.org/pdf/2505.21476>

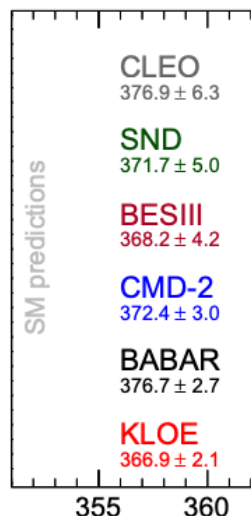
# Hadronic Vacuum Polarization: HVP

The new 2021 review

data-driven

~100 ppb (parts-per-billion)

- 8 significant digits or



a flurry of  
different  
inconsistent



weighting a Bison



has someone added  
a sunflower seed?

are included in the “lattice  
light blue band, while the  
ction of  $a_\mu$  into agreement  
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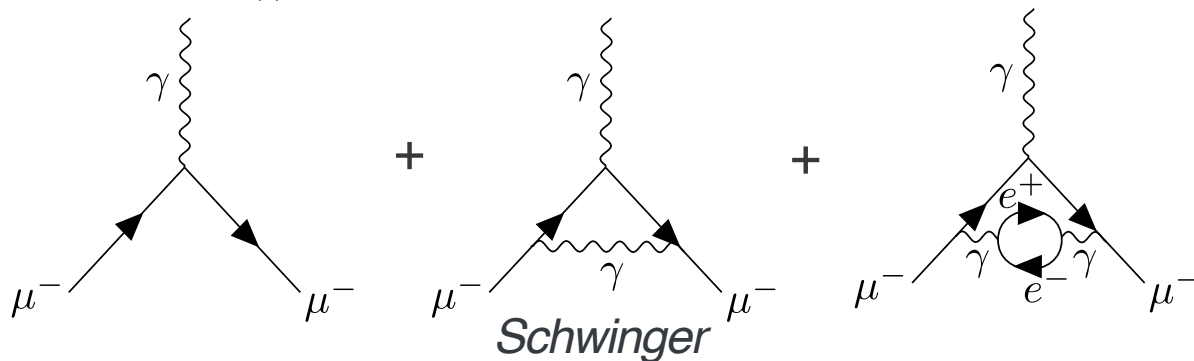


# Testing the Standard Model

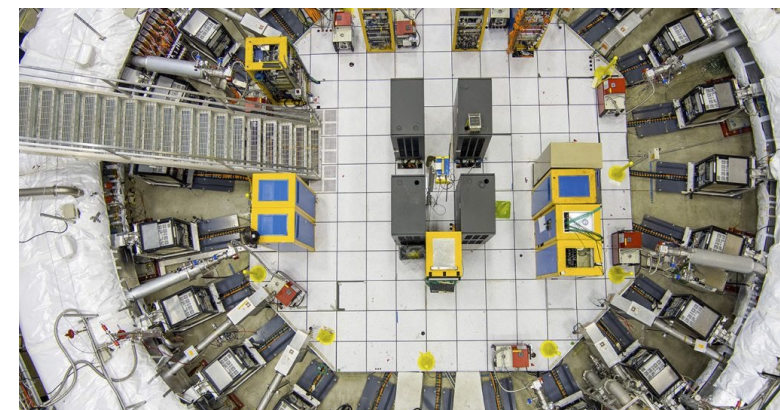
Interactions with **virtual particles** alter **g**  
QED

**Experiments** measure the  
sum of all contributions

Dirac-Term (2)



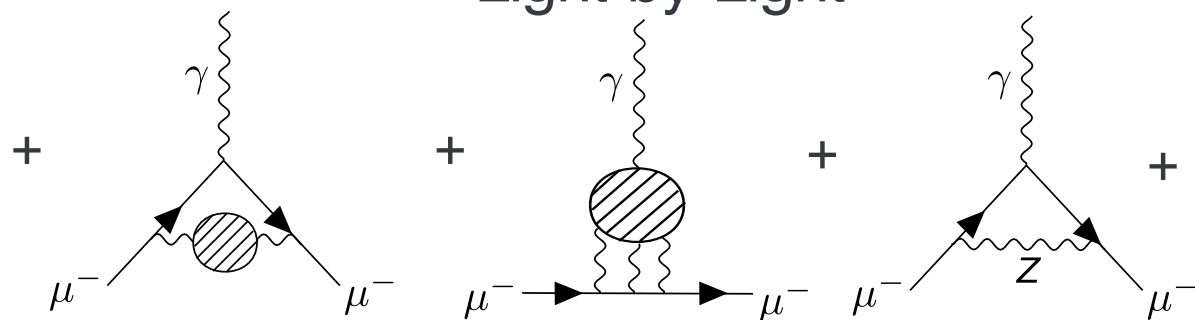
?



Hadronic Vacuum  
Polarization

Hadronic  
Light-by-Light

Electroweak



?



# Muons, Why?

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	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino

## 207 times more massive

Sensitivity of  $g-2$  to heavier particles ( $M$ )

scales with  $\left(\frac{m_l}{M}\right)^2$

$$\left(\frac{m_\mu}{m_e}\right)^2 \cong 43,000$$

Today:  $g_e$  has been measured to 0.13 ppt (!)

$g_\mu$  3 orders of magnitude less precise

$\rightarrow g_\mu$  still  $\sim 38$  times more sensitive to

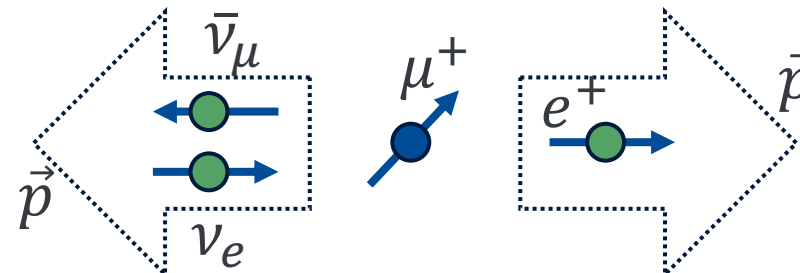
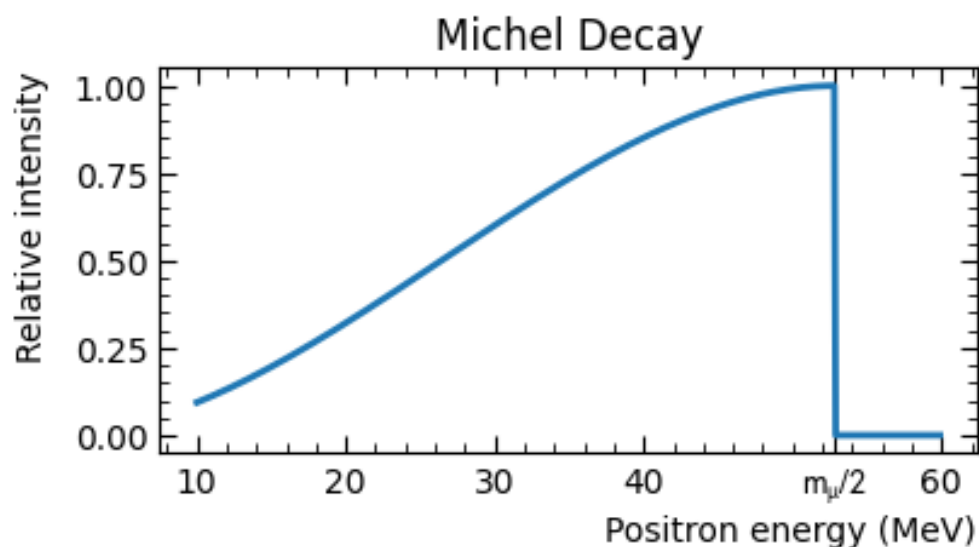
heavy New Physics

# Muons, Why?

## Self-analyzing (parity-violating)

Positrons are preferentially emitted in the direction of the muon's spin

Muon decay:  $\mu \rightarrow e \bar{\nu}_e \nu_\mu$



## Weak force: parity violating

- Produces “right-handed” anti-particles, spin aligned with momentum
- Produces “left-handed” particles, spin anti-aligned with momentum

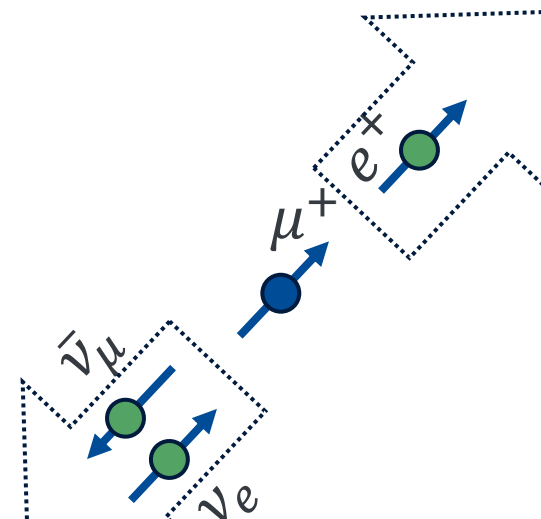
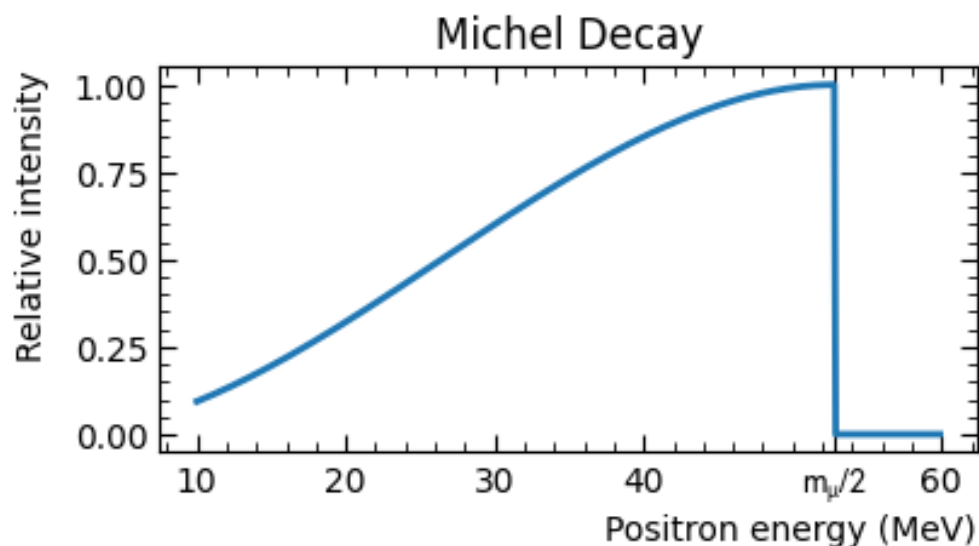


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	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino

**207 times more massive**

than electrons, **more sensitive** to virtual particles

**Self-analyzing** (parity-violating)

Positrons are preferentially emitted in the direction of the muon's spin

**High Statistics**

Feasible to produce at particle accelerators, lifetime of  $2.2 \mu\text{s}$  allows to measure spin precession

# Muon g-2?

all corrections

$$g_\mu = 2.00233184143(290)$$

$$g_\mu - 2$$

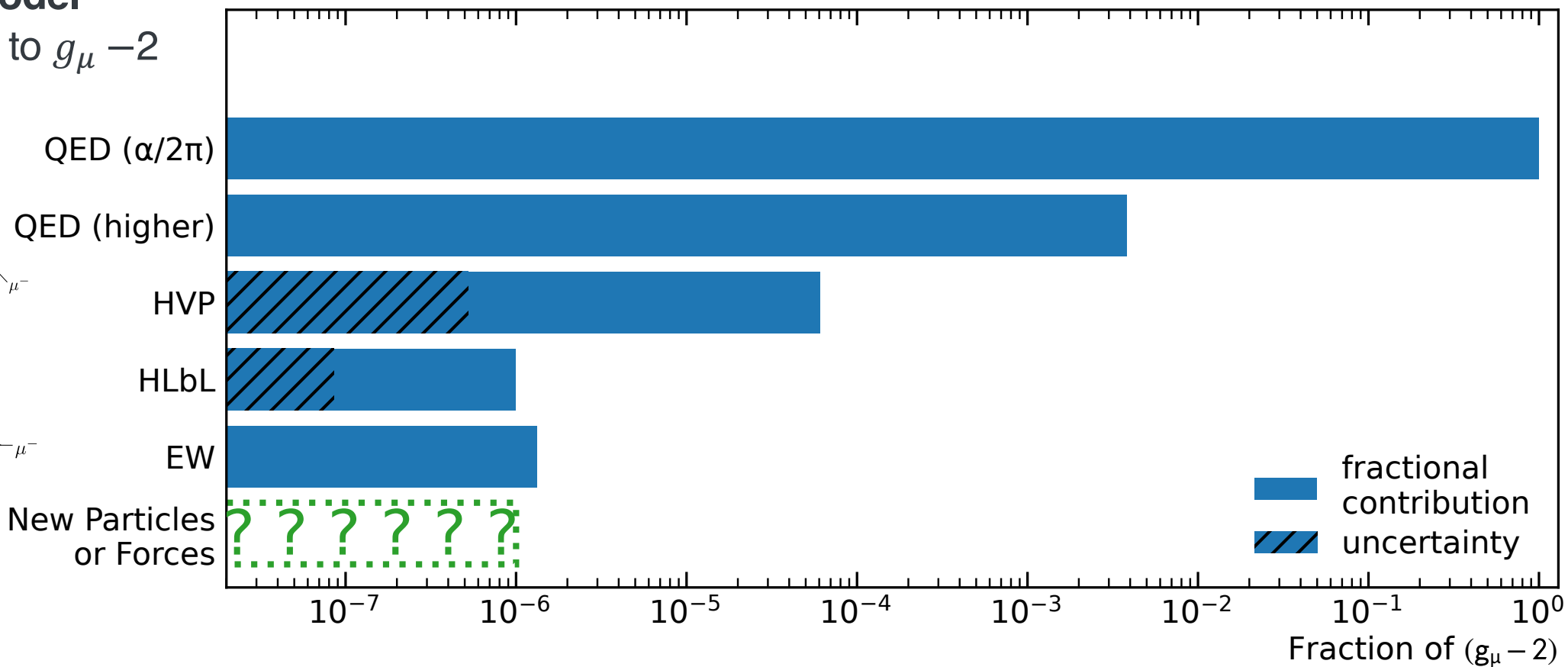
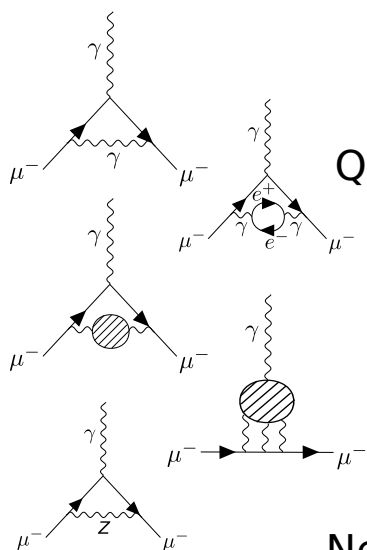
**Muon Anomaly:**

$$a_\mu \equiv \frac{g_\mu - 2}{2}$$



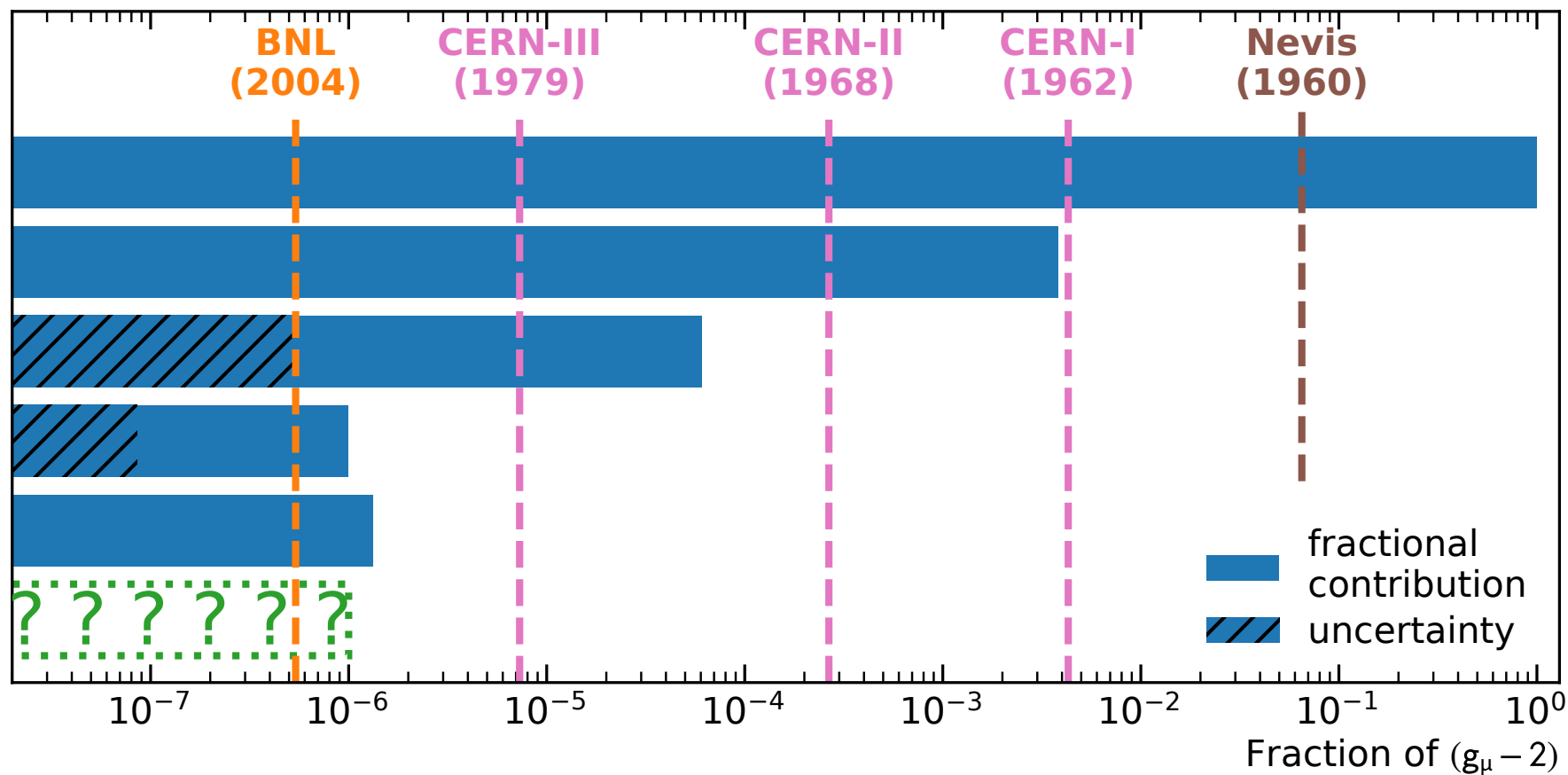
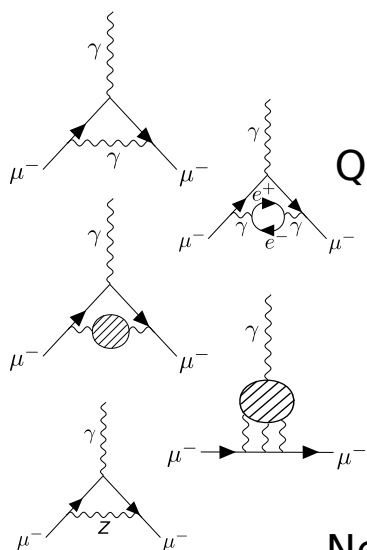
# Measure Muon $g-2$ to **test** the Standard Model

Standard Model  
components to  $g_\mu - 2$



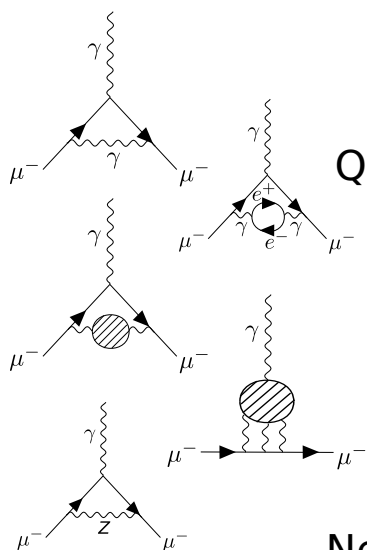
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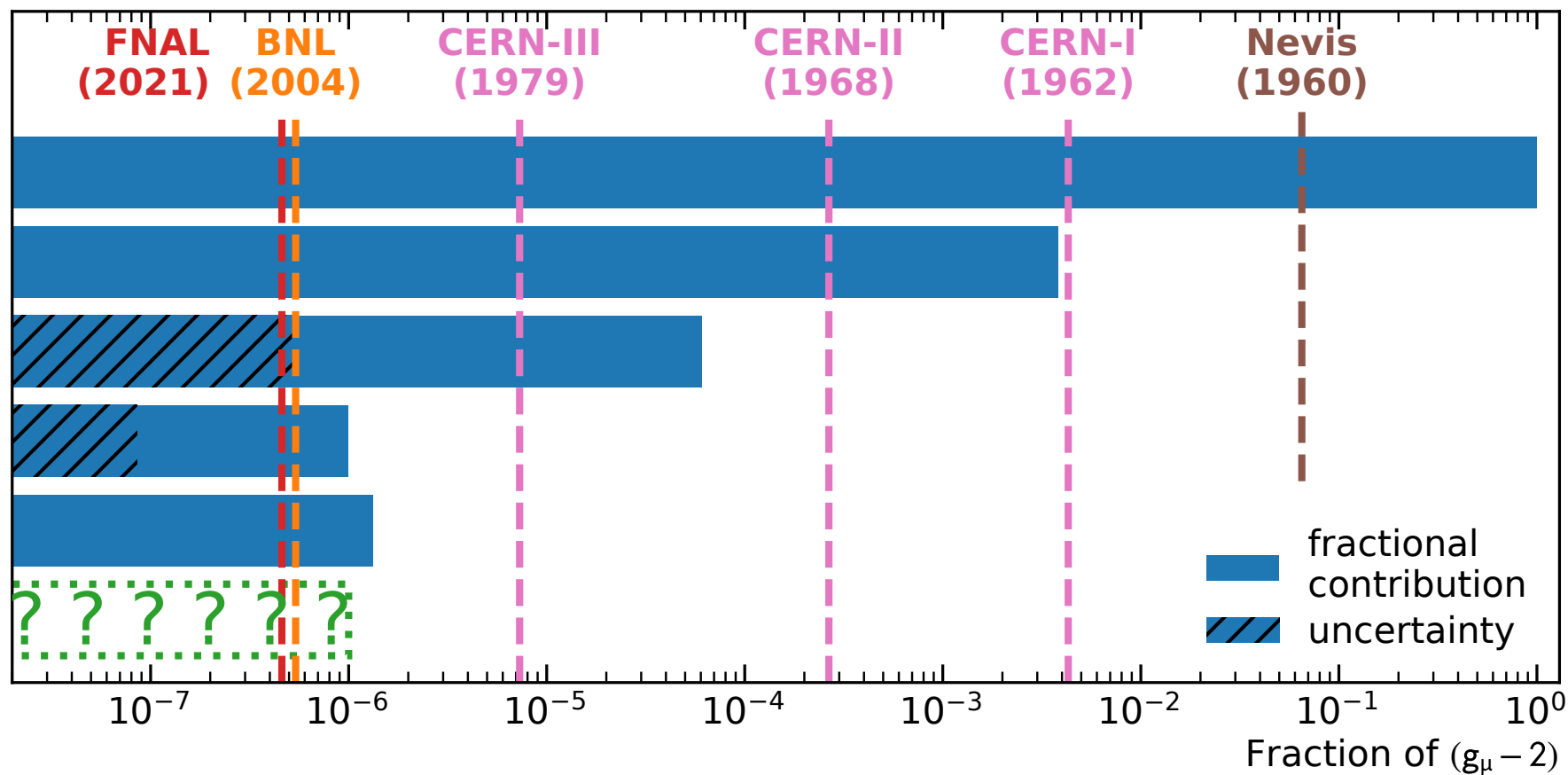


# Measure Muon $g-2$ to **test** the Standard Model

Standard Model  
components to  $g_\mu - 2$



New Particles  
or Forces

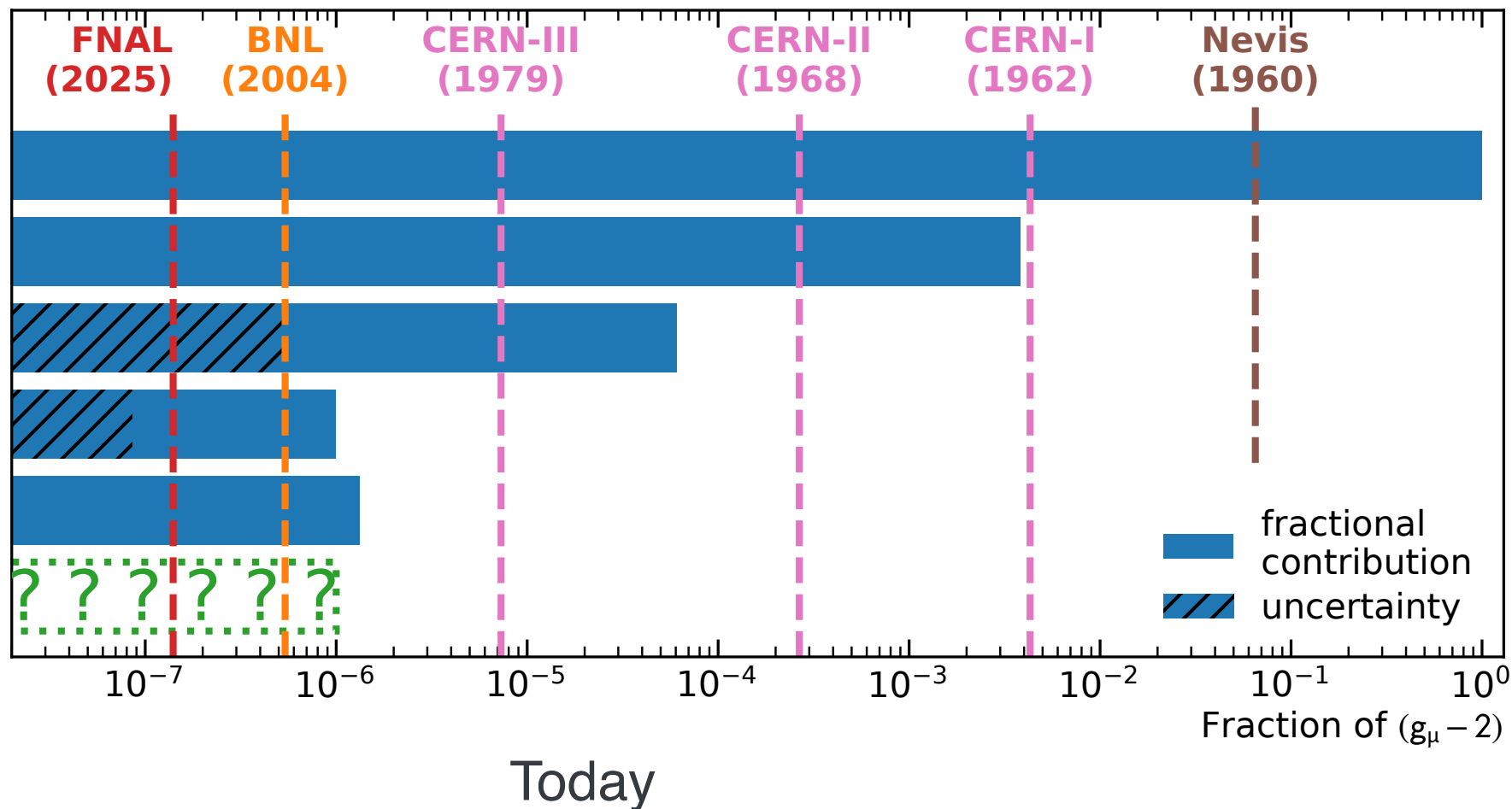
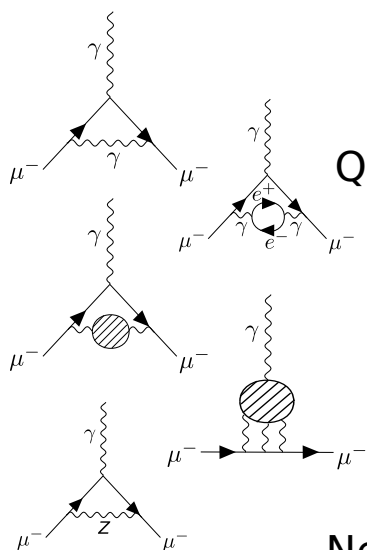


2021: Muons made News!



# Measure Muon $g-2$ to **test** the Standard Model

Standard Model  
components to  $g_\mu - 2$

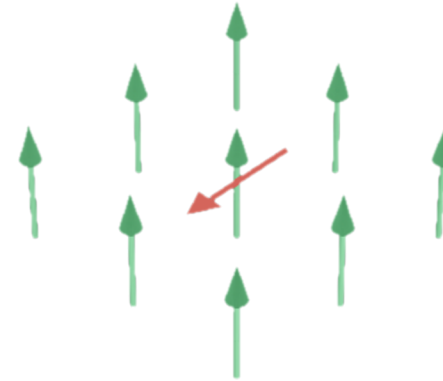


# Measurement

Muon Spin precession in  
uniform magnetic field

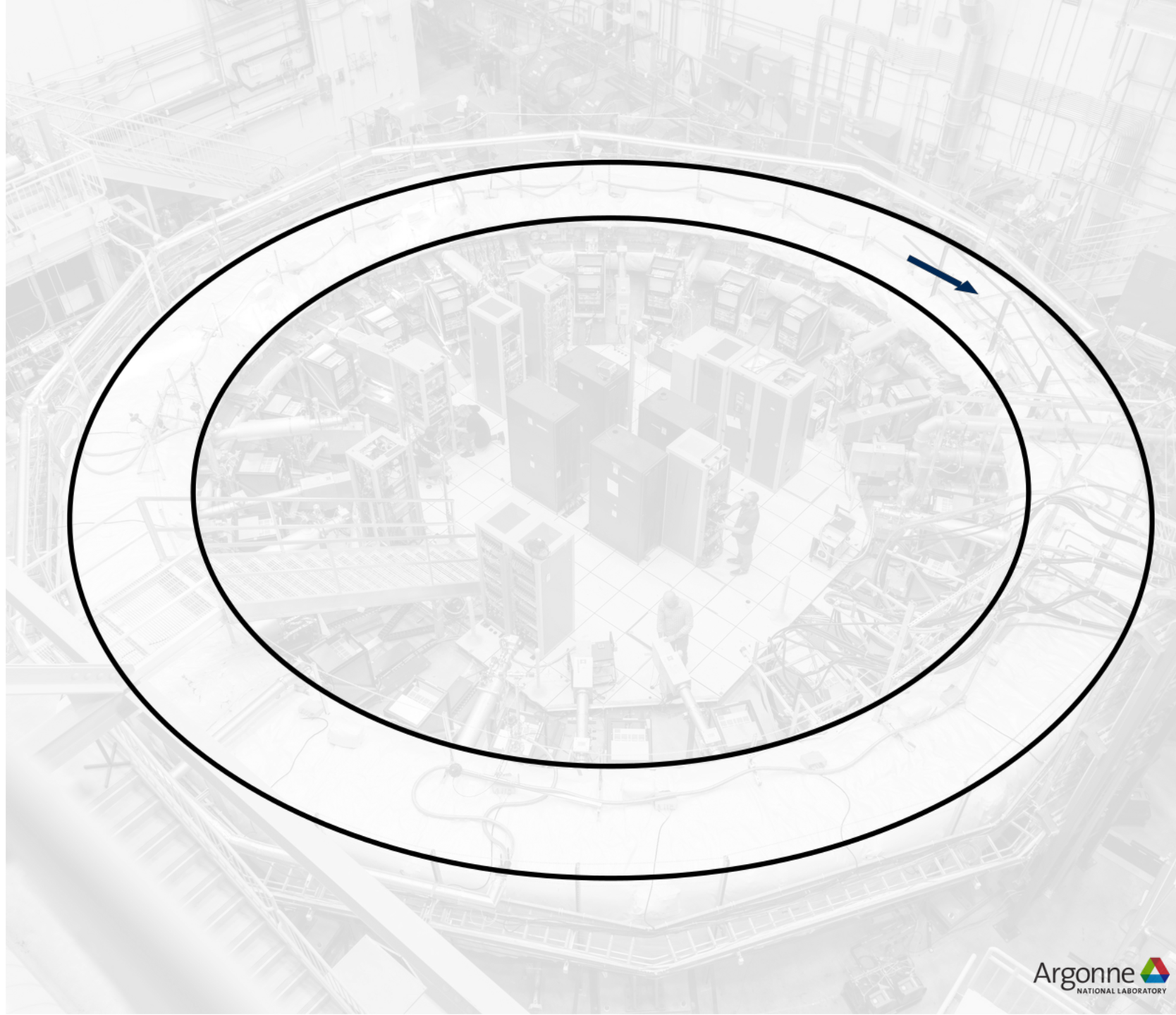
**Spin:**

$$\vec{\omega}_s = \frac{g_\mu}{2} \frac{e}{mc} \vec{B}$$



# Measurement Principal

Store **Polarized Muons**



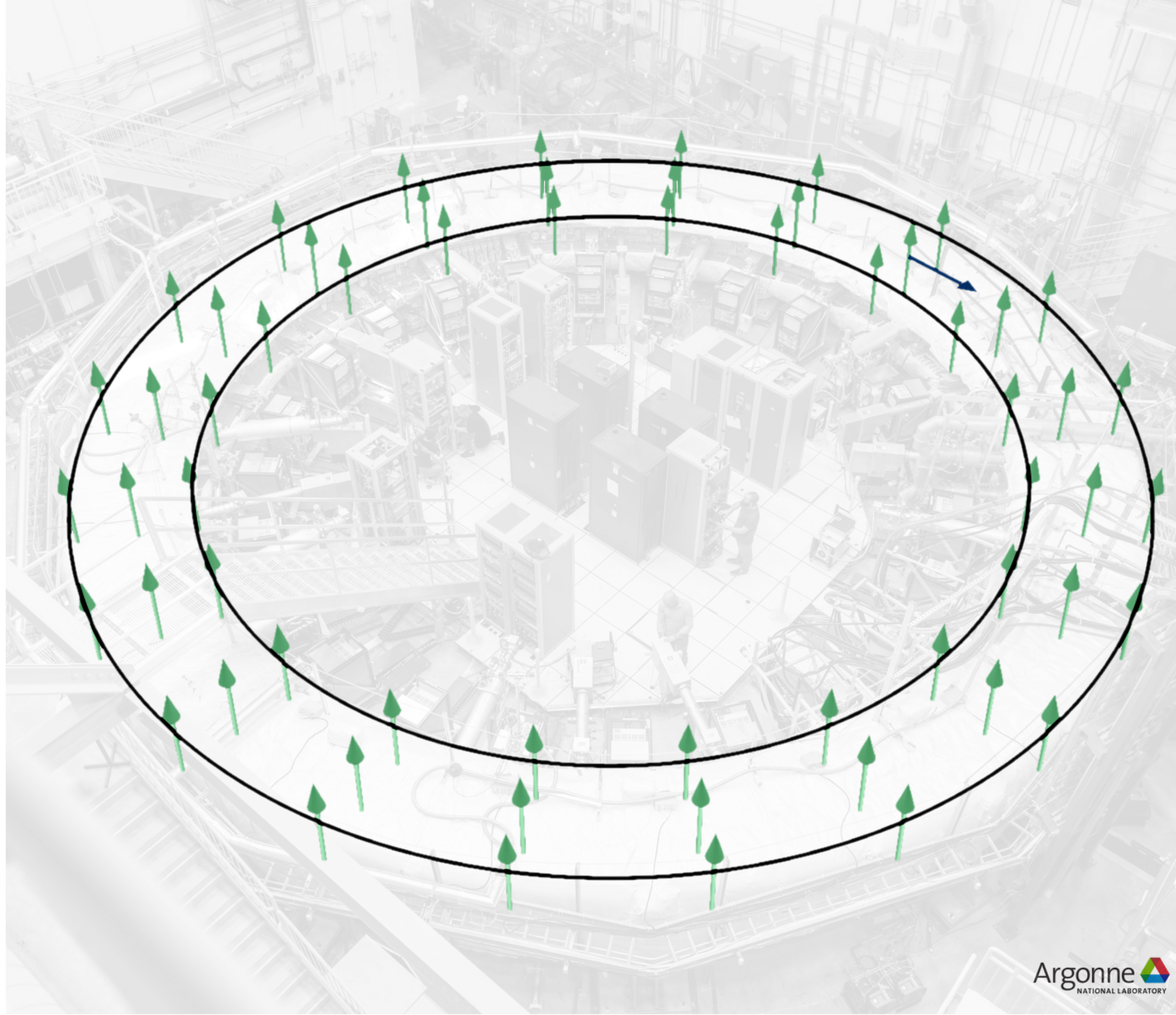


# Measurement Principal

Store **Polarized Muons** in  
a **Dipole Magnetic Field**

Momentum: 

$$\vec{\omega}_c = \frac{e}{mc} \vec{B}$$



# Measurement Principal

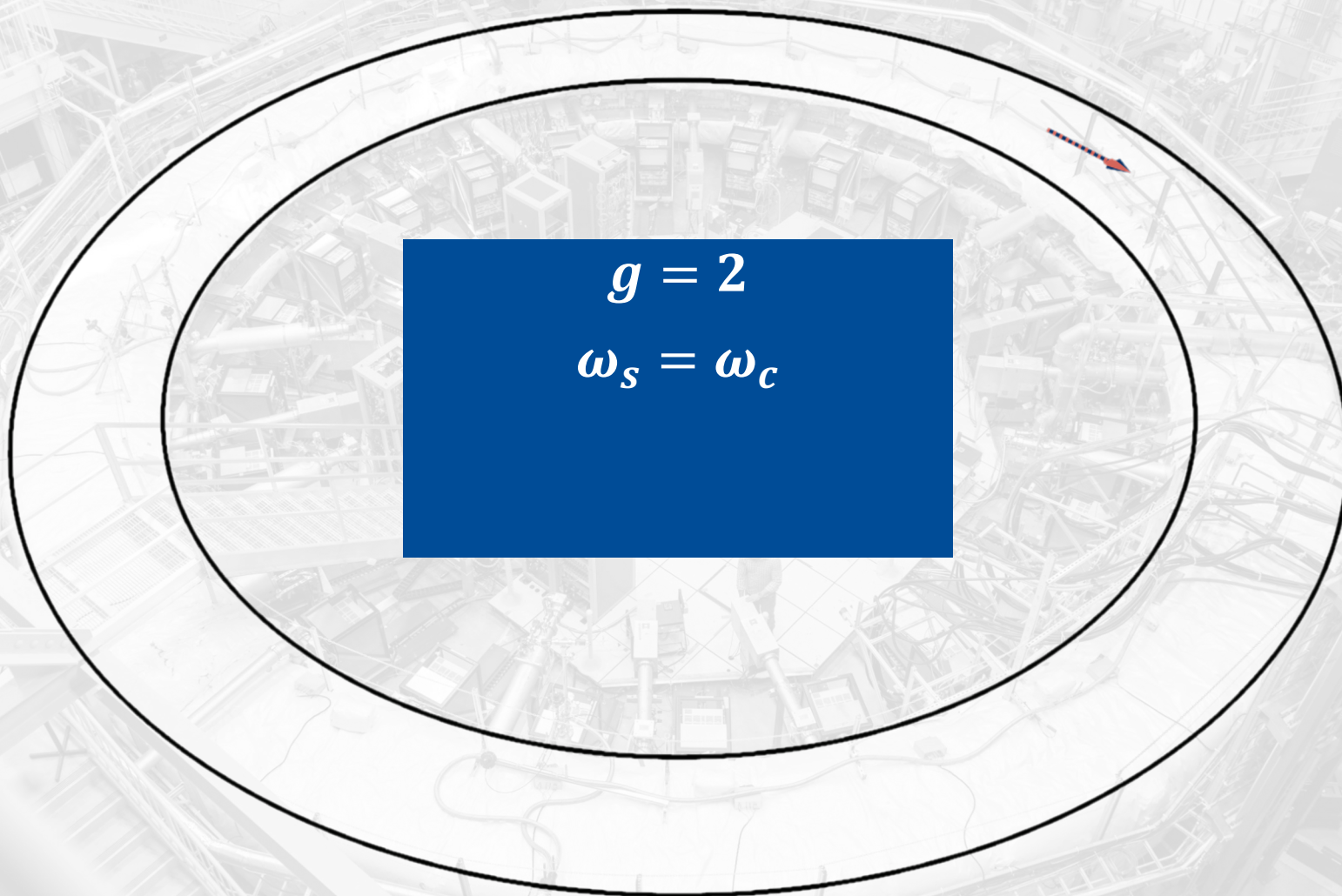
Store **Polarized Muons** in  
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Momentum: 

$$\vec{\omega}_c = \frac{e}{mc} \vec{B}$$

Spin: 

$$\vec{\omega}_s = \frac{g_\mu}{2} \frac{e}{mc} \vec{B}$$





# Measurement Principal

Store **Polarized Muons** in  
a **Dipole Magnetic Field**

Momentum: 

$$\vec{\omega}_c = \frac{e}{mc} \vec{B}$$

Spin: 

$$\vec{\omega}_s = \frac{g_\mu}{2} \frac{e}{mc} \vec{B}$$

$$g > 2$$

$$\begin{aligned}\omega_a &= \omega_s - \omega_c \\ &= \frac{g_\mu - 2}{2} \frac{e}{mc} B\end{aligned}$$



$$\omega_a = a_\mu \frac{e}{mc} B$$

Measure:  $\omega_a, B$

Extract:  $a_\mu$

$$a_\mu \equiv \frac{g_\mu - 2}{2}$$

Magnetic Anomaly

$$\tilde{\omega}'_p = \gamma'_p B$$

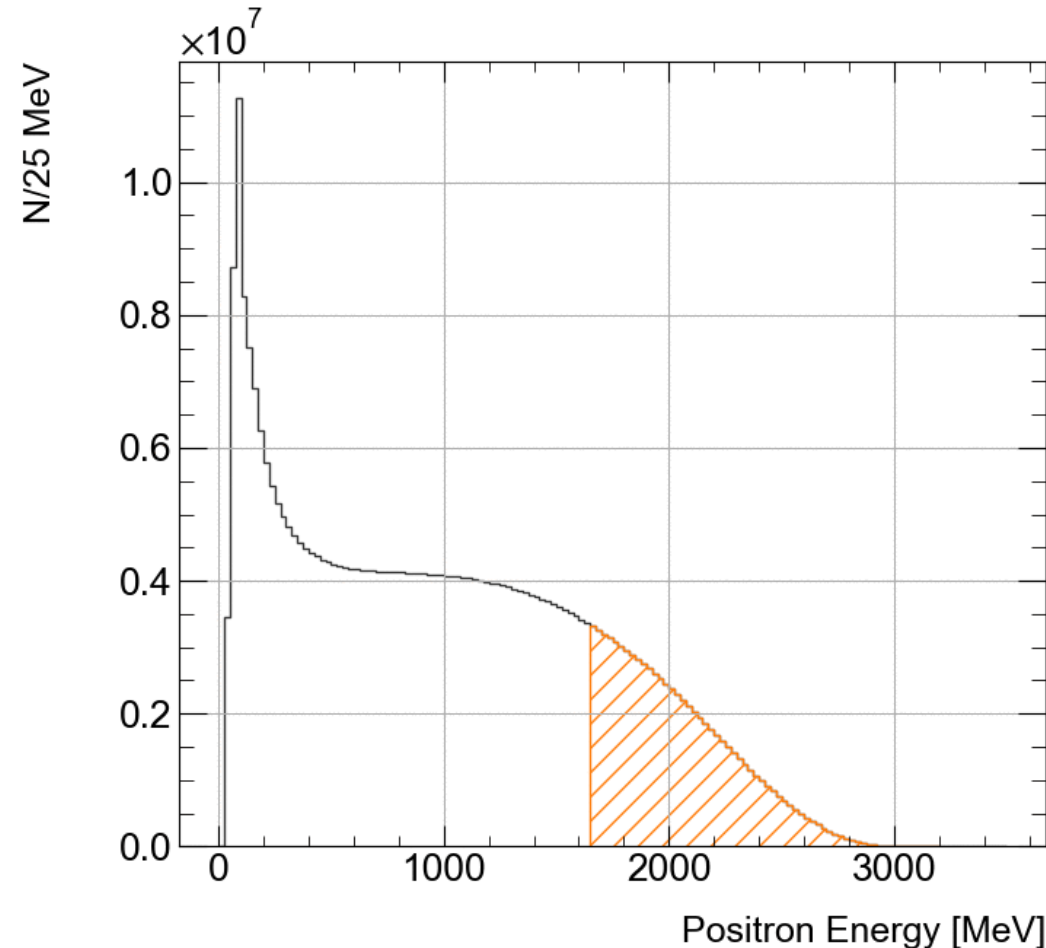
$\gamma'_p$ : Gyromagnetic ratio of shielded **protons**

Measure the **magnetic field** in terms  
the **precession frequency of protons**

Nuclear Magnetic Resonance (NMR)

# ⚙ Measuring the Spin Precession $\omega_a$

Due to parity violation, “self-analyzing”,  
the number of **high energy**  $e^+$  oscillates as  
the  $\mu^+$  spin rotates

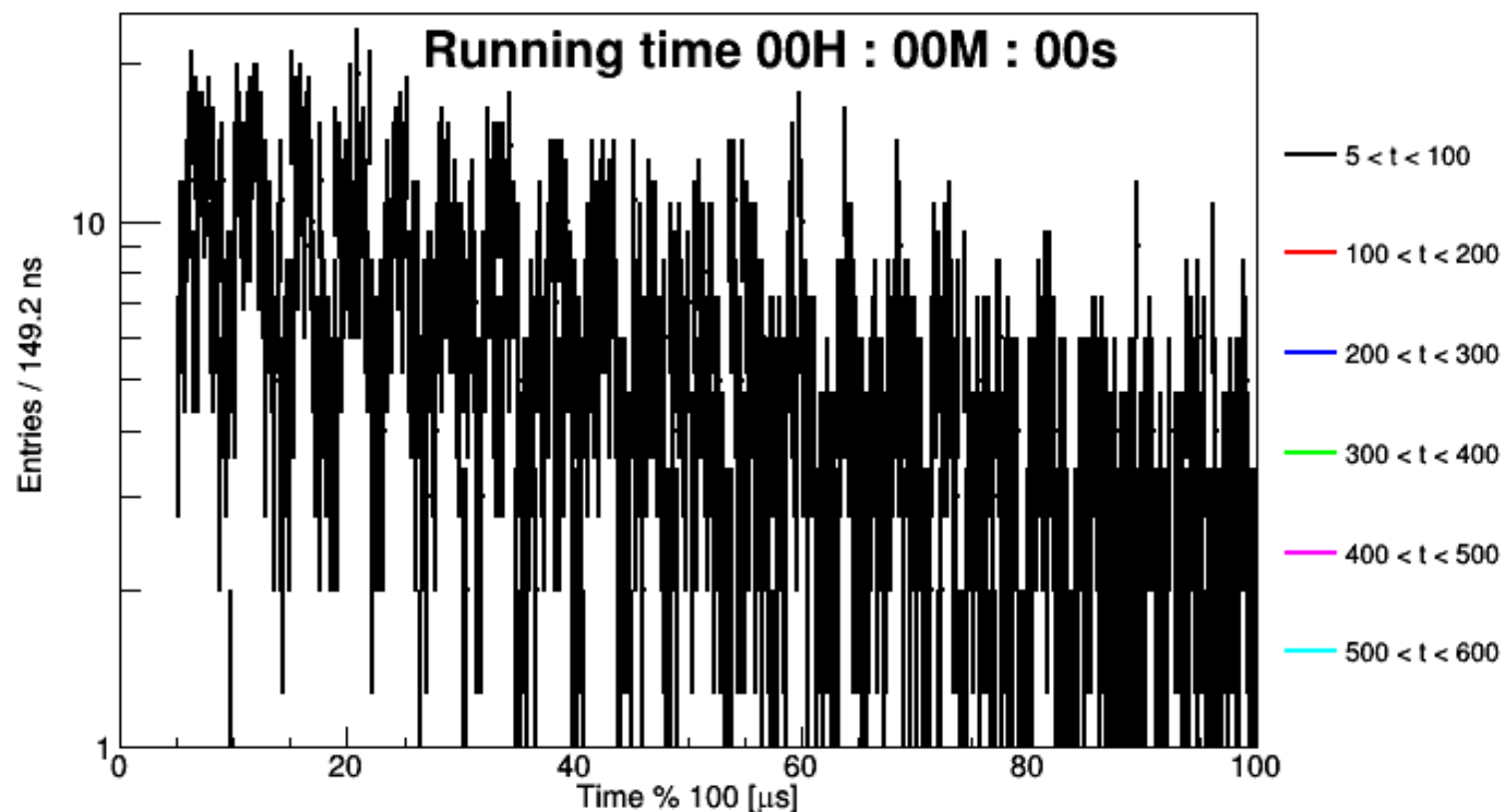




# Measuring the Spin Precession $\omega_a$

Simplest fit model captures **exponential decay** & **g-2 oscillation**

$$N(t) = N_0 e^{-t/\tau} [1 + A \cos(\omega_a t - \phi_0)]$$

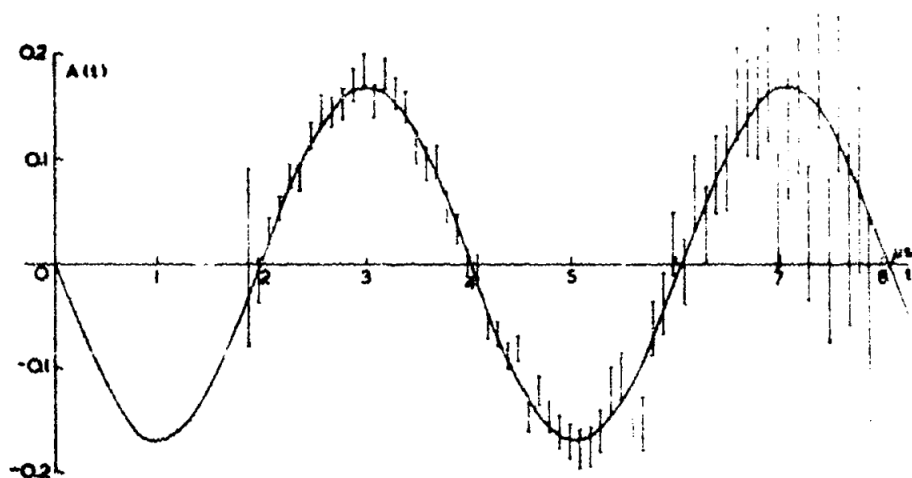


# The Storage Ring Technique

## CERN I (1962)

Direct measurement of

$$a_{\mu} = \frac{g-2}{2}$$

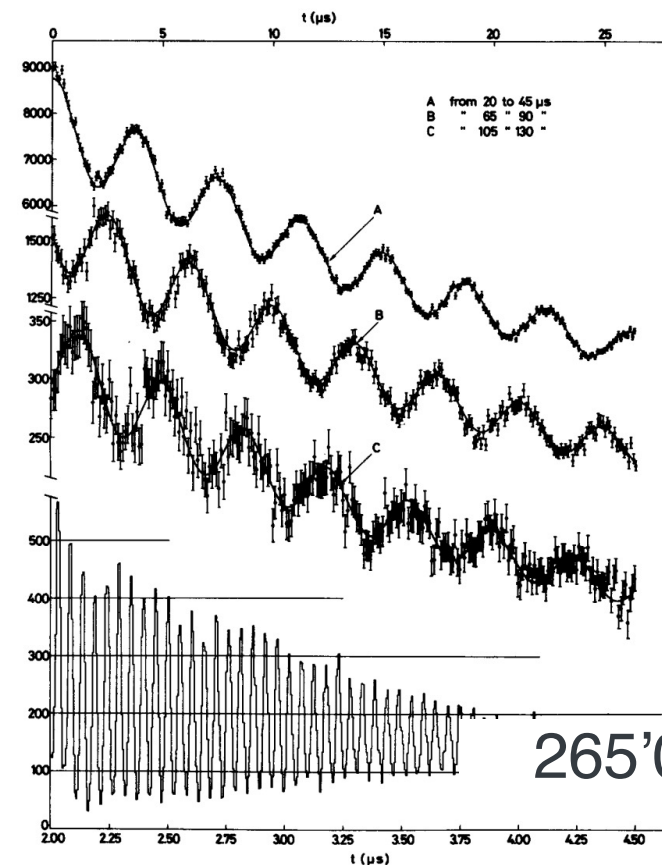


4'300'000 ppb

[https://doi.org/10.1016/0031-9163\(62\)90263-9](https://doi.org/10.1016/0031-9163(62)90263-9)

## CERN II (1968)

Pioneered Storage Ring technique, increased statistics!



265'000 ppb

[https://doi.org/10.1016/0370-2693\(68\)90261-X](https://doi.org/10.1016/0370-2693(68)90261-X)



# The Magic Momentum

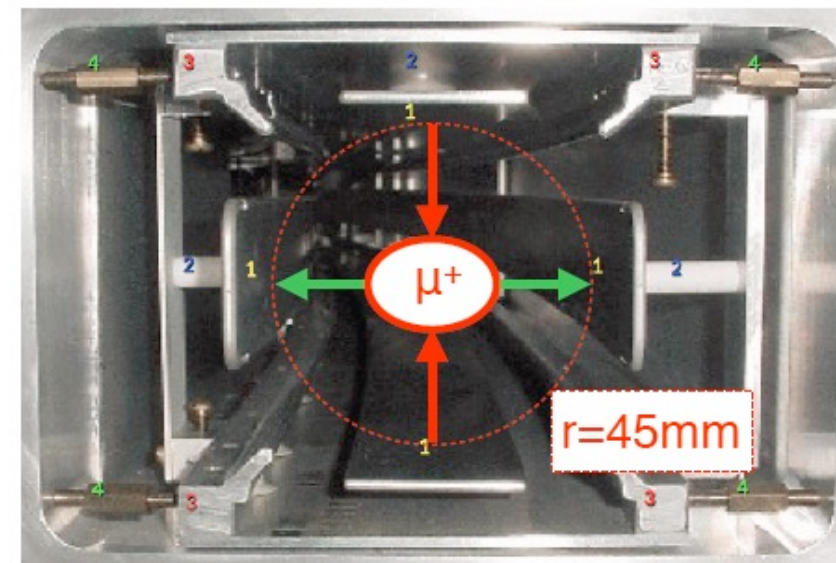
$$\vec{\omega}_a \approx \frac{e}{m} \left( a_\mu \vec{B} + \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right)$$

$\sim 0$

Measure:  $\omega_a, B$

Extract:  $a_\mu$

**Magic Momentum:** 3.1 GeV/c,  $\gamma = 29.3$   
Electric-Field term cancels

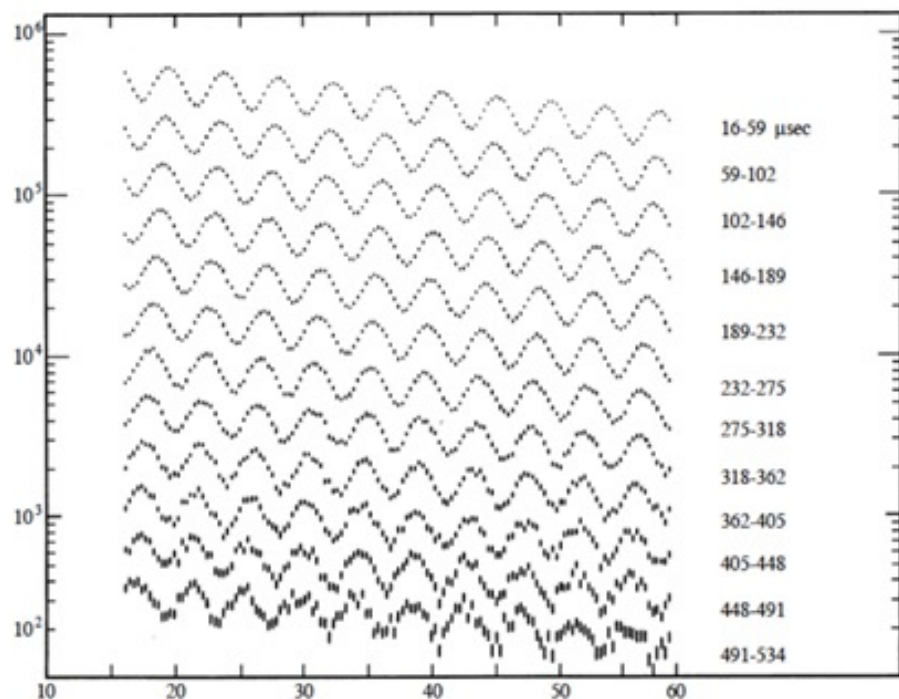


Focus muon beam with  
electric fields!

# The Magic Momentum Era

**CERN III (1979)**

Pioneered Magic Momentum

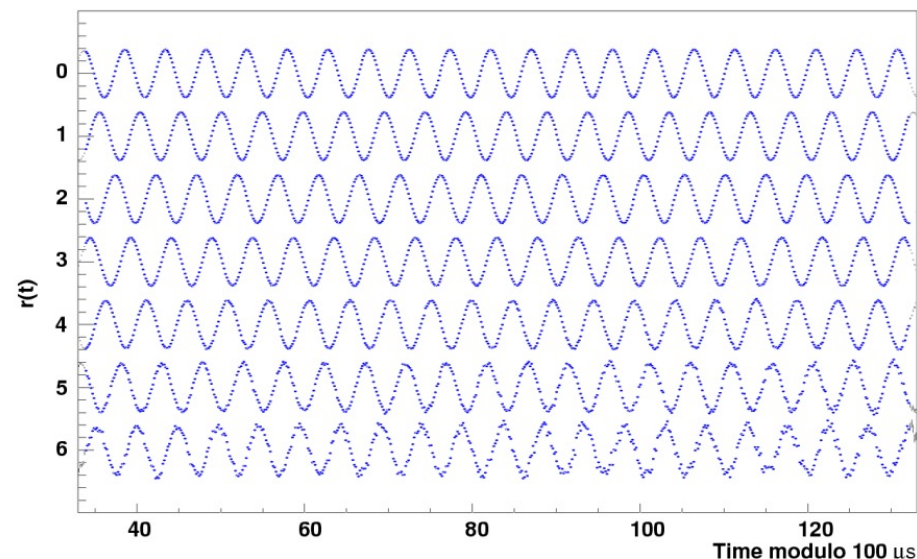


7'000 ppb

[https://doi.org/10.1016/0550-3213\(79\)90292-X](https://doi.org/10.1016/0550-3213(79)90292-X)

**BNL (2004)**

Direct muon injection



540 ppb

<https://link.aps.org/doi/10.1103/PhysRevD.73.072003>



# 2013: The Big Move



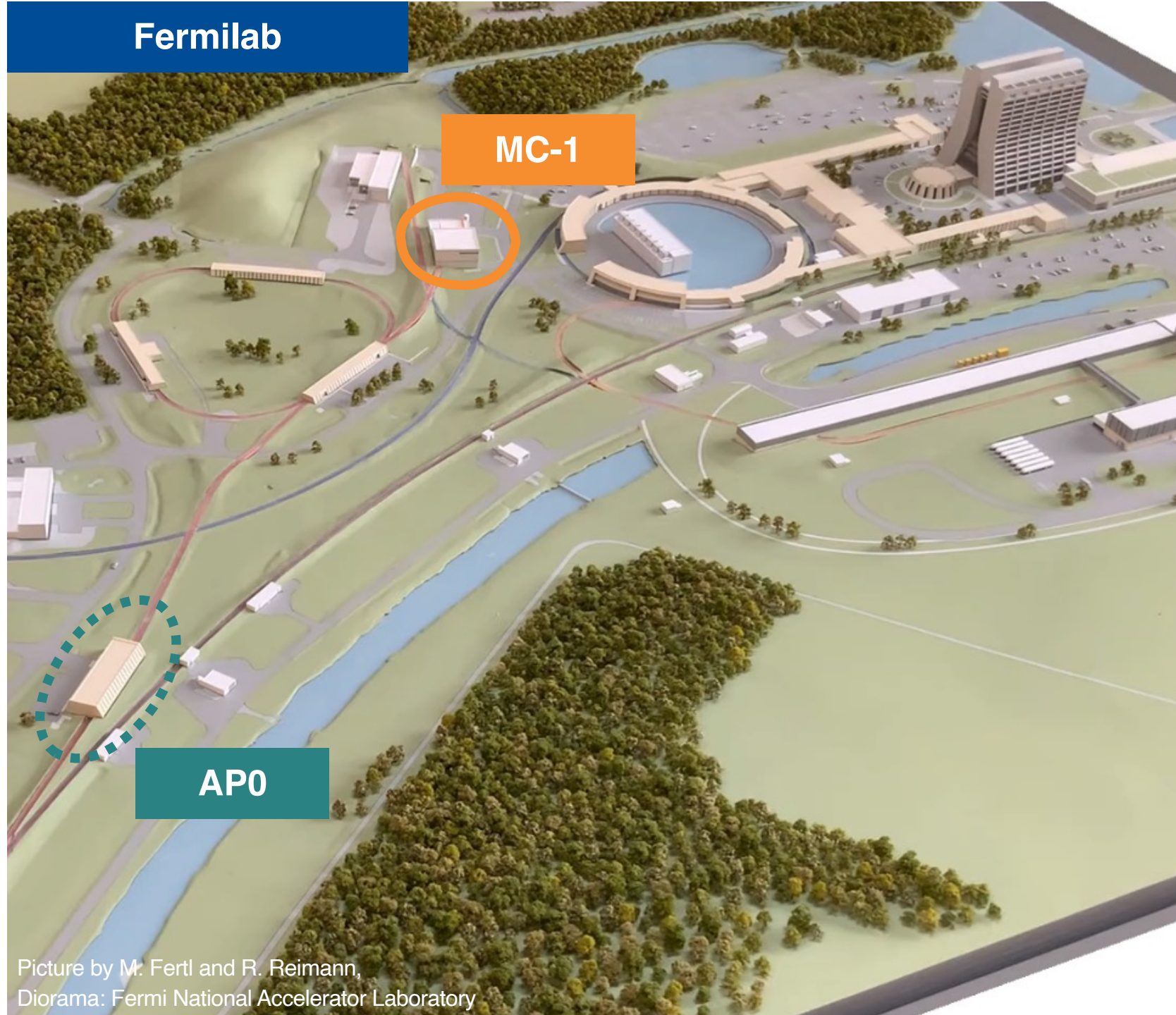


# Fermilab Muon Campus

Polarized 3.1 GeV/c  
“magic momentum”  
Muons to the **MC-1** building

from pions produced at the  
**target hall** (AP0) from 8 GeV/c  
protons from the Main Injector

2x8 bunches, every ~1.4s

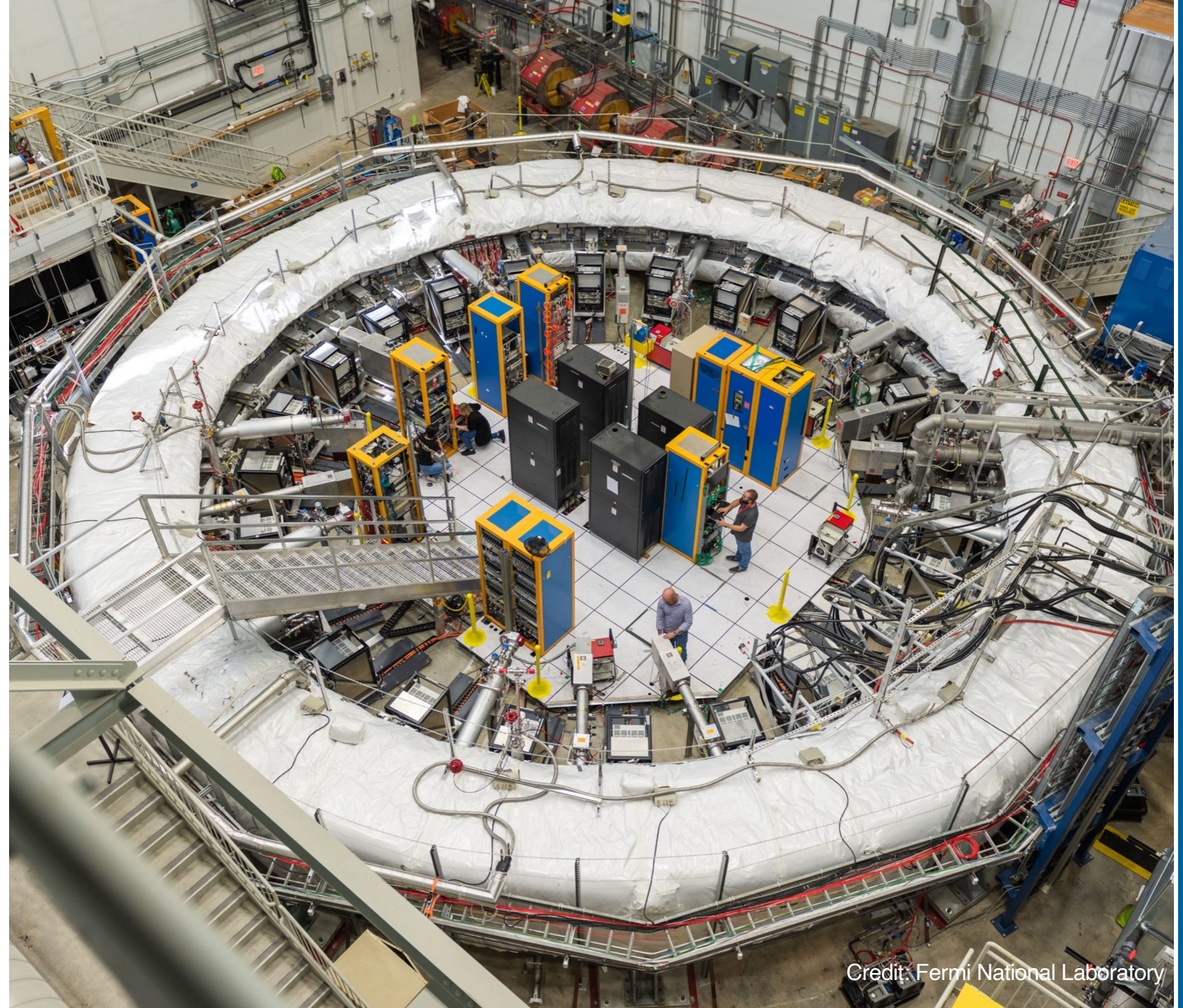
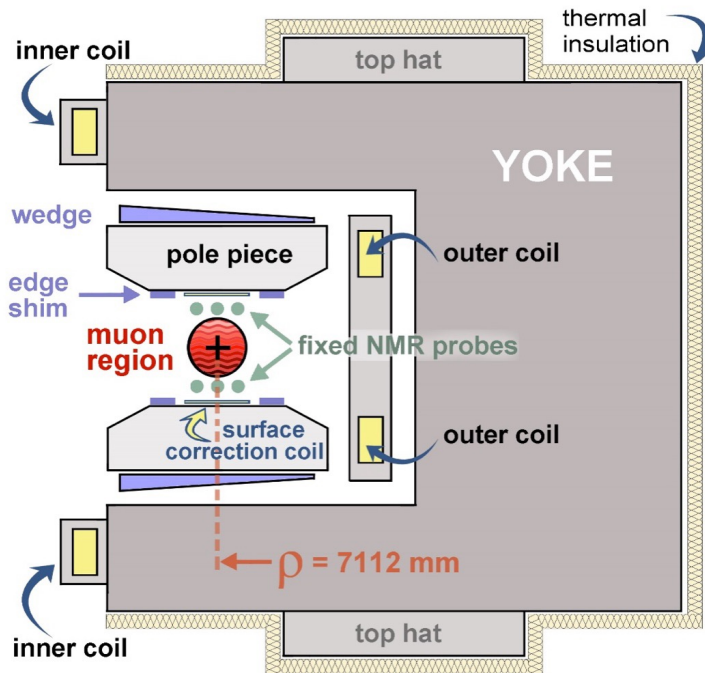


Picture by M. Fertl and R. Reimann,  
Diorama: Fermi National Accelerator Laboratory



# Measurement Principal

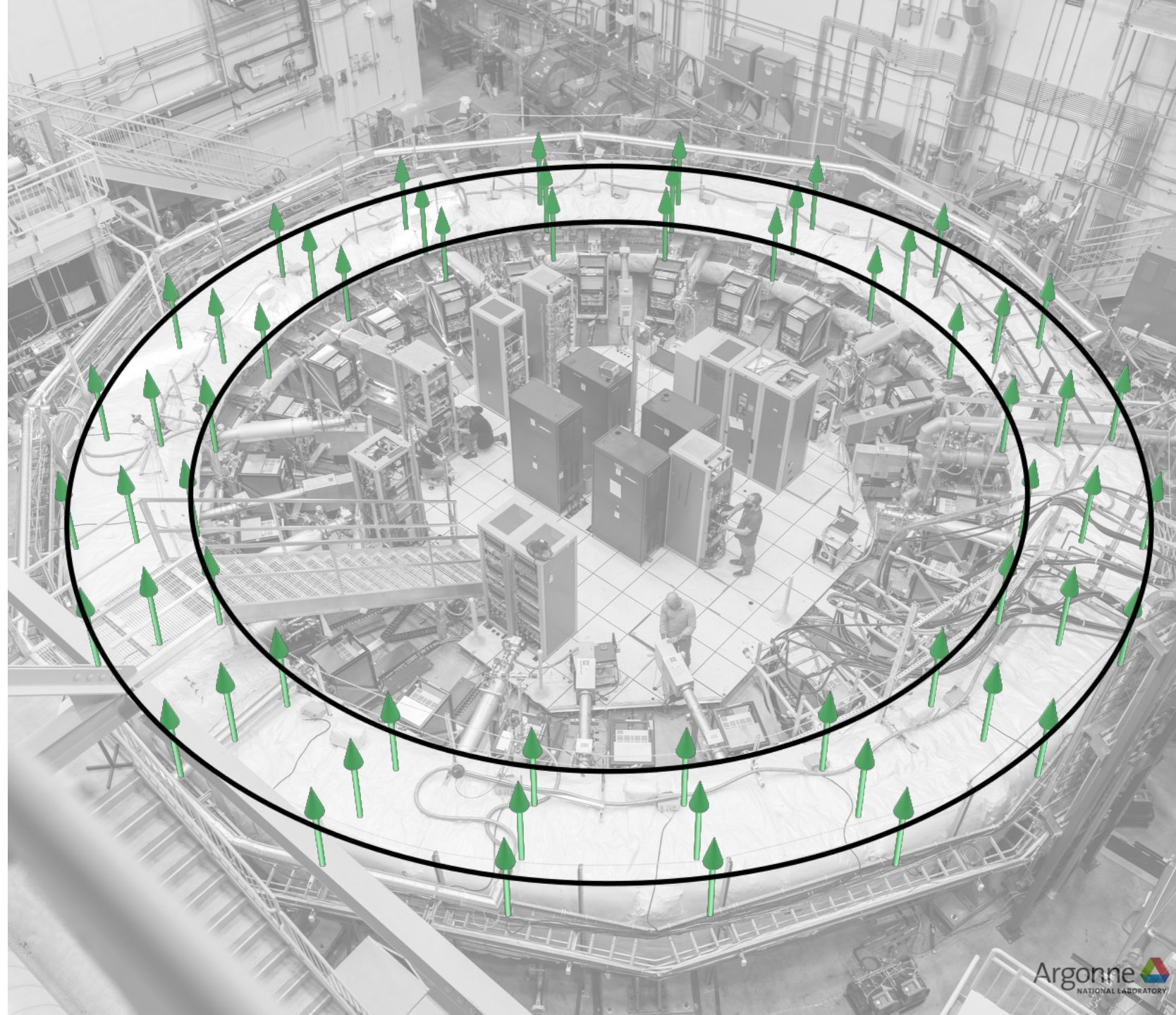
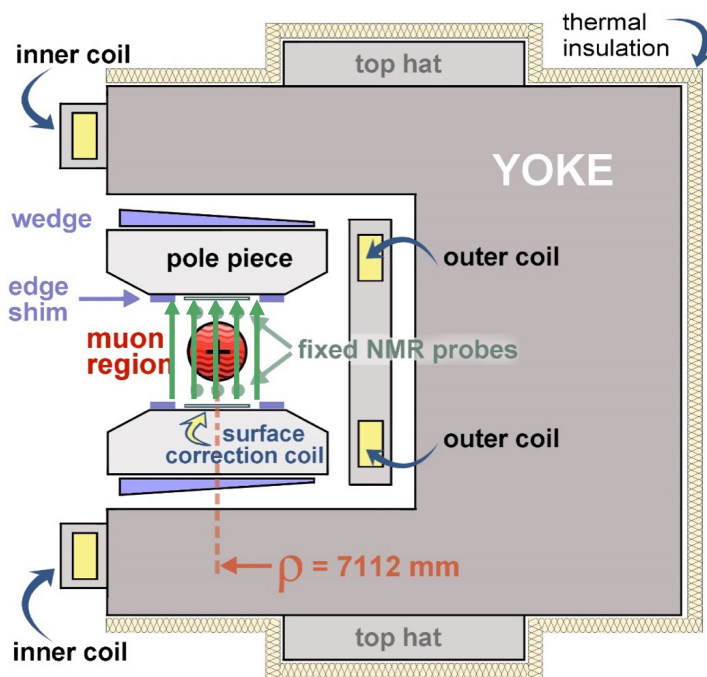
- Superconducting 1.45 T
- Designed and optimized for homogeneity





# Measurement Principal

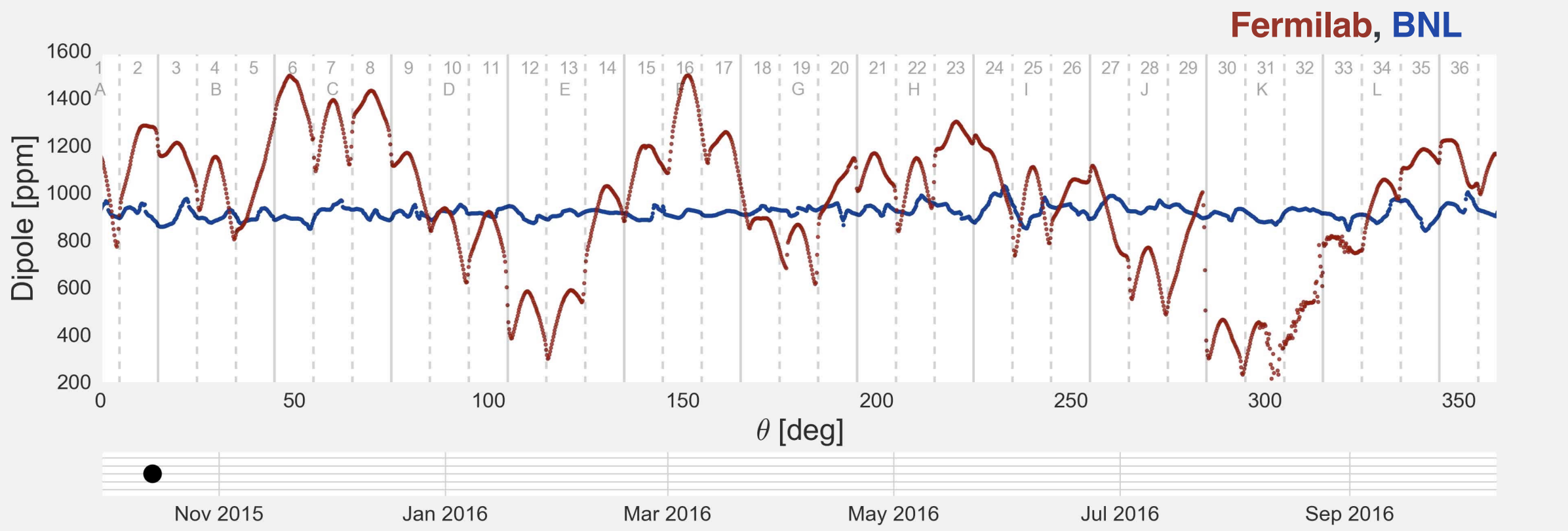
- Superconducting 1.45 T
- Designed and optimized for homogeneity





# Magnetic Field Shimming

(Long) before any muons entered the ring

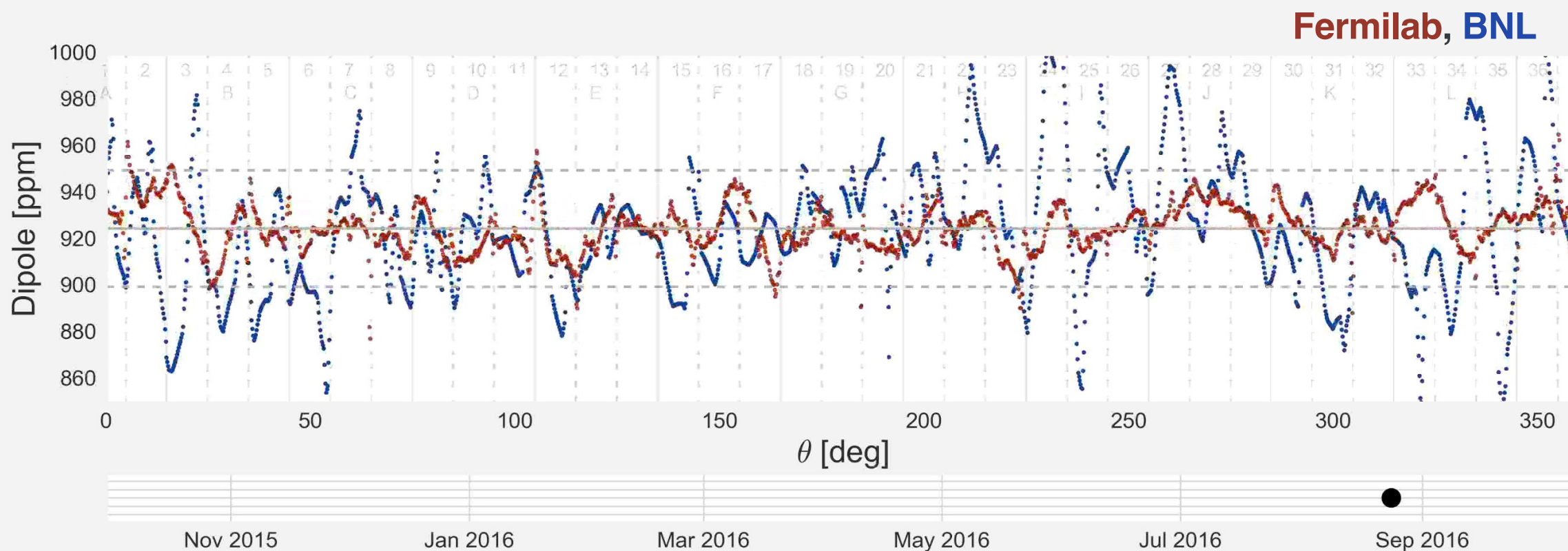






# Magnetic Field Shimming

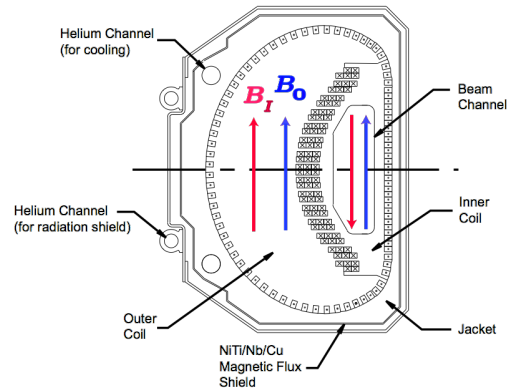
(Long) before any muons entered the ring



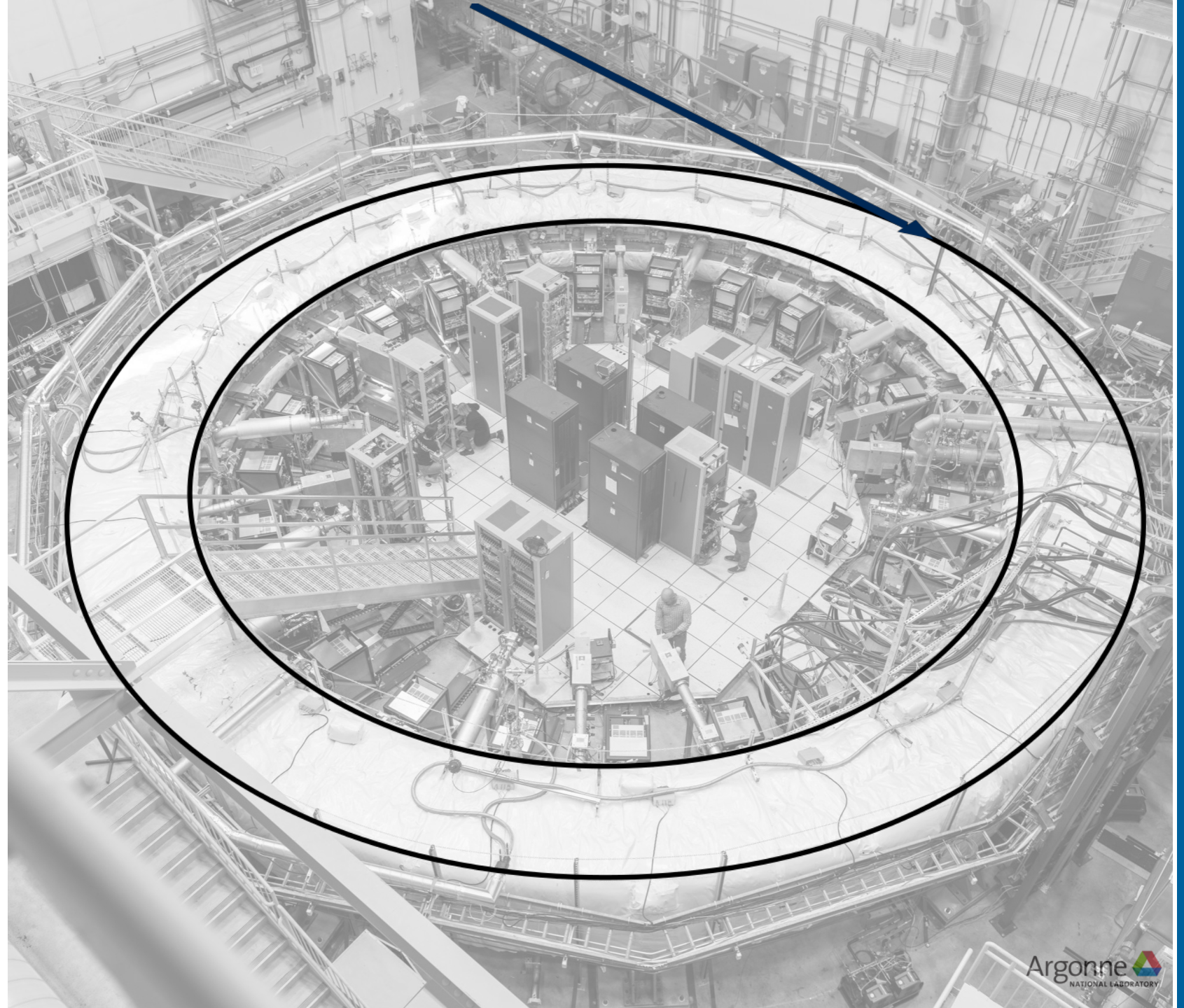


# Injection

Field-free injection  
path through **inflexor**  
magnet



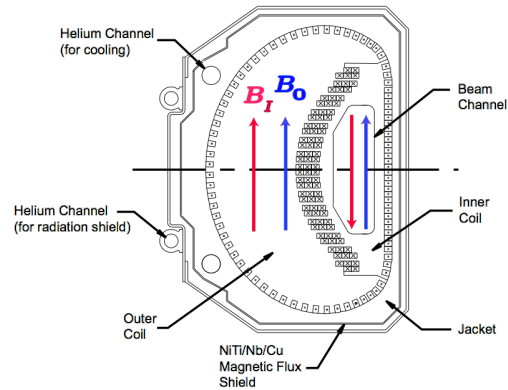
**8 cm offset**  
from storage center



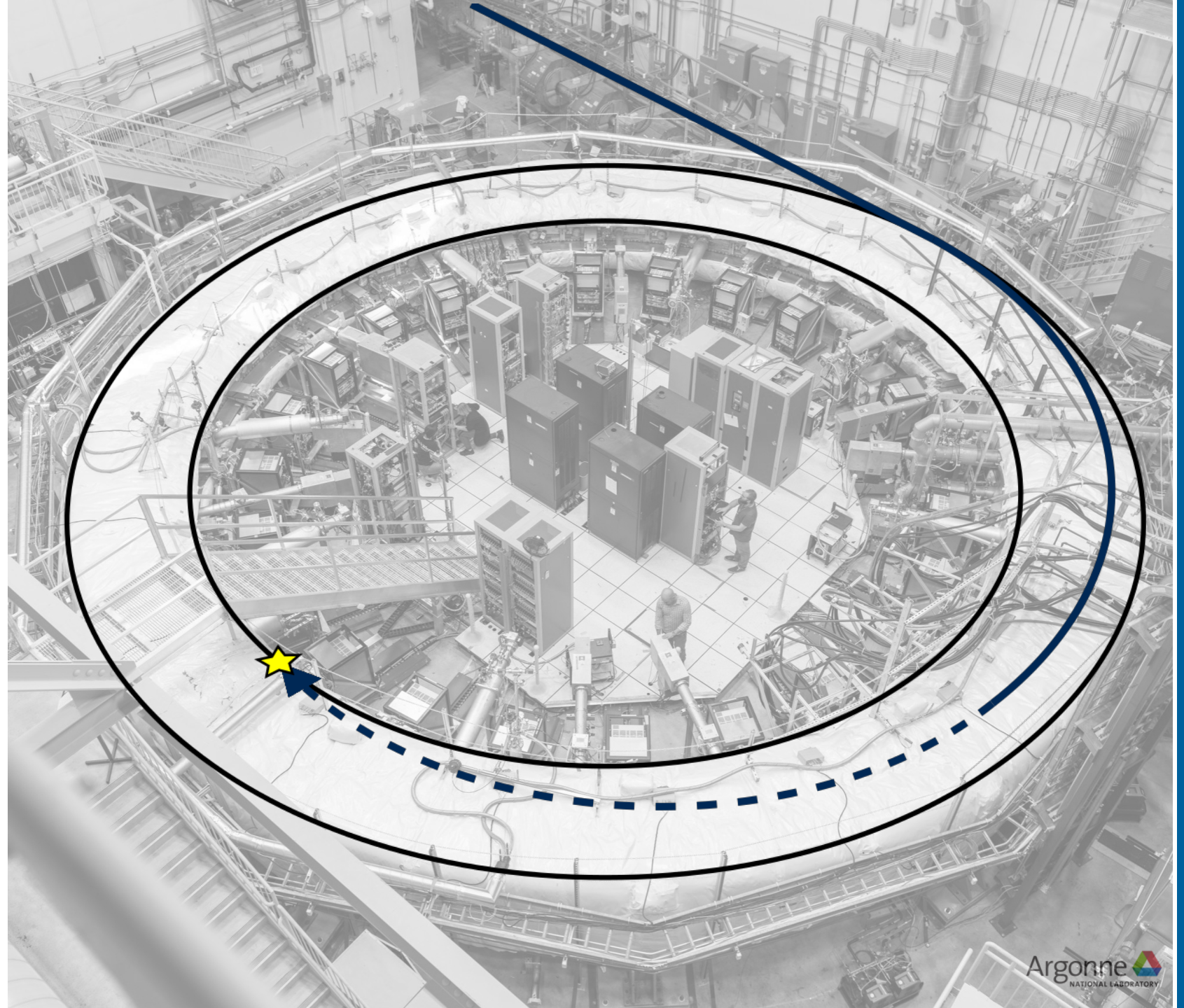


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Field-free injection  
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magnet



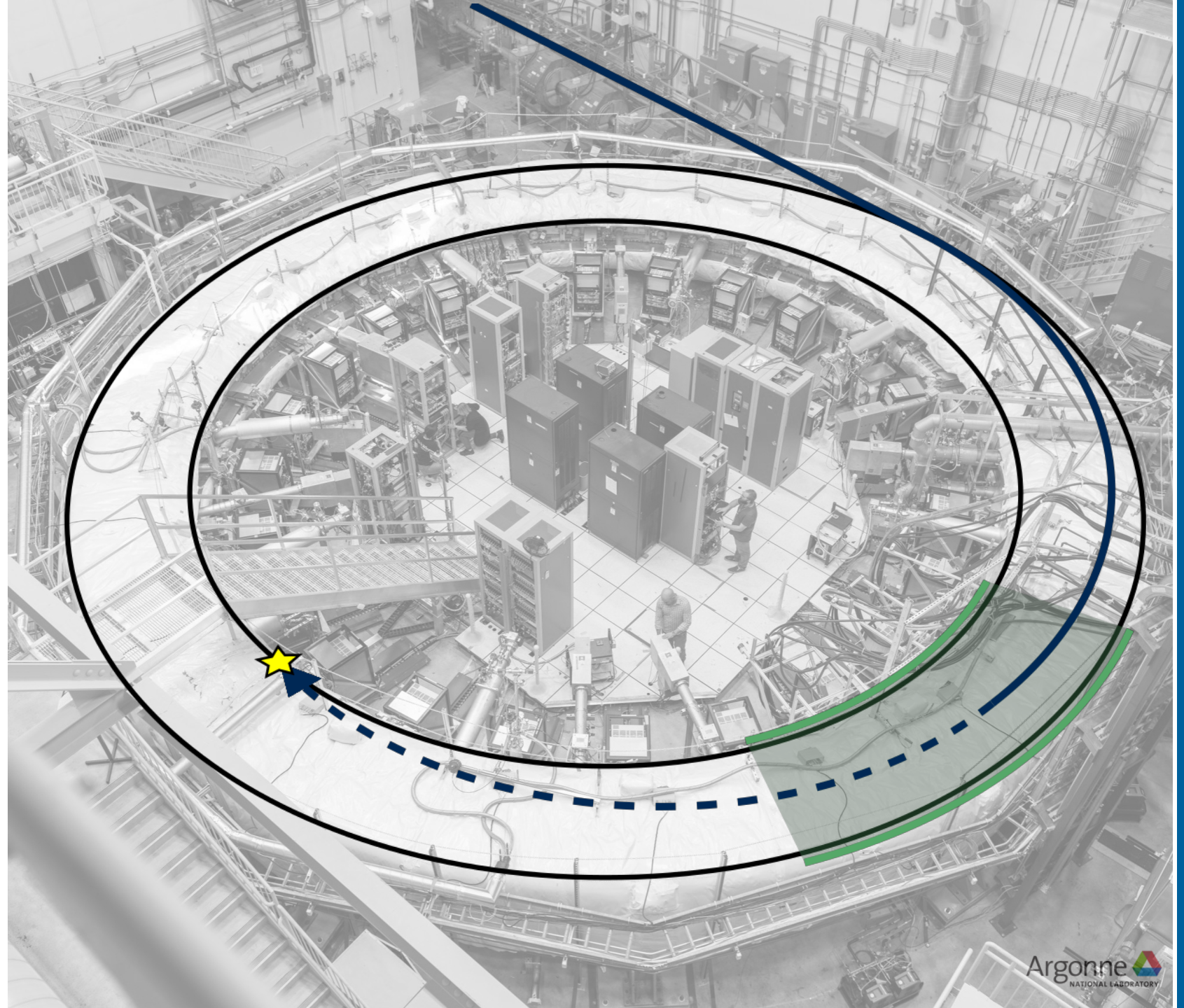
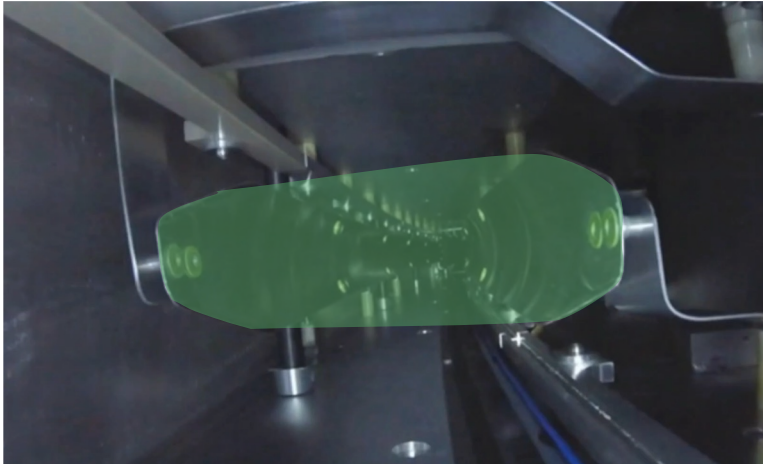
**8 cm offset**  
from storage center







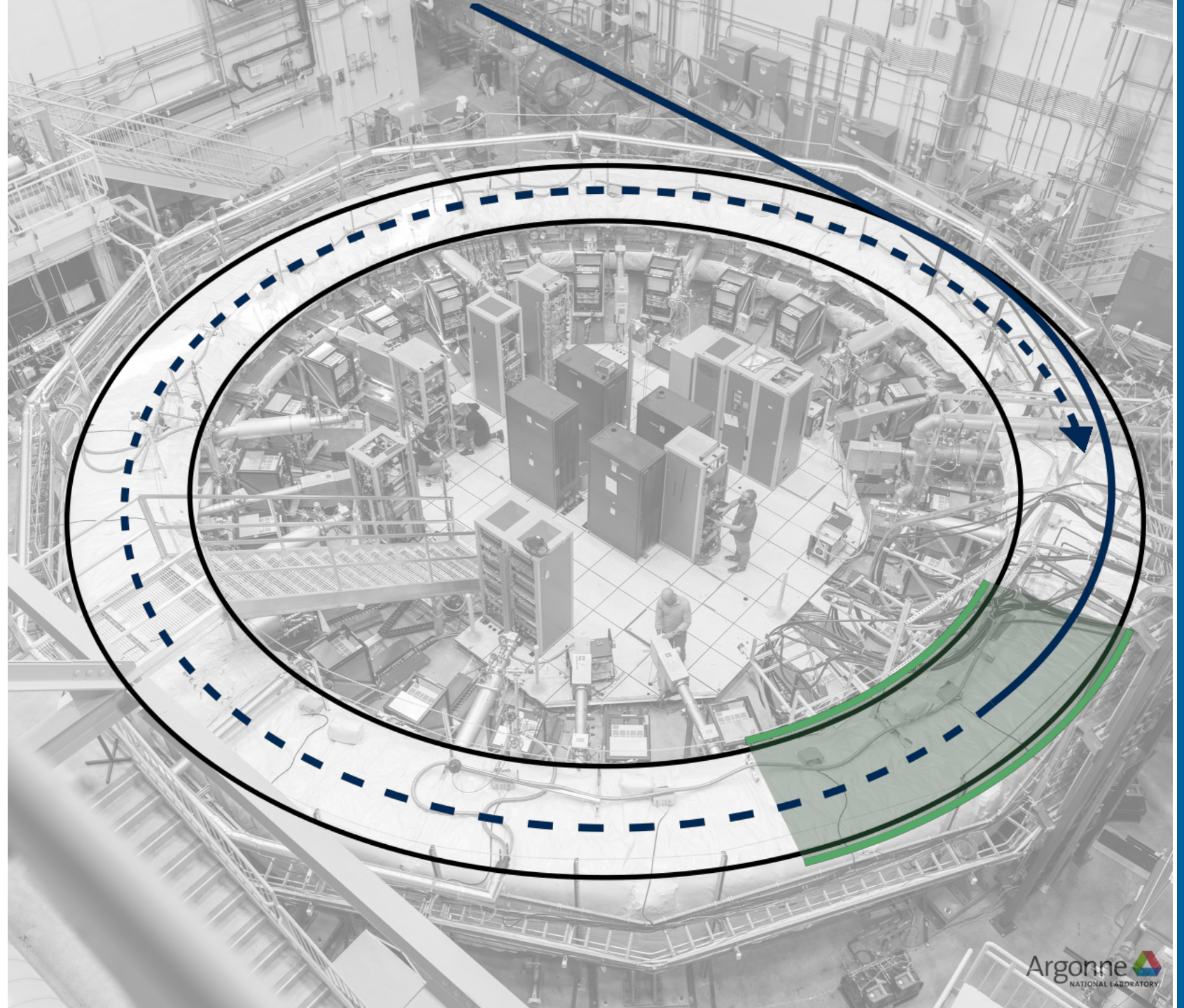
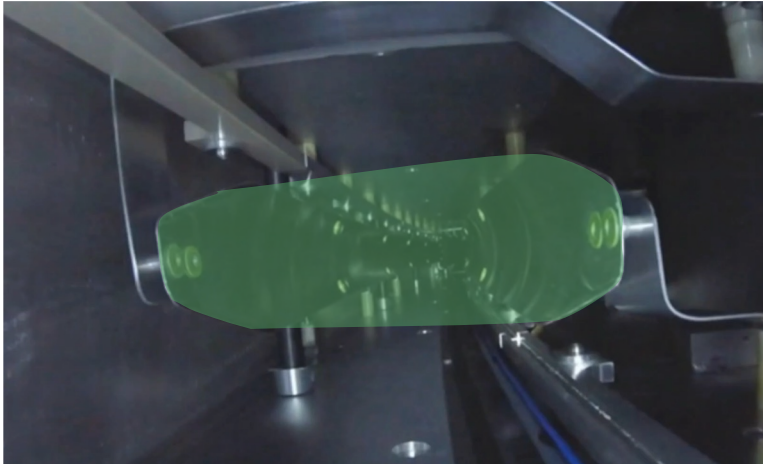
steer muon onto orbit  
in the first passing







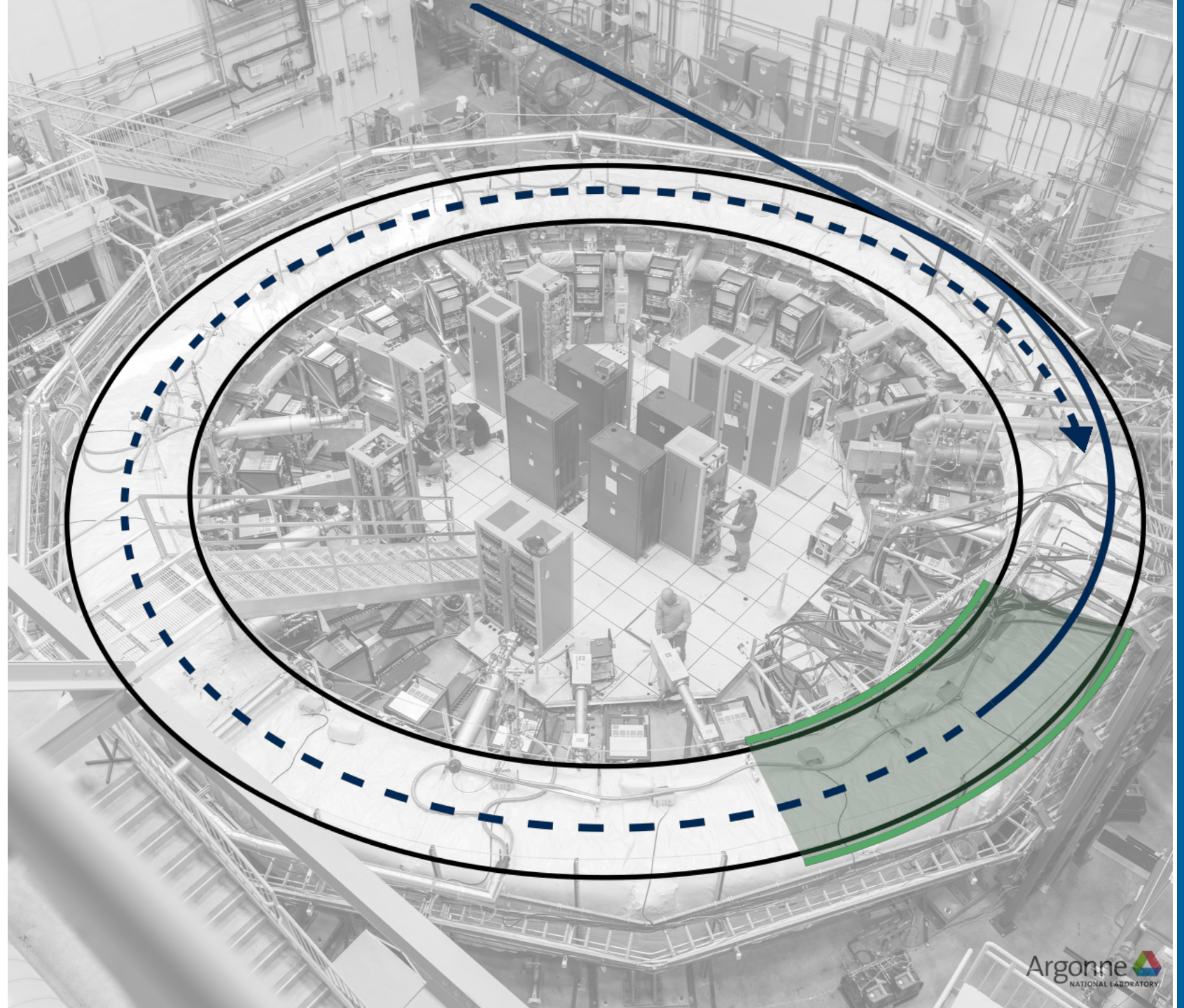
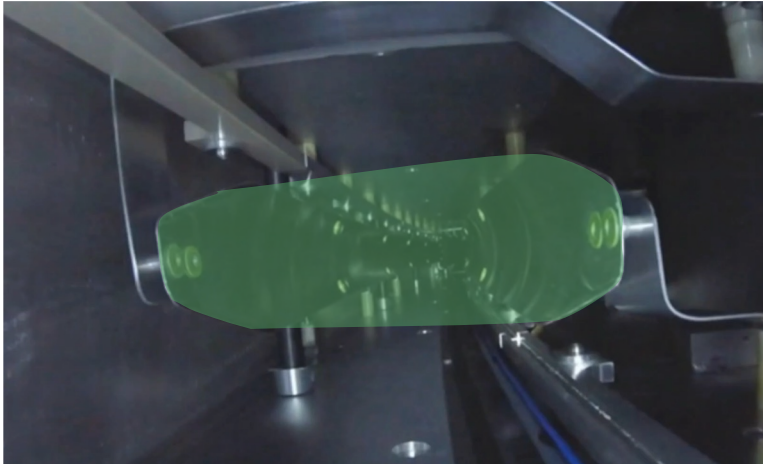
**steer muon onto orbit  
in the first passing**







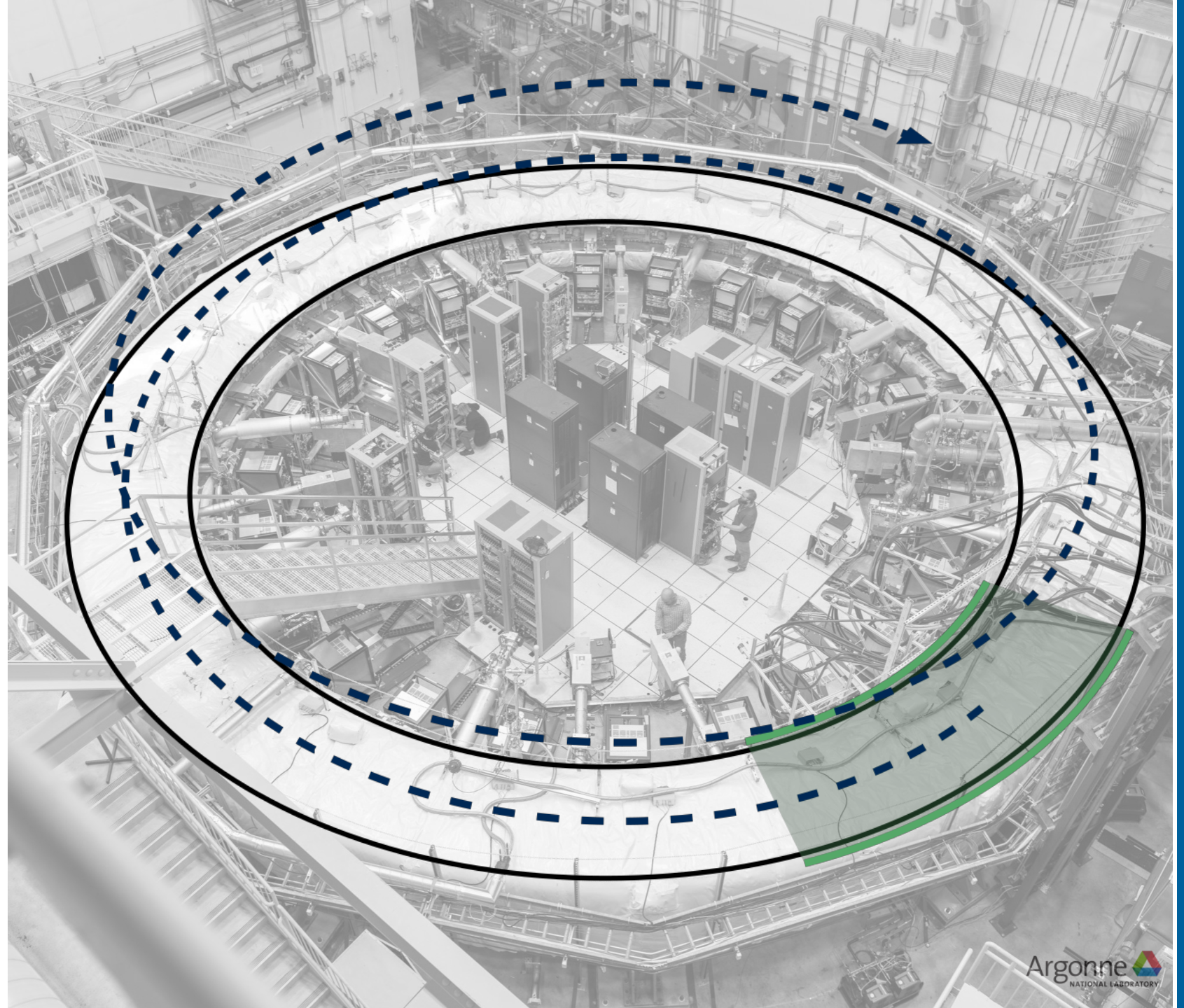
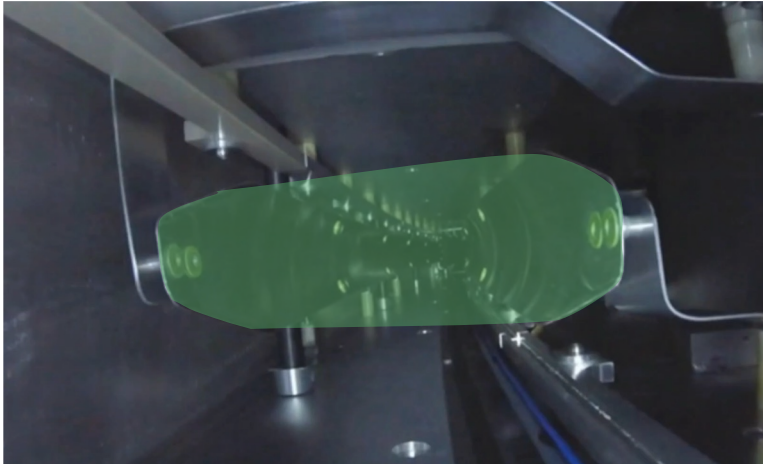
**steer muon onto orbit  
in the first passing**







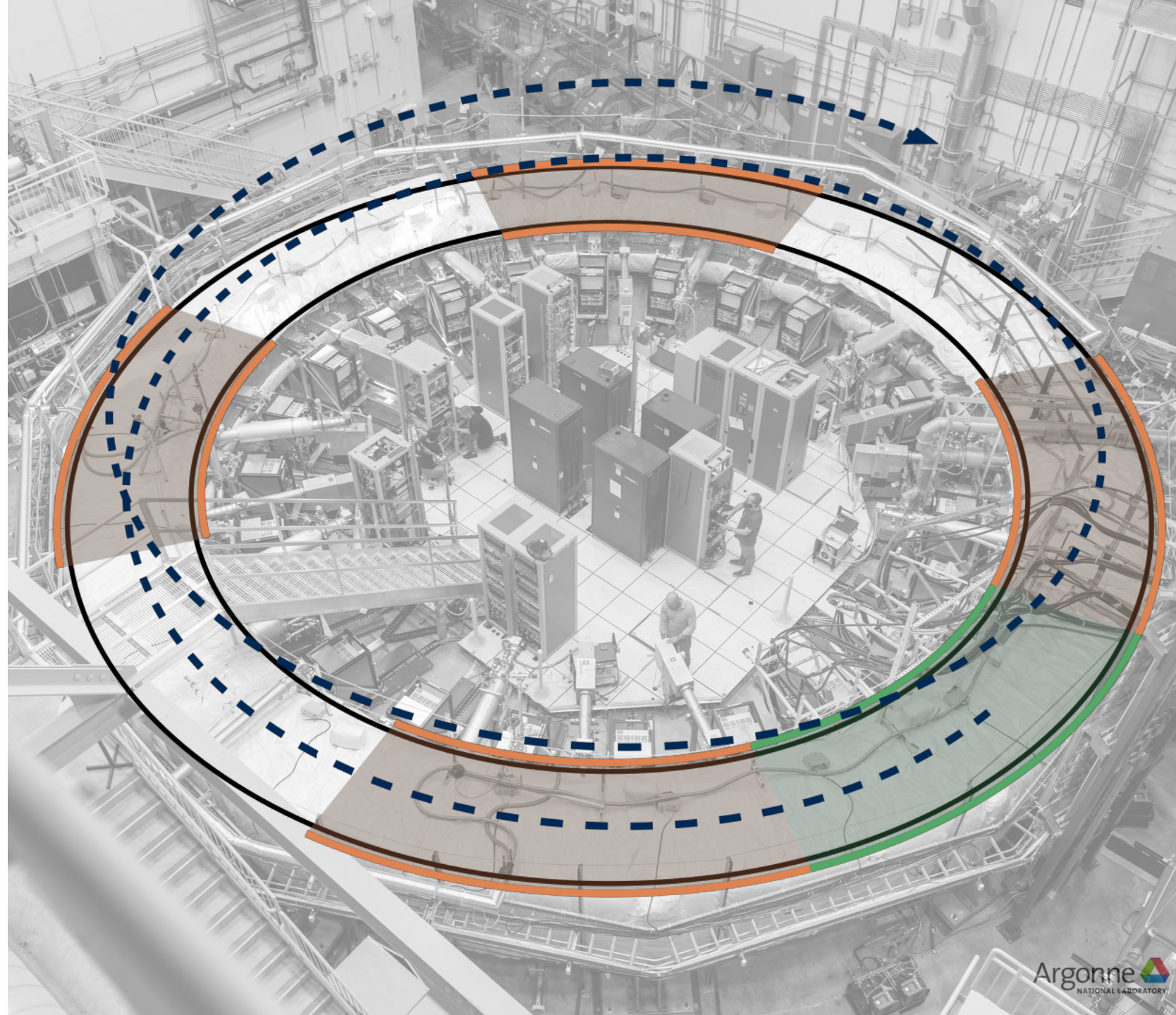
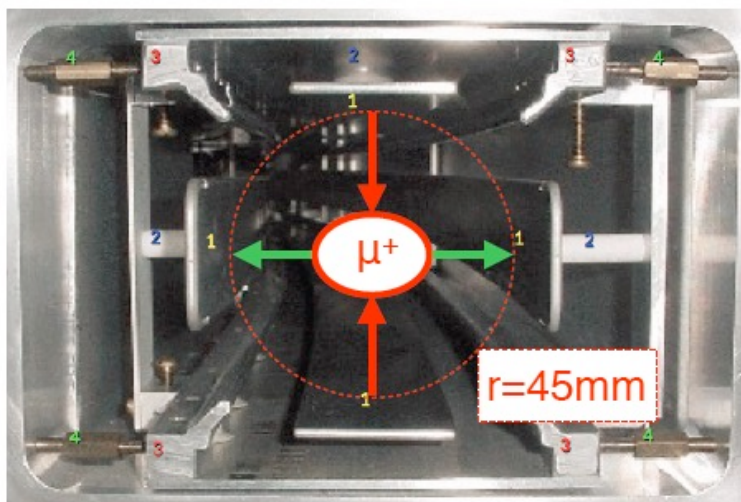
steer muon onto orbit  
in the first passing





# Electrostatic Quadrupoles

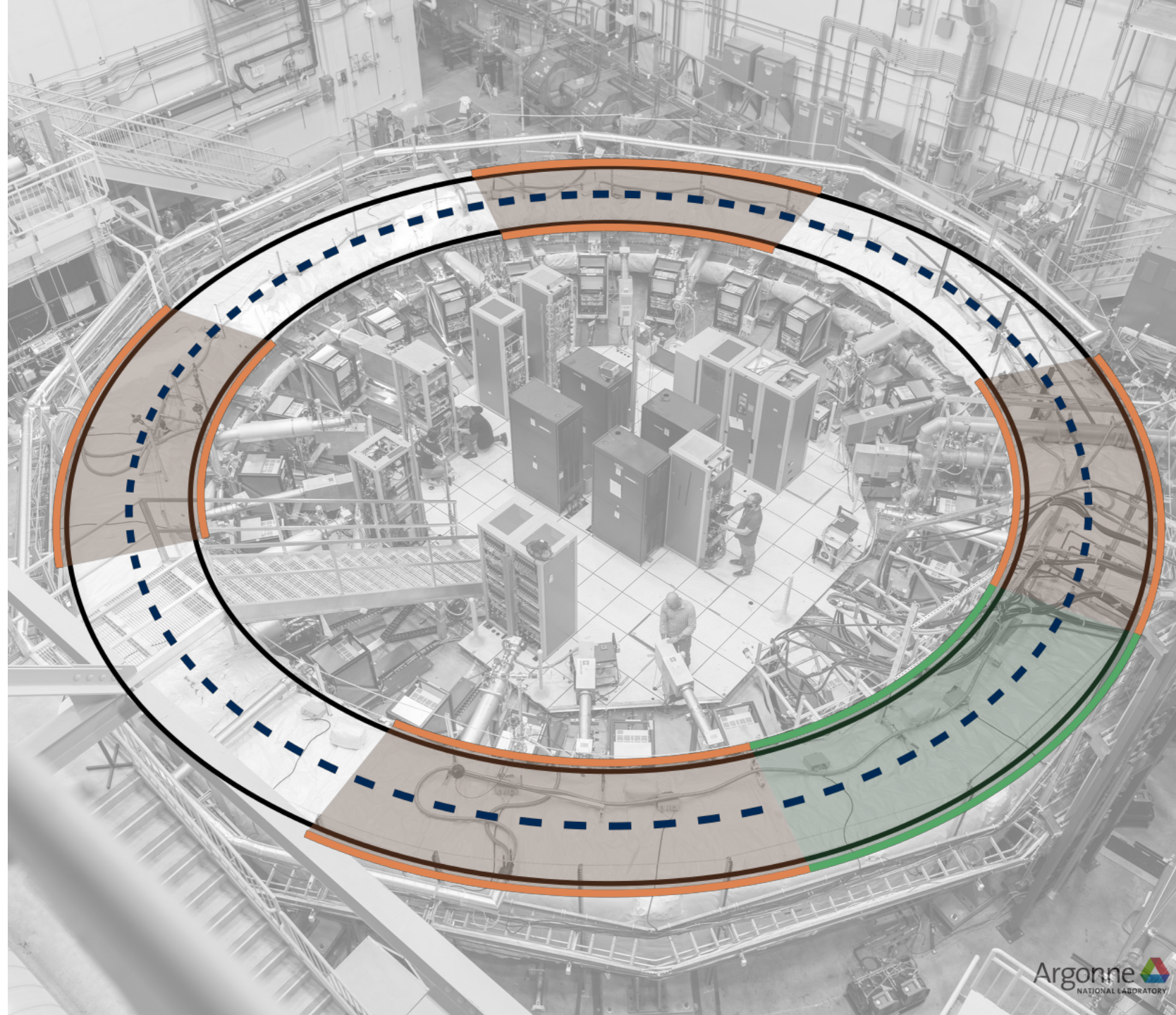
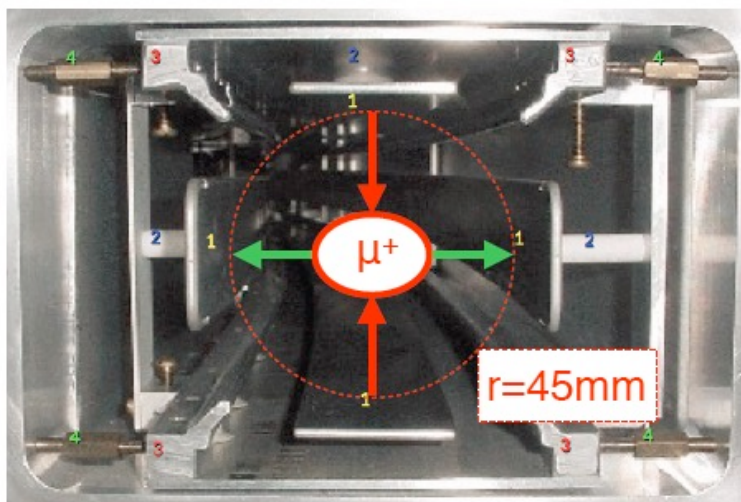
Electric fields for  
vertical focusing





# Electrostatic Quadrupoles

Electric fields for  
vertical focusing





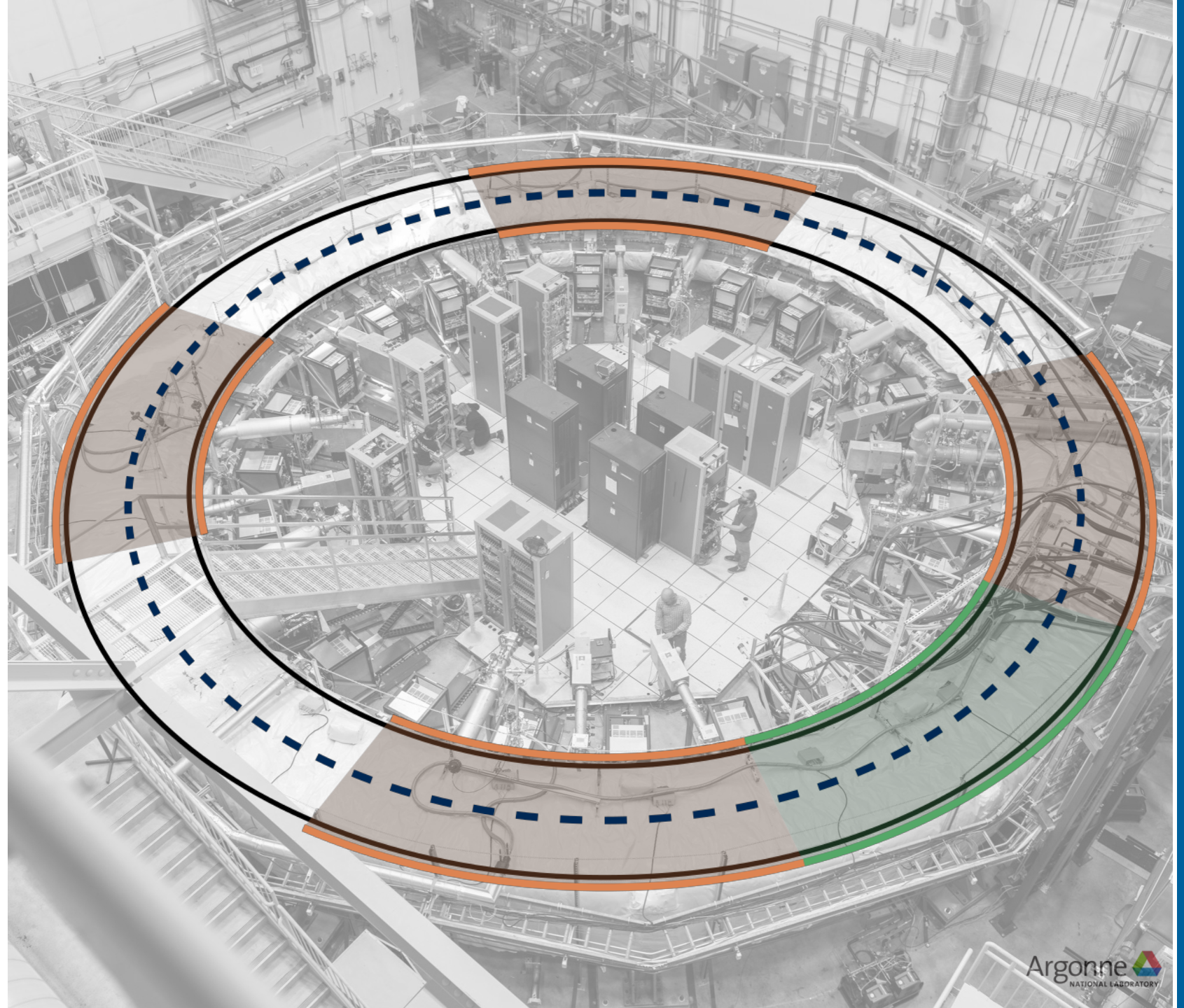
# Muon Storage

Cyclotron period: 149.2ns

few 1000 muons at a time

Boosted lifetime: 64  $\mu$ s

Storage up to 700  $\mu$ s





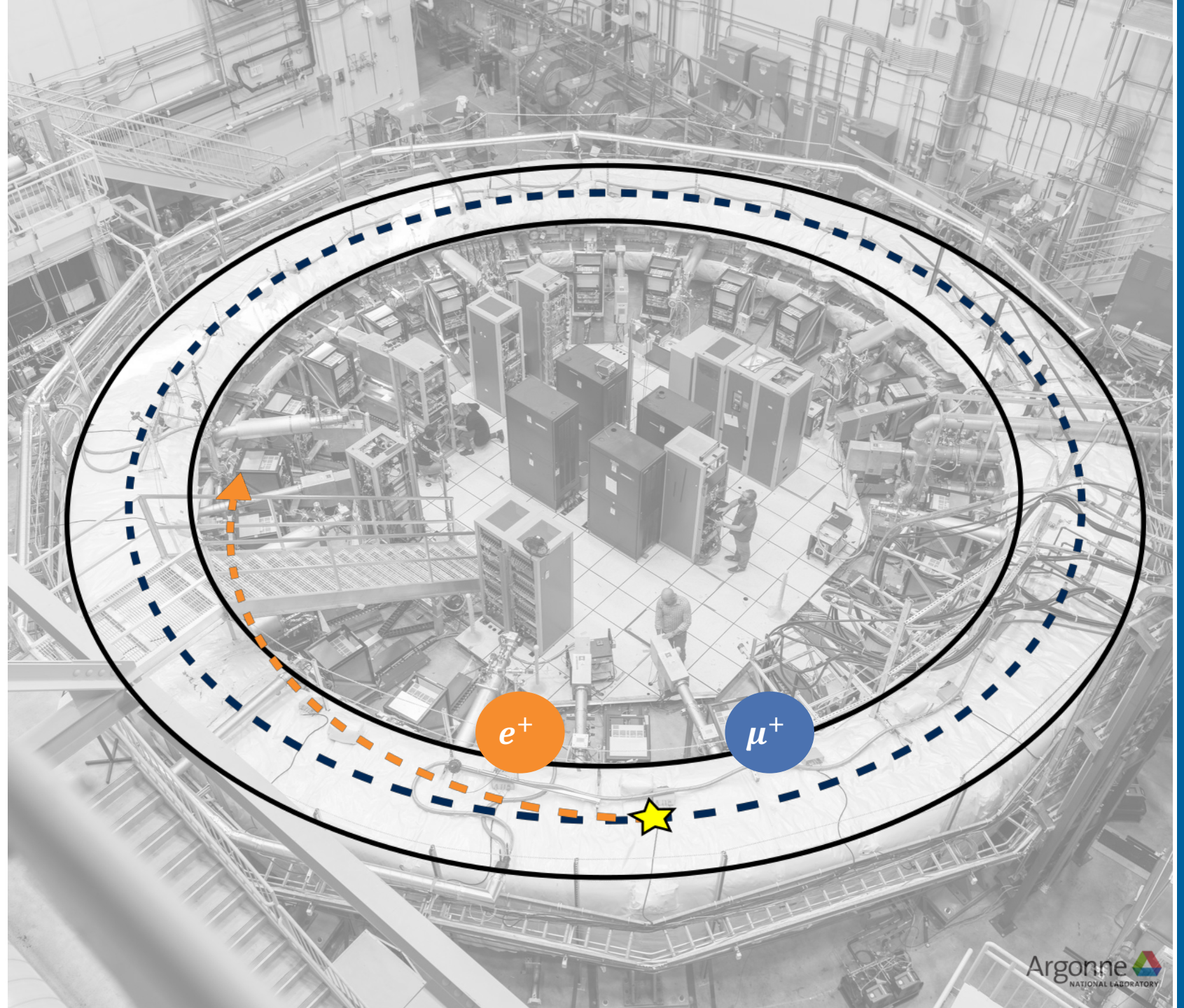
# Muon Decay

Muon decay to positrons and invisible neutrinos

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$$

Parity Violation:

“self-analyzing”  
 $\mu^+$  **spin** information  
encoded in  $e^+$  **energy**

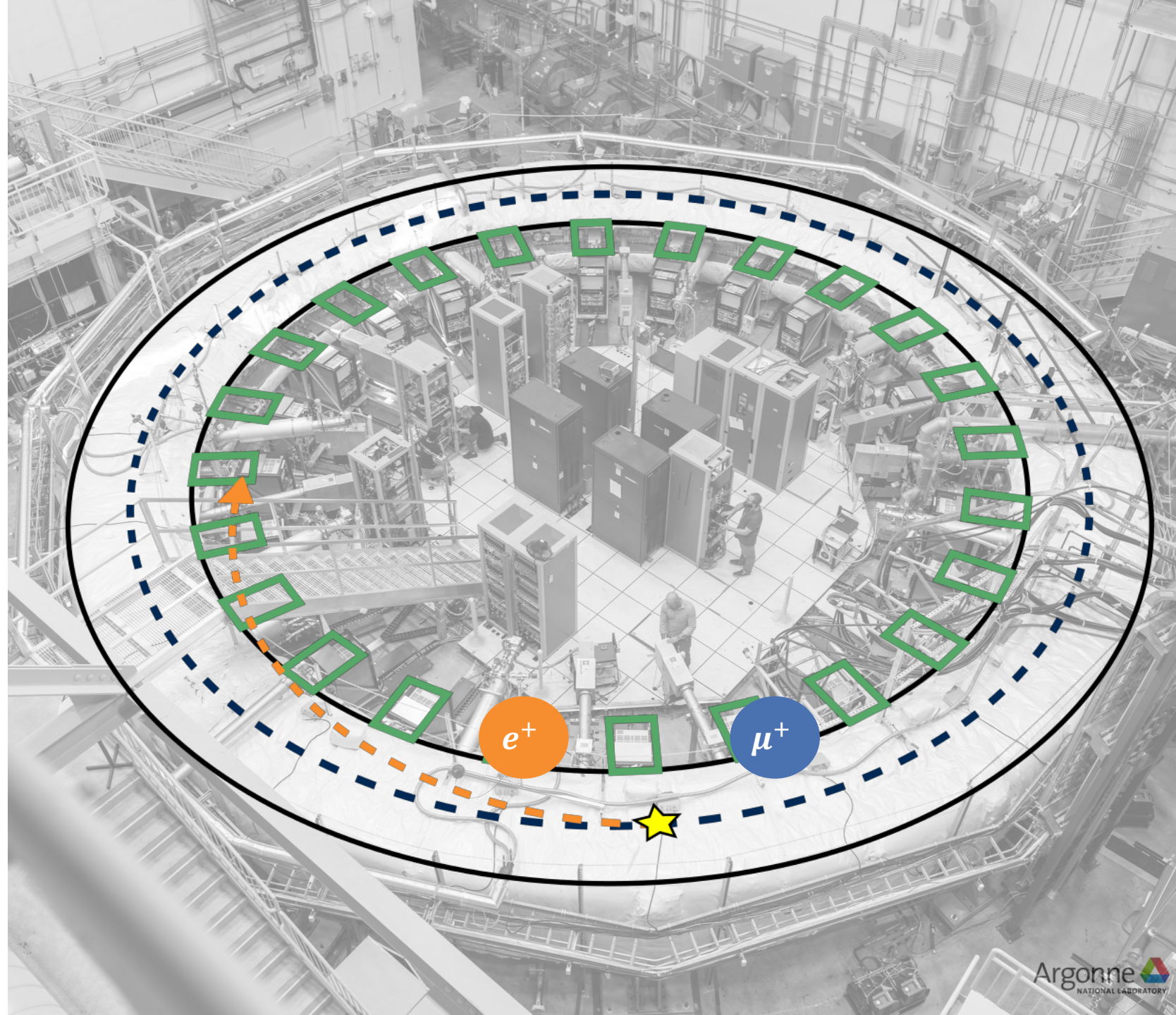
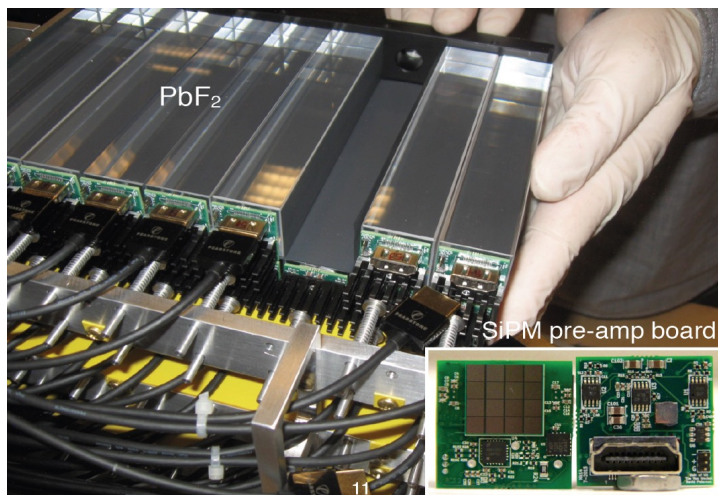




# Calorimeters

## 24 Calorimeters

with 54 (9x6) Cherenkov  $\text{PbF}_2$  crystals read out by SiPMs, arrival time ( $\sim 100\text{ps}$ ), energy of  $e^+$  ( $\sim 5\%$  at  $2\text{GeV}$ )





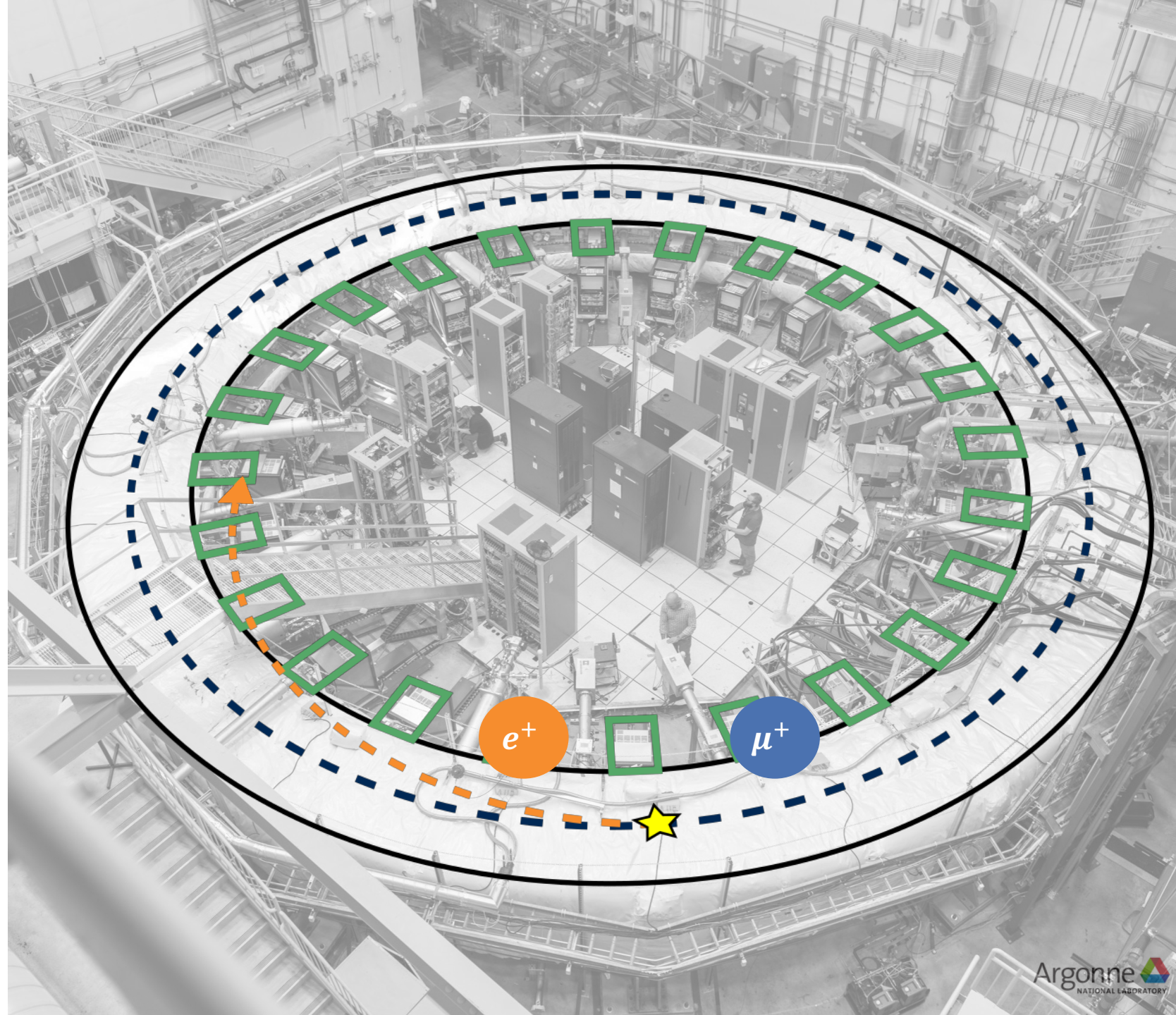
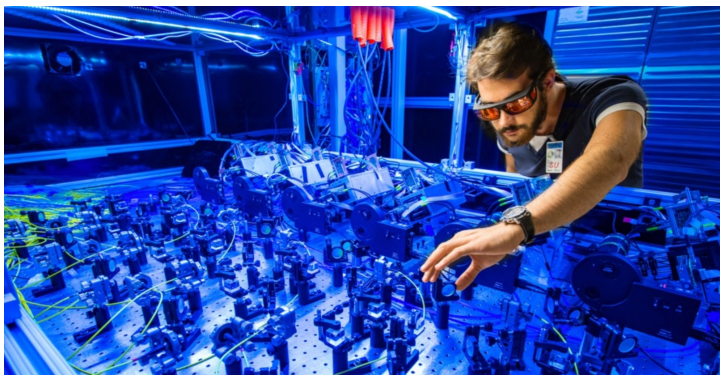
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with 54 (9x6) Cherenkov PbF<sub>2</sub> crystals read out by SiPMs, arrival time ( $\sim 100\text{ps}$ ), energy of  $e^+$  ( $\sim 5\%$  at 2GeV)

## Laser system for gain calibration

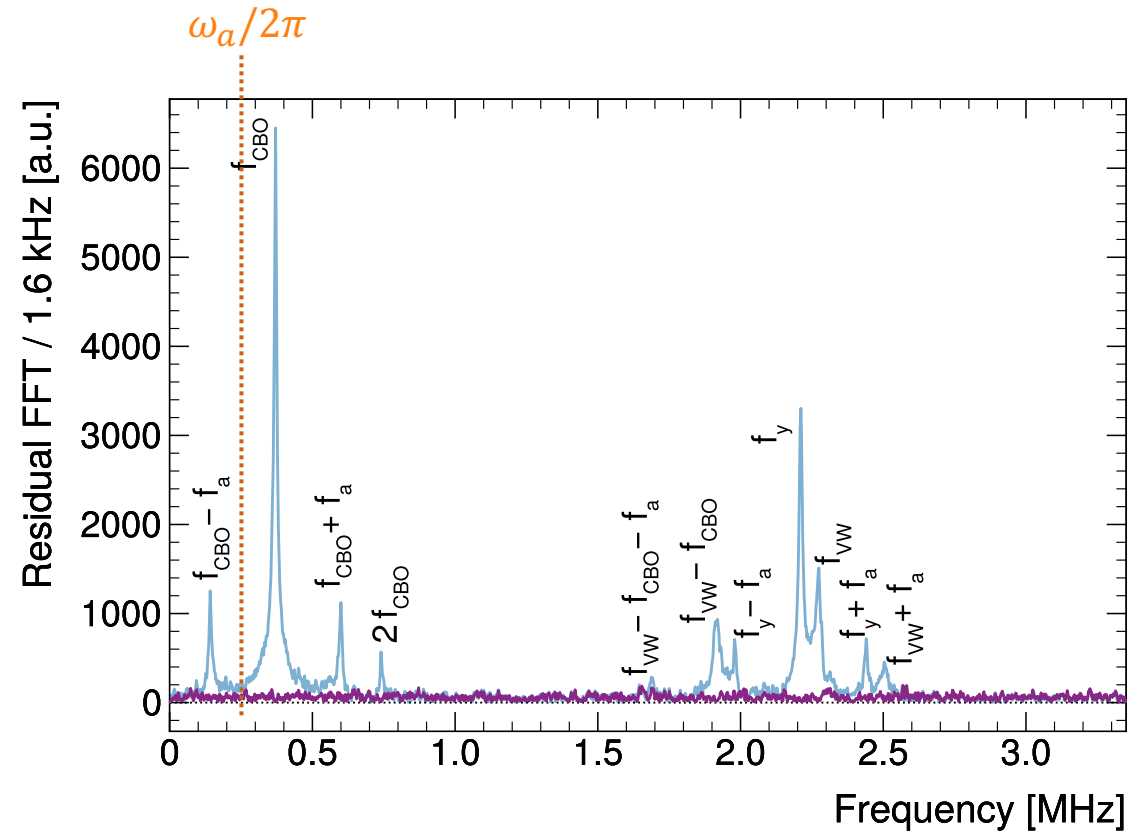
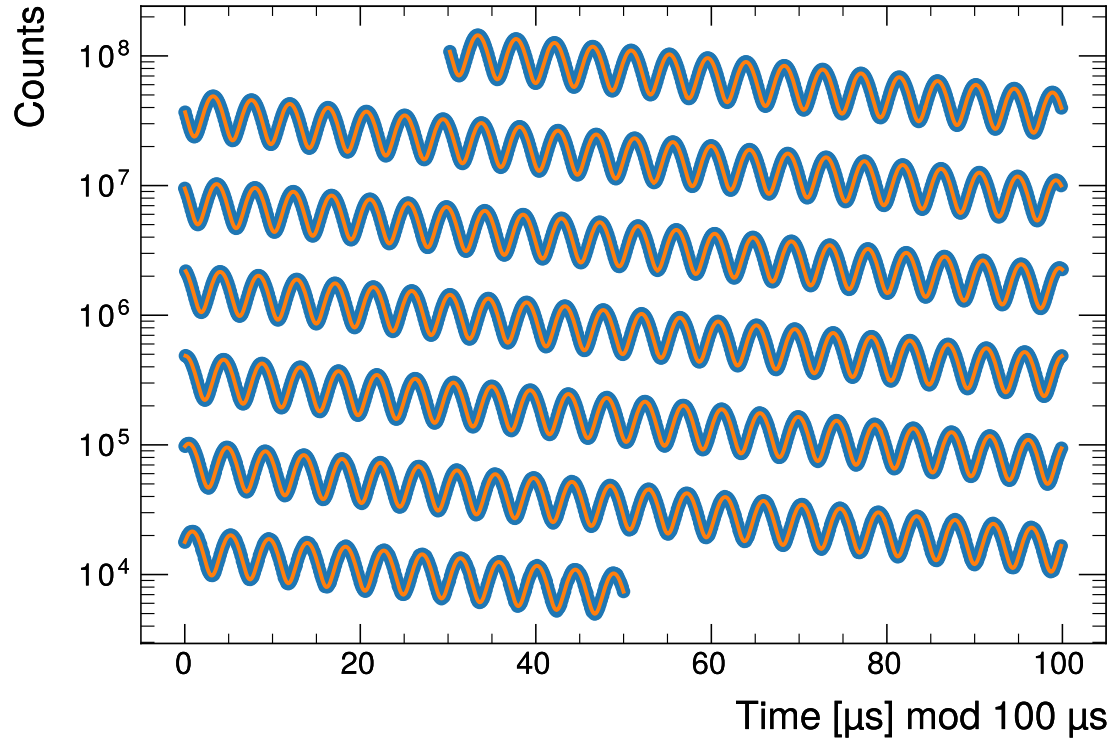
stability  $10^{-4}$  over a muon fill



# Measuring the Spin Precession

Simplest fit model captures **exponential decay** & **g-2 oscillation**

$$N(t) = N_0 e^{-t/\tau} [1 + A \cos(\omega_a t - \phi_0)]$$







~350ppb ~170ppb

~30ppb

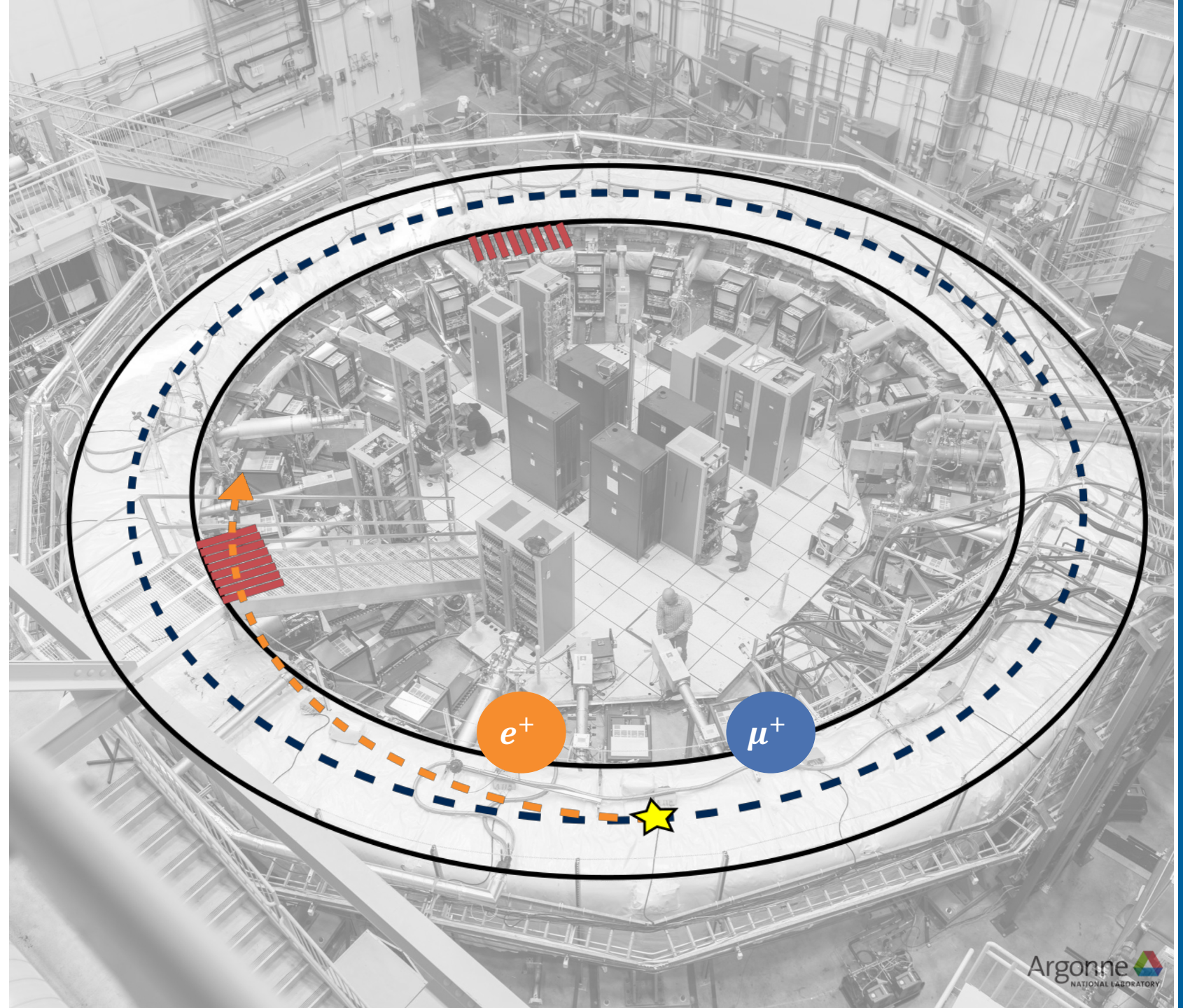
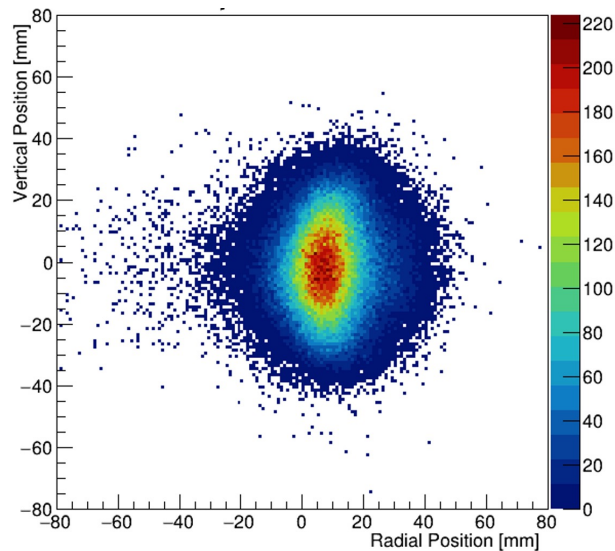
$$\omega_a = \omega_a^m \left( 1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml} \right)$$

Electric-field & Up/Down motion  
Spin precesses slower than  
in basic equation

Phase changes over each fill:  
Phase-Acceptance, Differential  
Decay, Muon Losses

2 straw-tracker stations  
each 8 modules, 4 layers of 32  
straws, 50:50 Ar:Ethane

# Reconstruct Muon Distribution

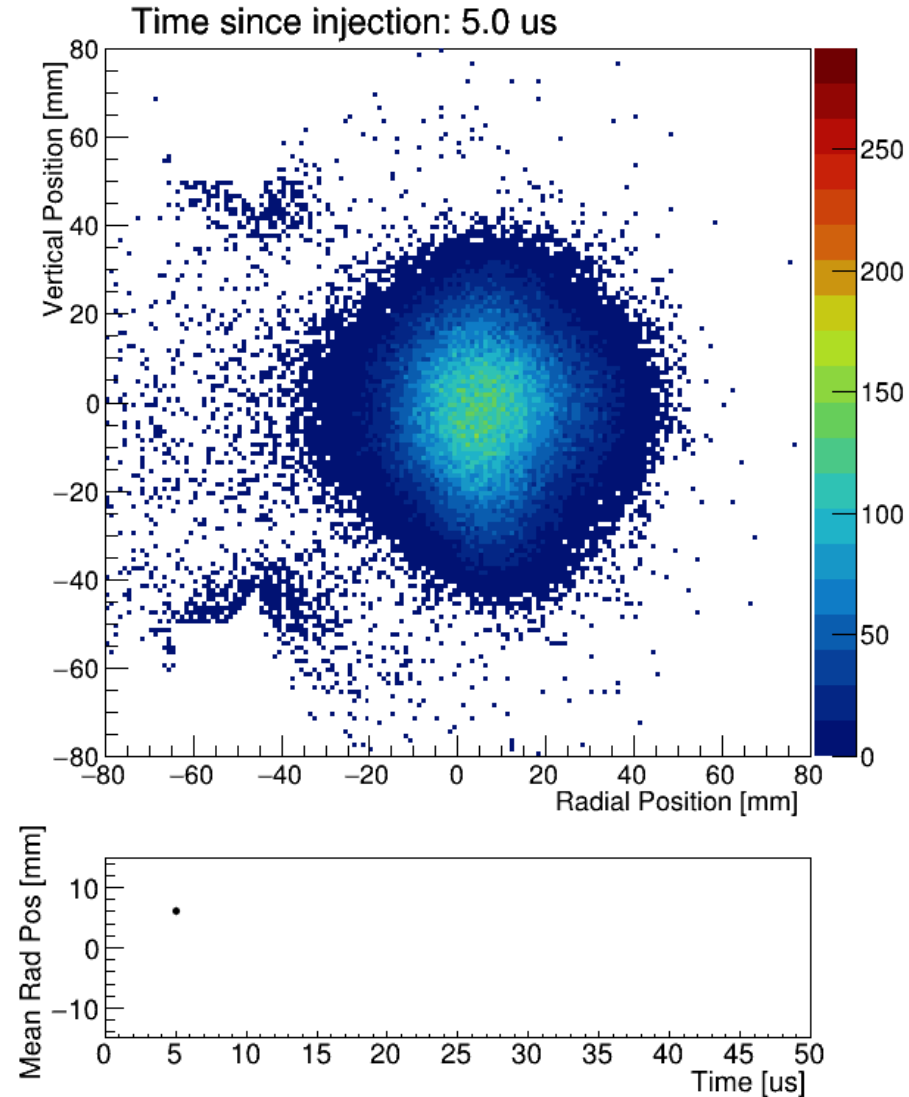






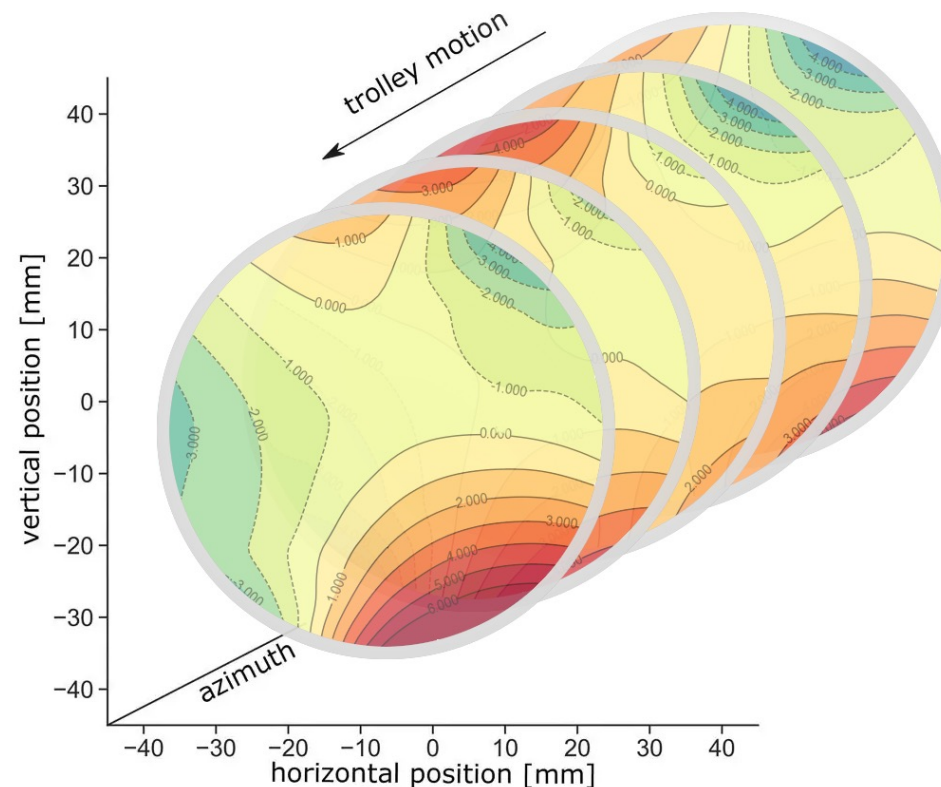
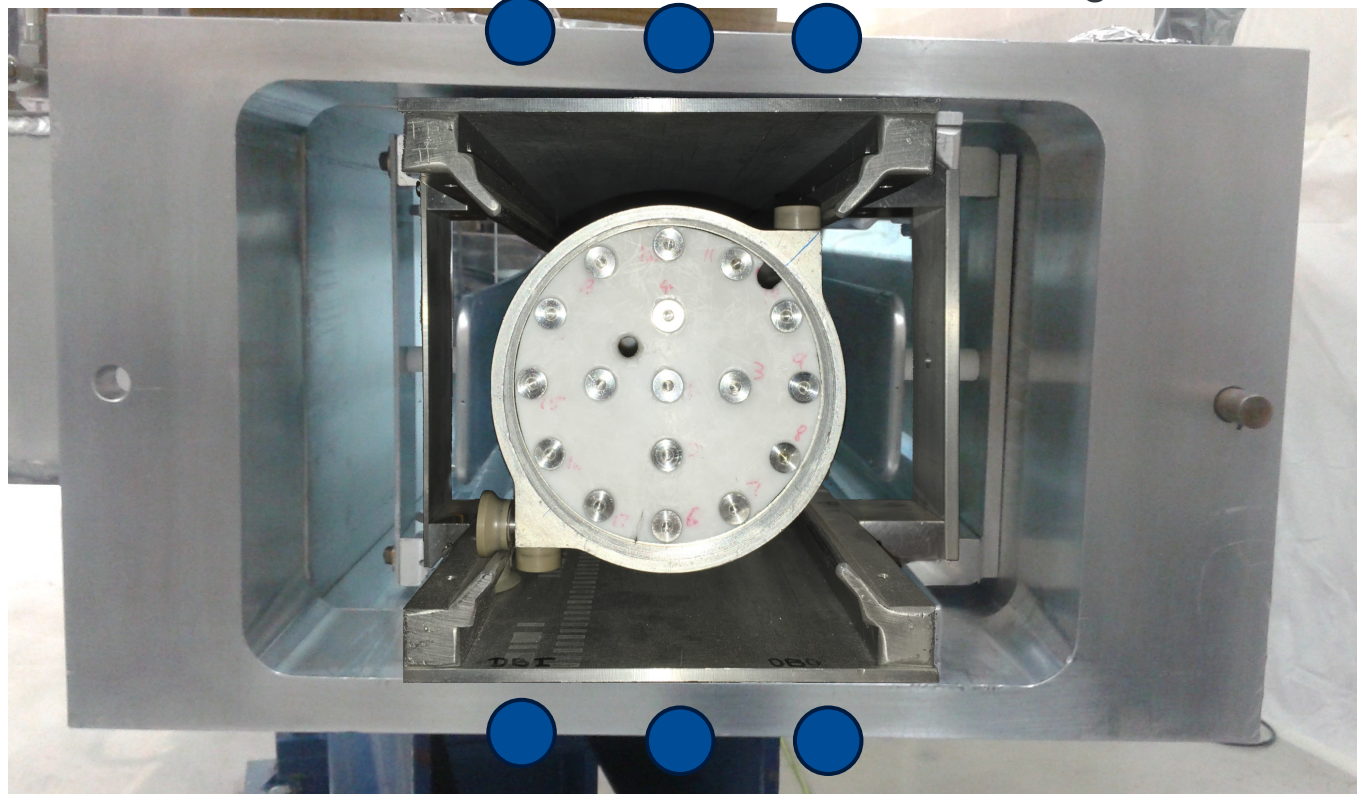
# Muon Beam Motion

Example: Coherent Betatron Oscillation (CBO)



# Magnetic Field Mapping & Tracking

Field Monitor: Fix installed NMR probes  
at 72 azimuthal locations around the ring



Trolley: Field Mapper  
The field between field maps (trolley runs) is tracked by the fixed NMR probes.



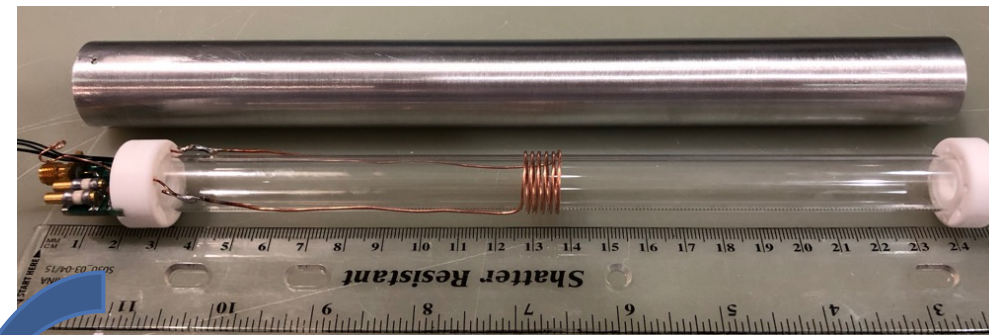
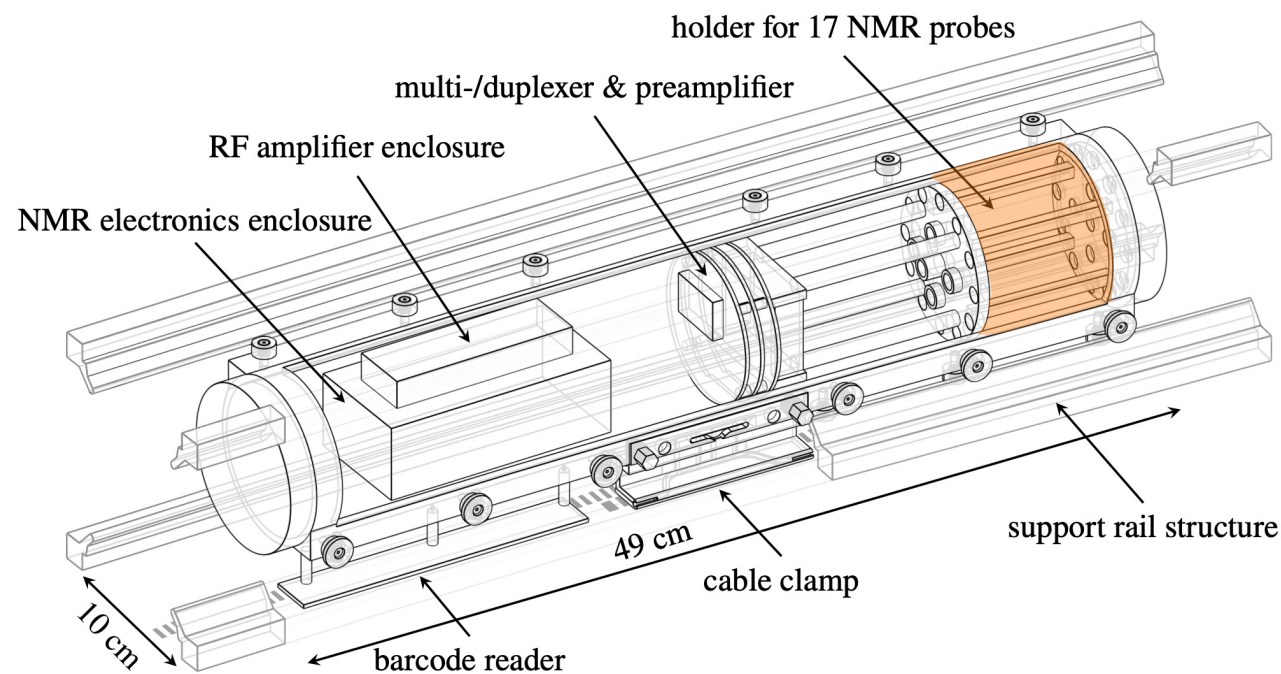


# Magnetic Field Calibration

with respect to **shielded protons in a spherical sample**:  $\omega_p'$

NMR probes in the  
"trolley's magnetic environment"

in-situ



water-based cylindrical **Calibration Probe**

- Material effect
- sample shape

$\omega_p'$ : shielded protons in  
a spherical sample

# Argonne's 4T Test Solenoid

0 to 4T very homogenous magnetic field

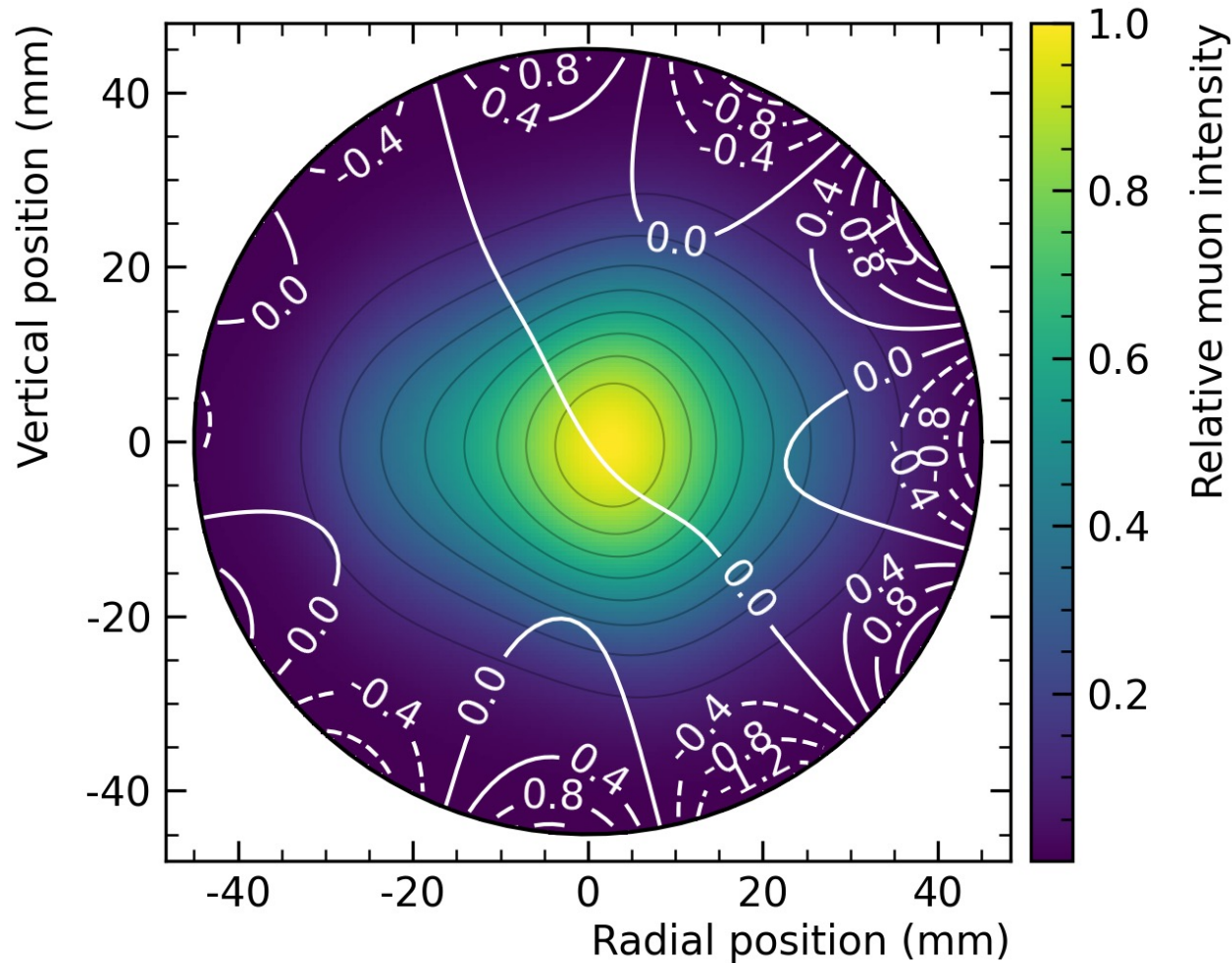
Stony Brook led  
detector test





# ⚙ Magnetic Field Muon Weighting

$$\tilde{\omega}'_p = \langle \omega'_p \times \mathbf{M} \rangle (1 + B_k + B_q)$$



Magnetic field seen by the muons,  
weight by the Muon Distribution  $M$

- Muon distribution from the **trackers**, propagated around the ring using our **simulation frameworks**



~30ppb    ~20ppb

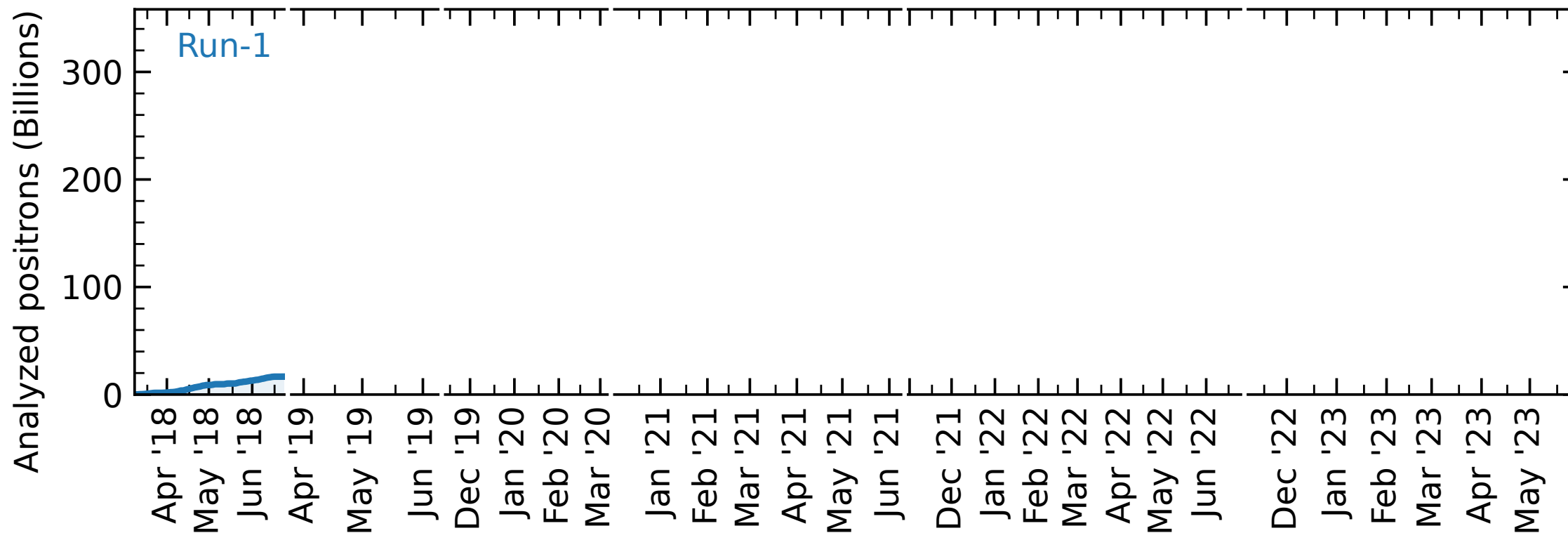
$$\tilde{\omega}'_p = \langle \omega'_p \times \mathbf{M} \rangle (1 + B_k + B_q)$$

**Transient magnetic fields**  
synchronous to the muon injection  
not covered by the  
asynchronous NMR measurements





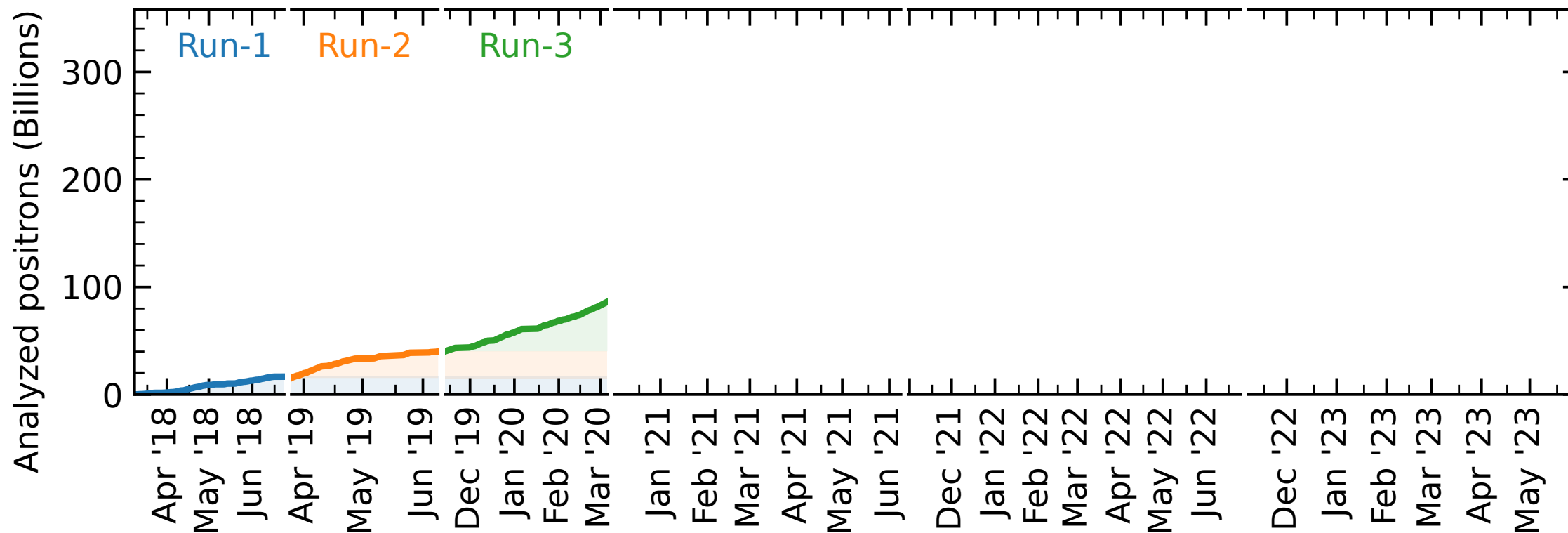
# Data Collection – 6 Runs over 6+ Years



April 2021: **Run-1** results, roughly matching the BNL dataset



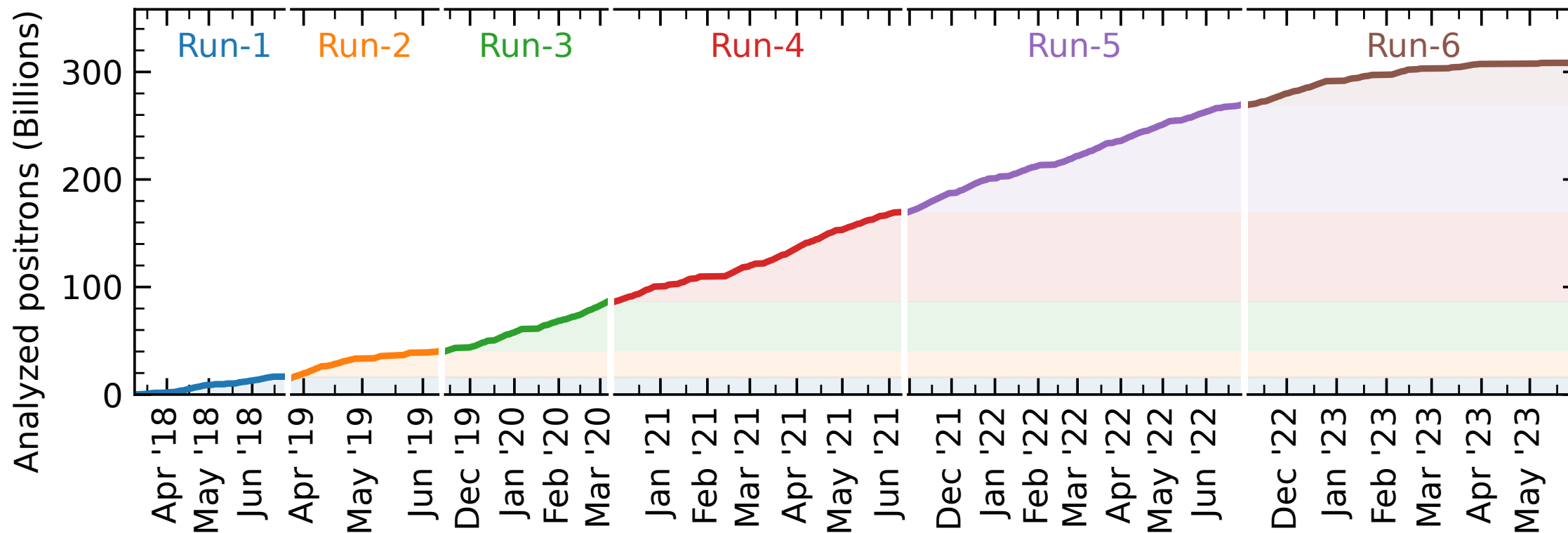
# Data Collection – 6 Runs over 6+ Years



April 2021: **Run-1** results, roughly matching the BNL dataset

August 2023: **Run-2/3** results, 4.6 times more data than Run-1

# Data Collection – 6 Runs over 6+ Years



April 2021: **Run-1** results, roughly matching the BNL dataset

August 2023: **Run-2/3** results, 4.6 times more data than Run-1

June 2025: **Run-4/5/6** results, 2.6 times the Run-1/2/3 dataset



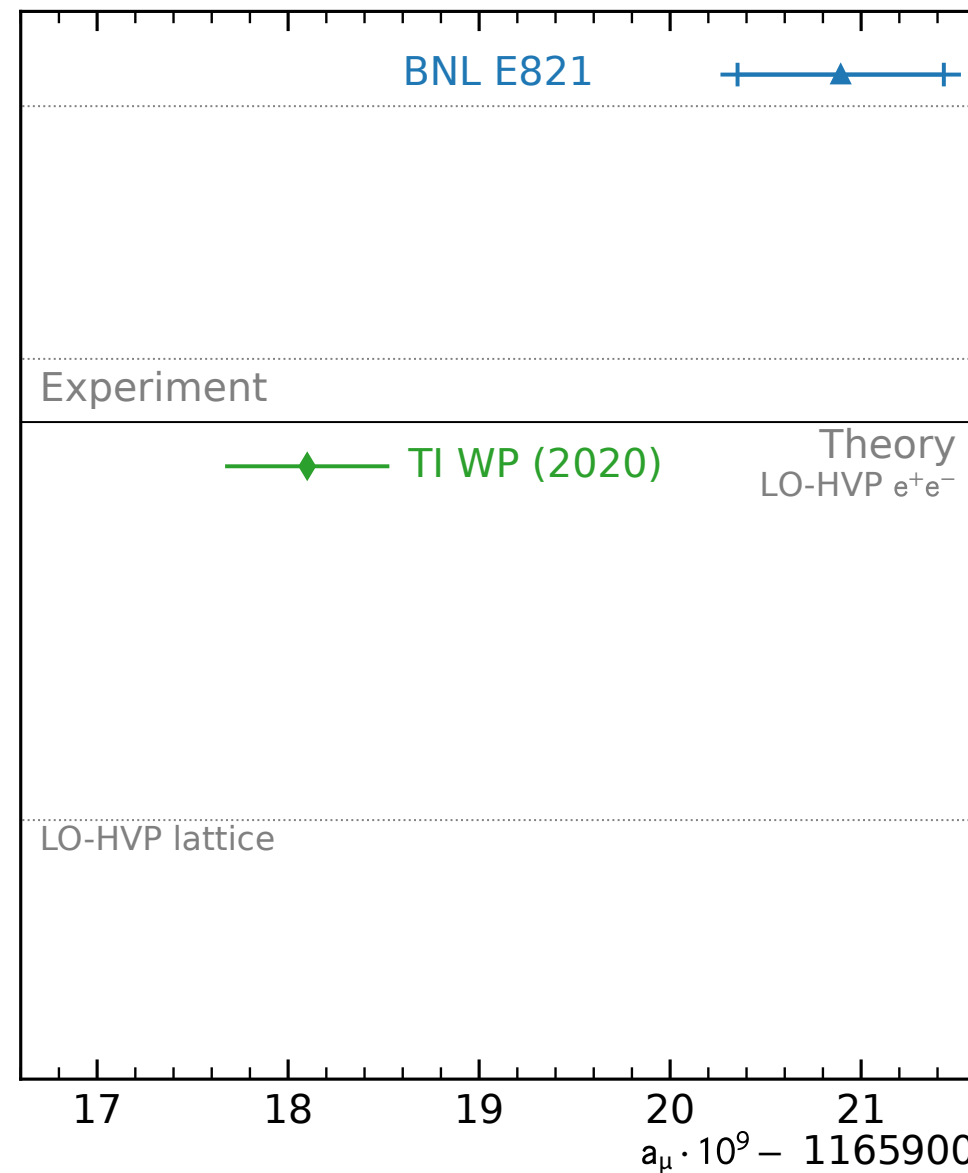
# Muon g-2 Theory Initiative (TI)

100+ theorist compile the theoretical  
input and provide recommendations

*[muon-gm2-theory.illinois.edu](https://muon-gm2-theory.illinois.edu)*

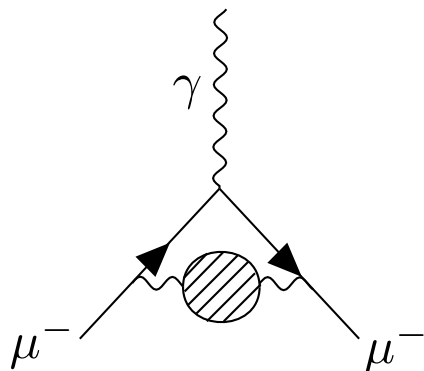
## TI White Paper 2020

Physics Reports 887 (2020) 1-166

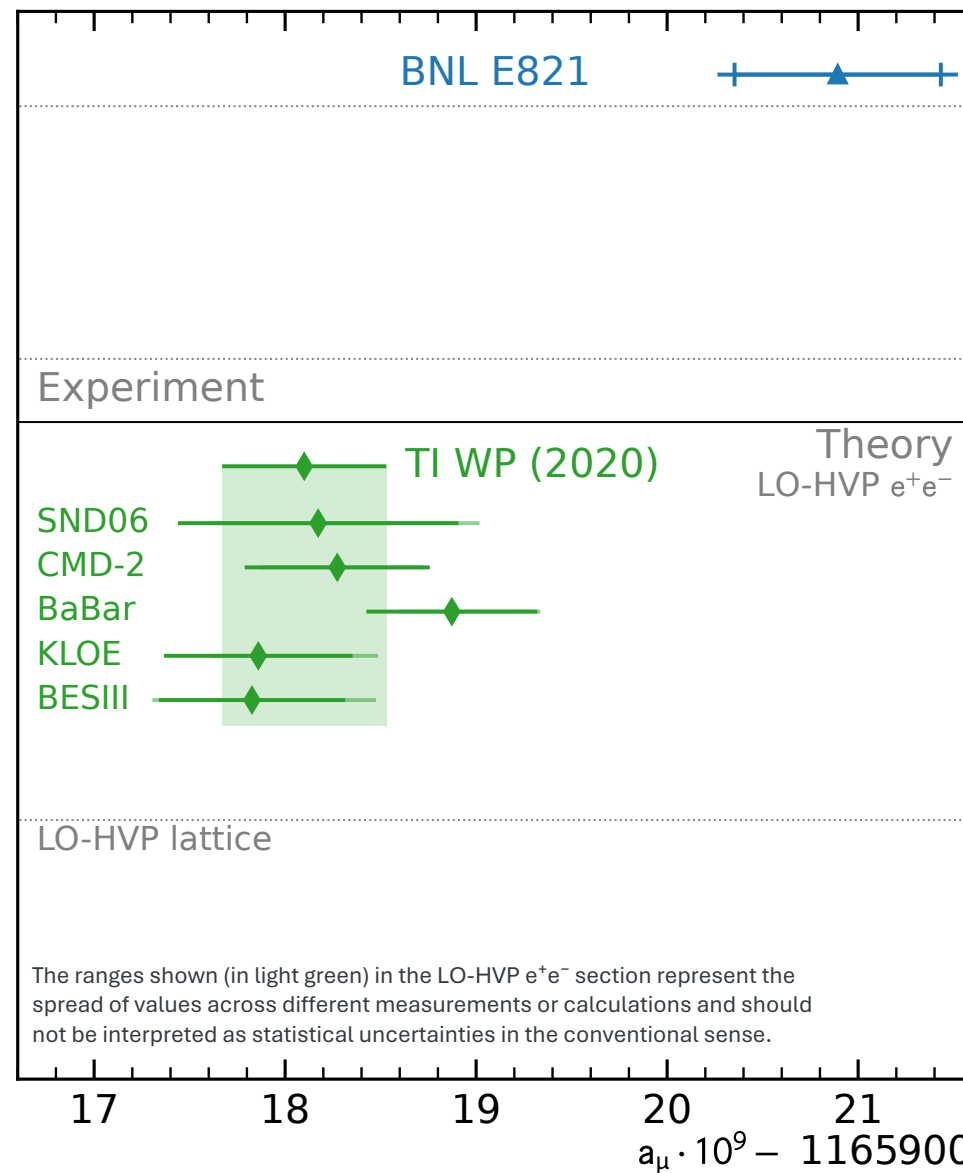


# TI White Paper 2020

## Hadronic Vacuum Polarization (HVP)



**data-driven** dispersive approach from  $\sigma(e^+e^- \rightarrow \text{hadrons})$  data from different experiments over 20+ years

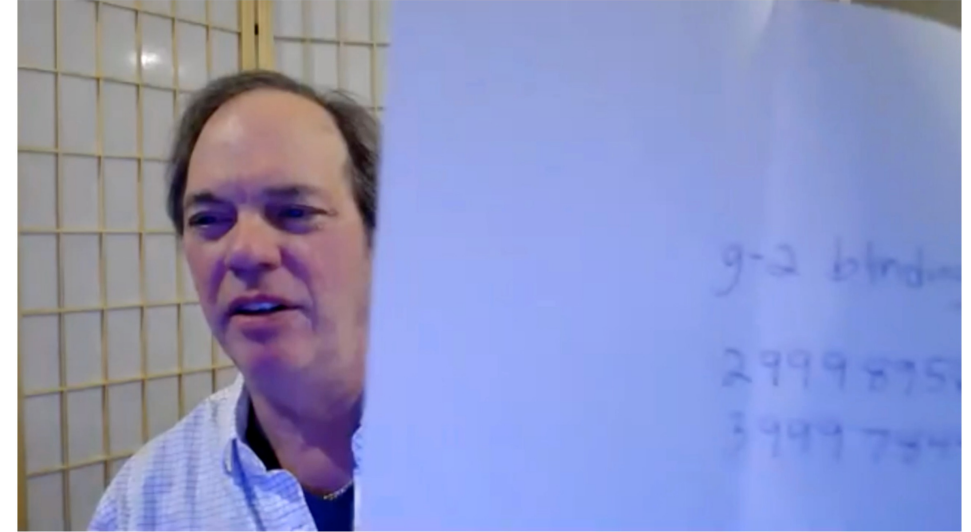




# Blinded Analysis

## Software & Hardware blinded

- Altered clock: 40 MHz -  $\delta$   
aka. value of  $\omega_a$  is not knowable
- $\delta$  secret to the collaboration  
until the vote for hardware  
unblinding



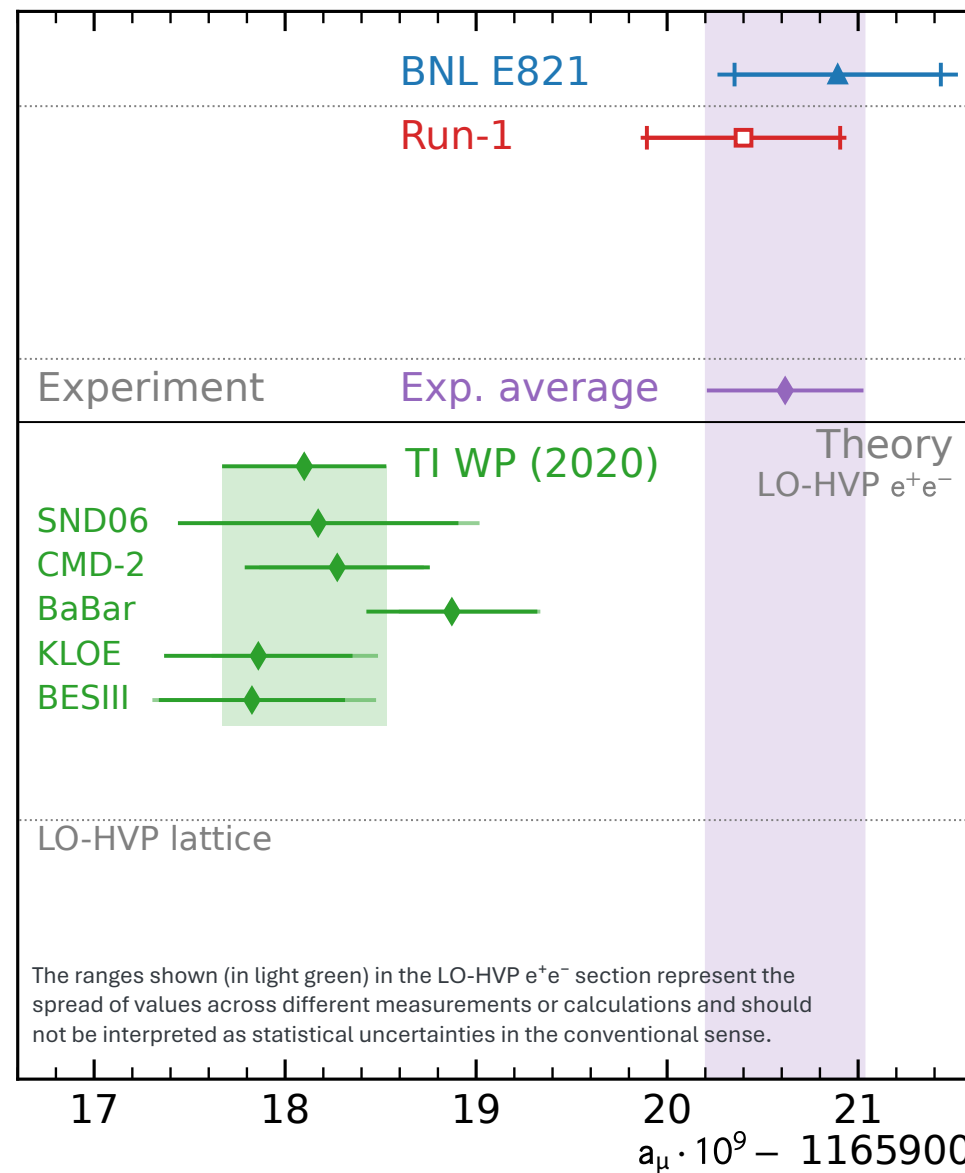
February 25<sup>th</sup> 2021, on Zoom



May 20<sup>th</sup> 2025, at Fermilab

# April 2021: Run-1

- 5% of our full dataset
- In good agreement with previous results





# April 2021 – Muons made News

## A Particle's Tiny Wobble Could Upend the Known Laws of Physics

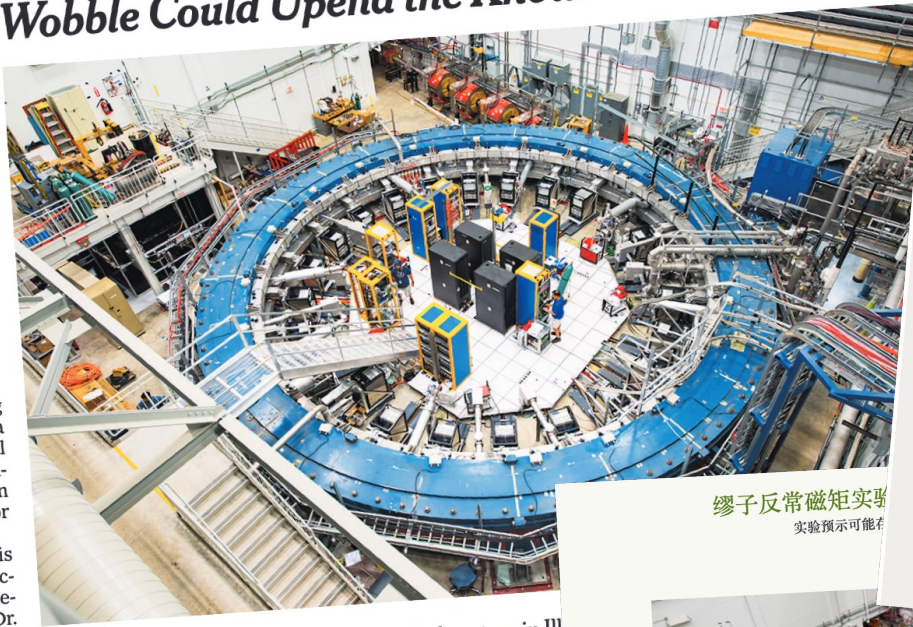
By DENNIS OVERBYE

Evidence is mounting that a tiny subatomic particle seems to be disobeying the known laws of physics, scientists announced on Wednesday, a finding that would open a vast and tantalizing hole in our understanding of the universe.

The result, physicists say, suggests that there are forms of matter and energy vital to the nature and evolution of the cosmos that are not yet known to science.

"This is our Mars rover landing moment," said Chris Polly, a physicist at the Fermi National Accelerator Laboratory, or Fermilab, in Batavia, Ill., who has been working toward this finding for most of his career.

The particle under scrutiny is the muon, which is akin to an electron but far heavier, and is an integral element of the cosmos. Dr. Polly and his colleagues — an international team of 200 physicists from seven countries — found that muons did not behave as pre-



A ring at the Fermi National Accelerator Laboratory in Ill.

缪子反常磁矩实验  
实验预示可能在



缪子反常磁矩实验

近日，在美国费米国家实验室进行的缪子反常磁矩实验结果与标准模型理论预言不相符，该结果与早期美国布鲁克海文实验室的未知粒子或者作用力。

“这意味着原本经历了多次考验，堪称完美的标准模型理论等待人类去发现。”缪子反常磁矩实验组在《中国科学报》。



Neue Erkenntnisse in der Teilchenphysik  
**Kundschafter ins Unbekannte**

Seit 50 Jahren ersehnen Forscher Einblicke in die Welt jenseits der bekannten Naturgesetze. Mit den Erkenntnissen aus dem Myon-g-2-Experiment könnte sich das Tor zu einer neuen Physik öffnen. Von Johann Grollie

SHARE



Muons twirl as they circulate in this ring-shaped accelerator at Fermilab, like race cars perpetually spinning out. REIDAR HAHN/FERMI LAB

Particle mystery deepens, as physicists confirm that the muon is more magnetic than predicted

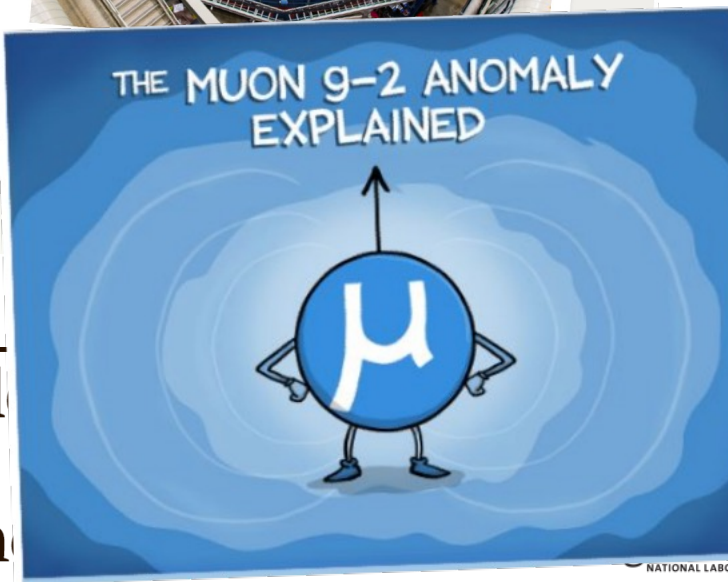
By Adrian Cho | Apr. 7, 2021, 11:00 AM



GHOST GUNS AND SUBATOMIC PARTICLES

Le Monde  
VENDREDI 9 AVRIL 2021

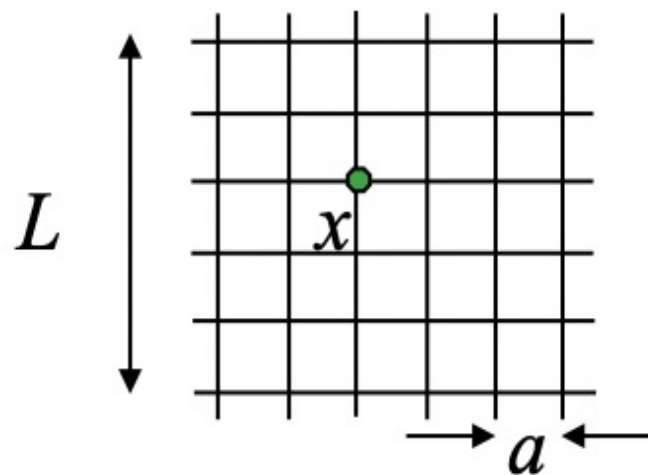
Une particule élémentaire polarise le modèle de la physique



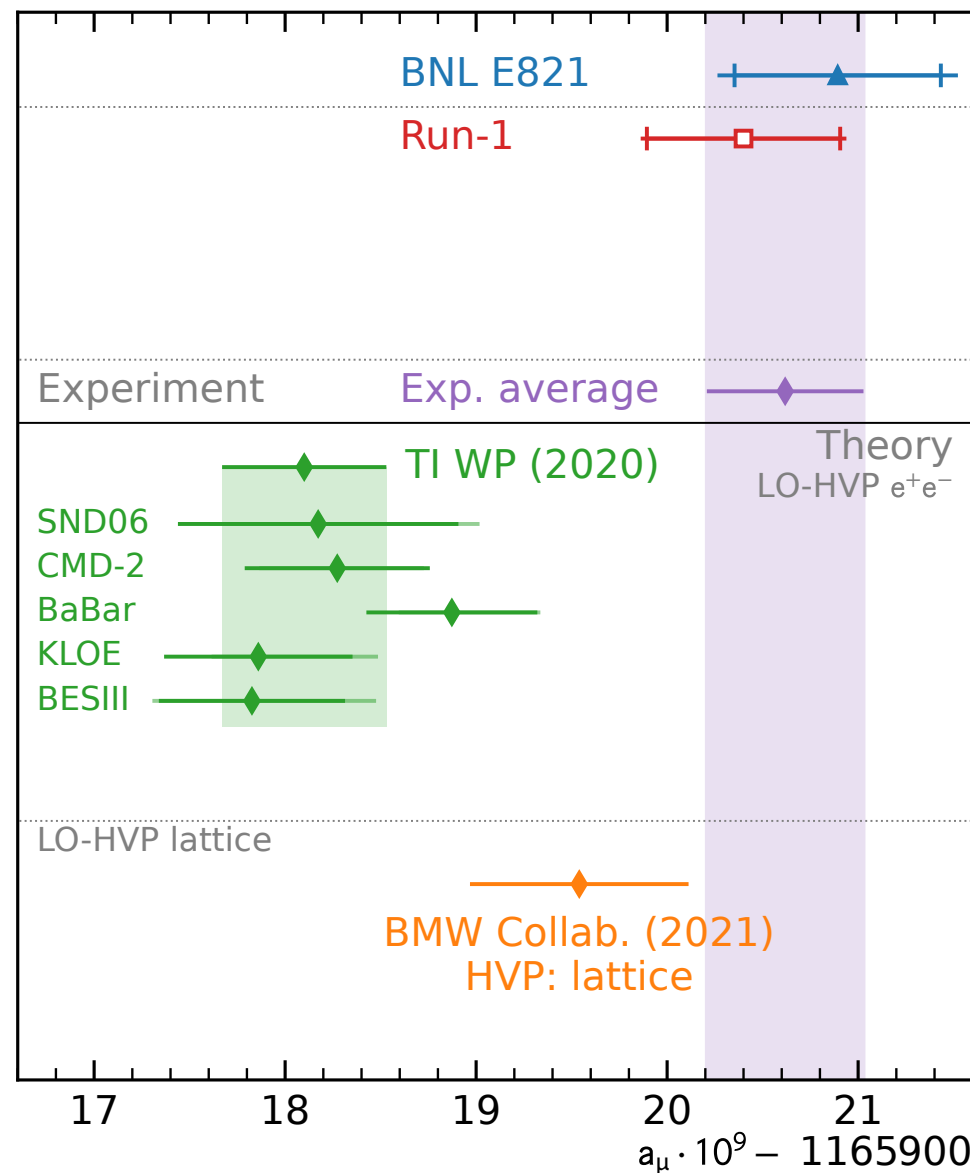


# HVP lattice calculation

First high-precision calculations of LO-HVP on lattice-QCD

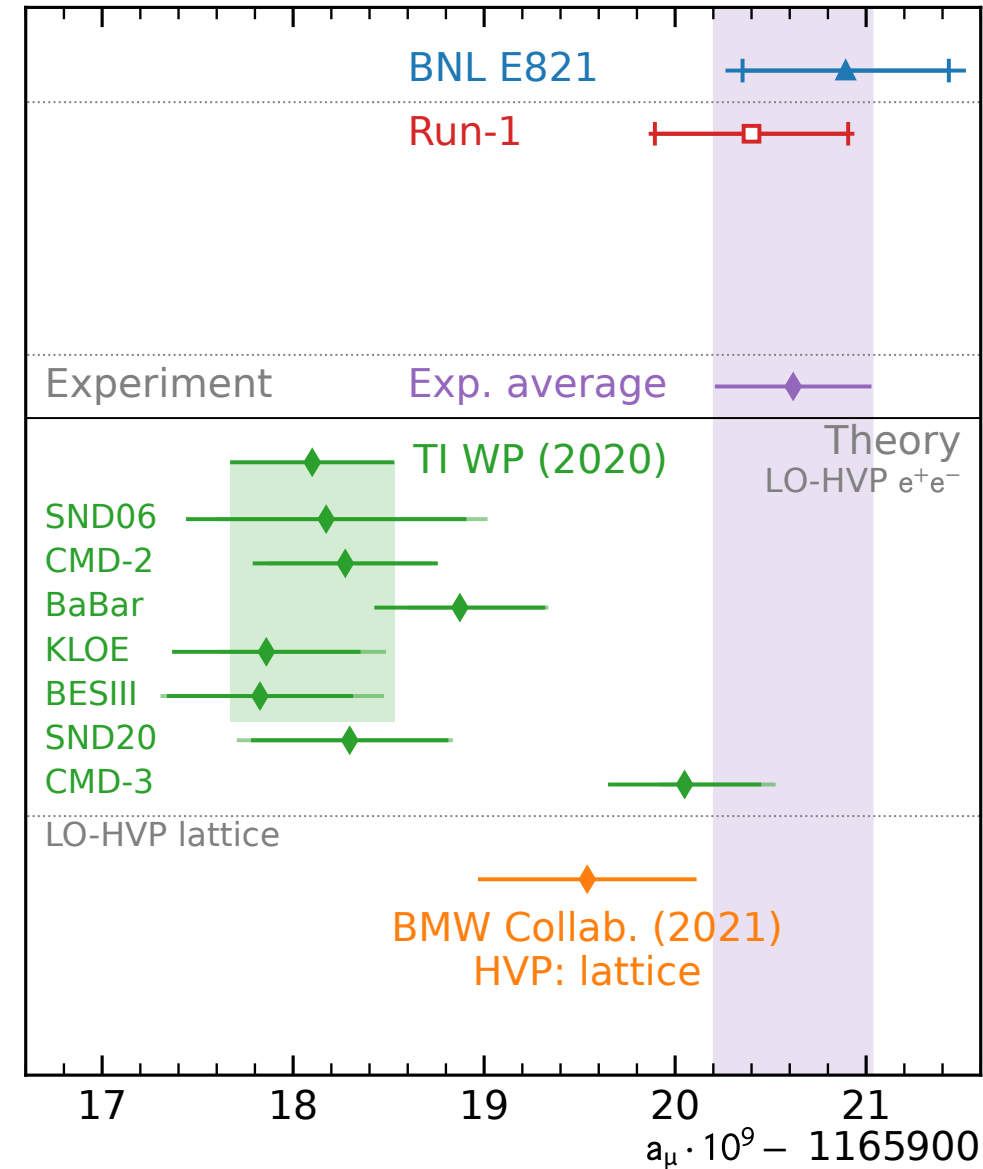


in tension with the data-driven  $e^+e^-$  approach



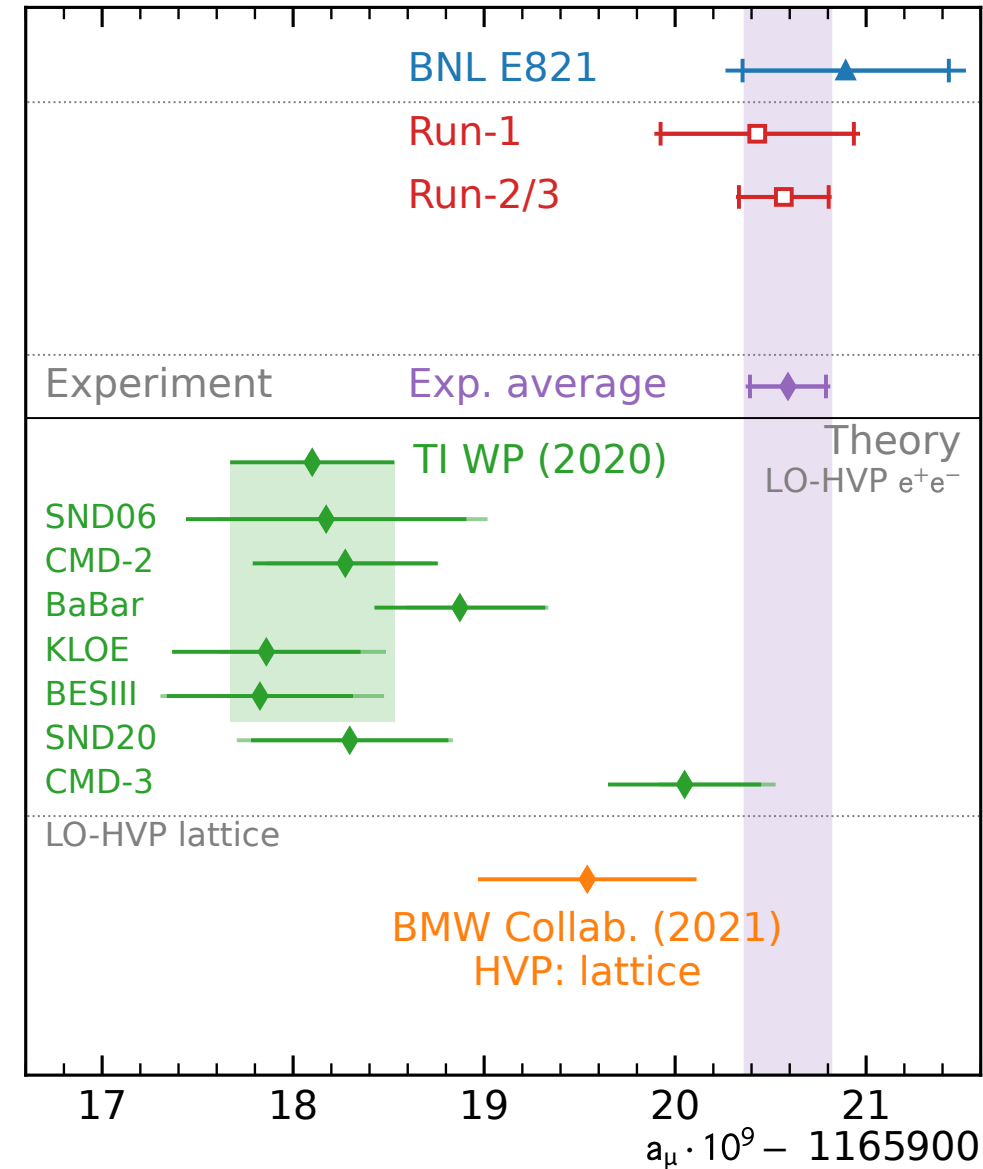
# New $e^+e^-$ Input Data

New  $\sigma(e^+e^- \rightarrow \text{hadrons})$  results from the **CMD-3 experiment** are in tension with WP (2020) input



# ⚙️ August 2023: Run-2/3

- 4.6 times more data
- More than a two-fold increase in precision



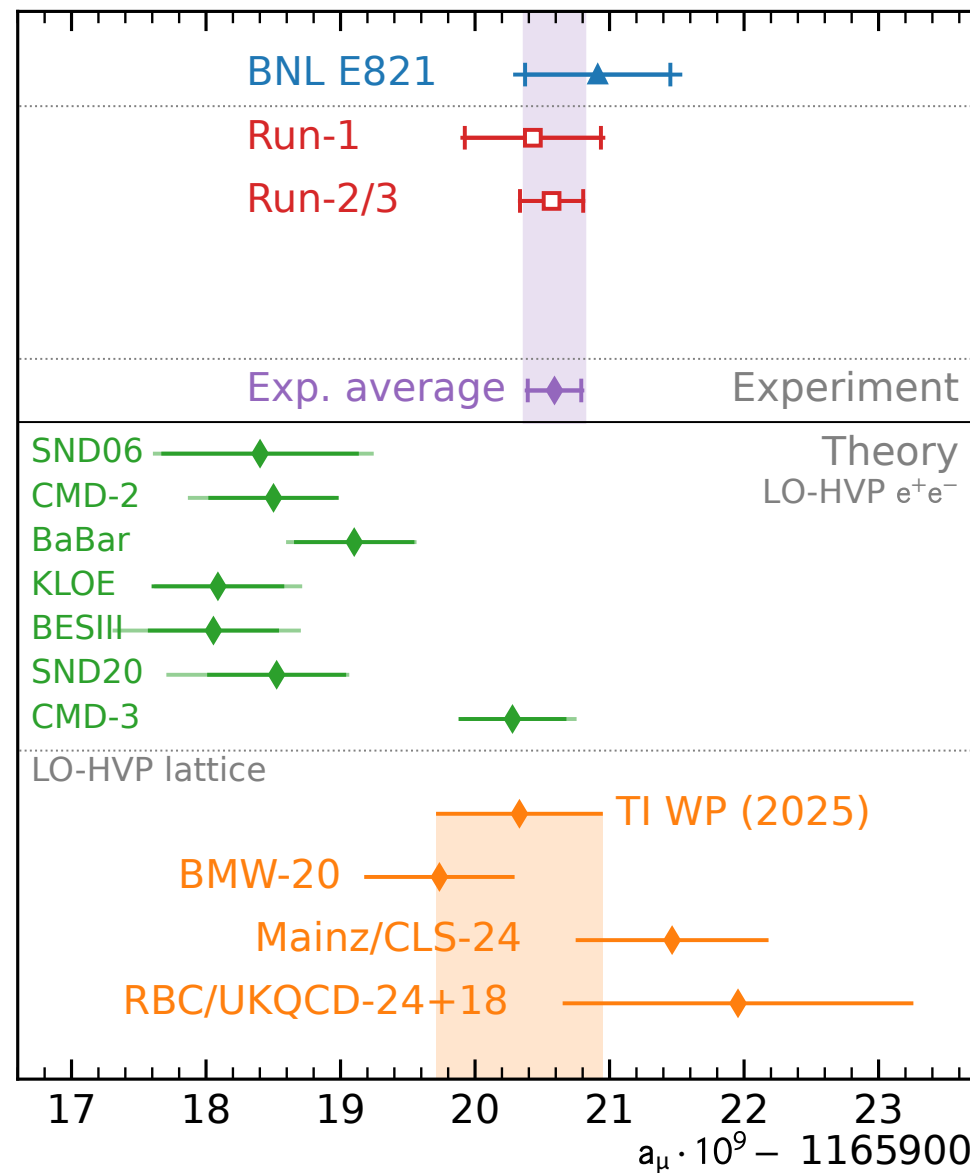


# TI White Paper 2025

New **TI White Paper (2025)** using only lattice-QCD based LO-HVP determination

- Uses input from several published lattice-QCD calculations to compile the WP (2025) value

All the details in  
**TI White Paper 2025**  
arXiv:2505.21476



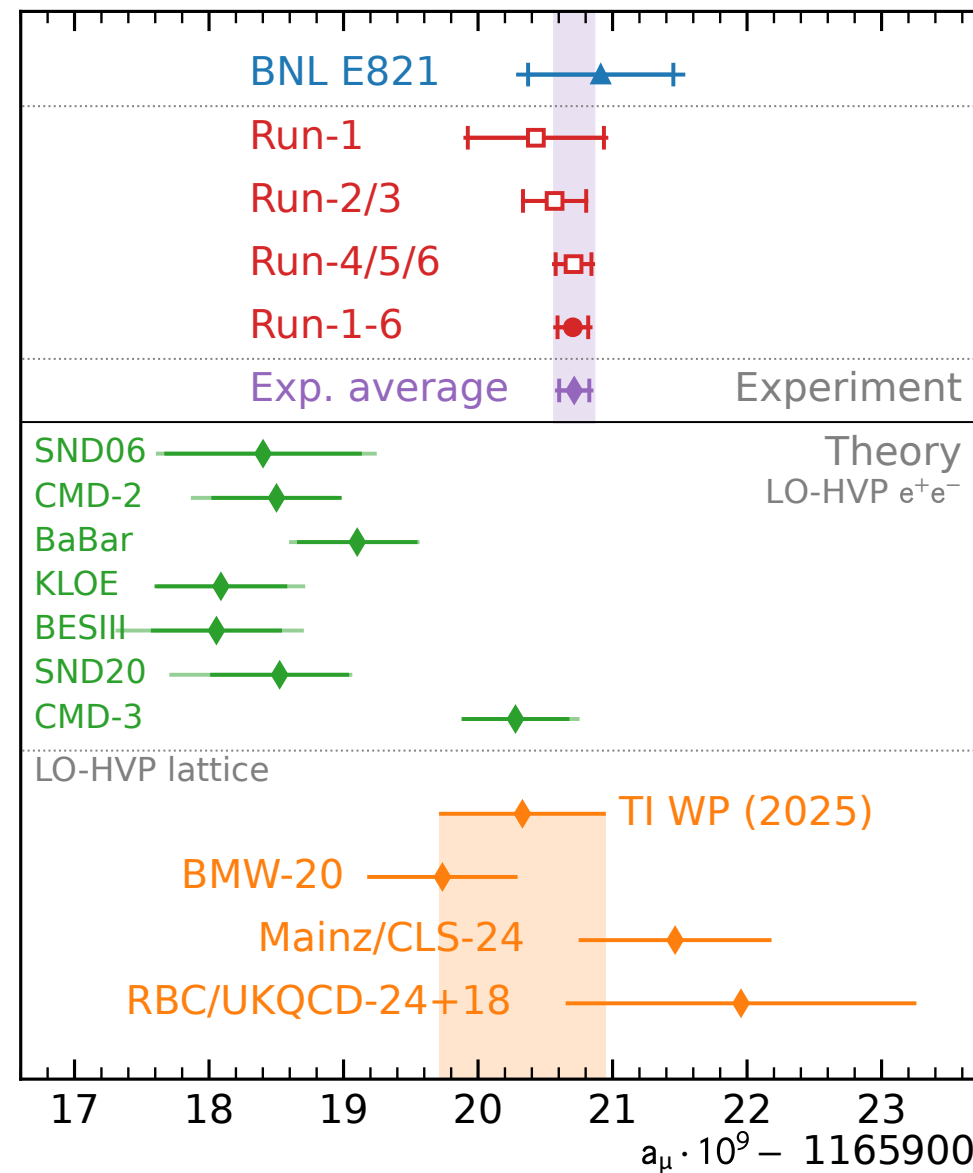
# June 2025: Run-4/5/6

- 2.6 times more data
- Final precision of 127 ppb, more than a 4-fold improvement over the BNL result

## Lepton-Photon 2025 (August)



2025 results are very consistent with 2009 for  $\pi\pi$  contribution to  $a_\mu$



# June 2025: Run-4/5/6

## The MUonE



Alternative way of measuring HPV with muon-electron scattering

Under design/construction at CERN

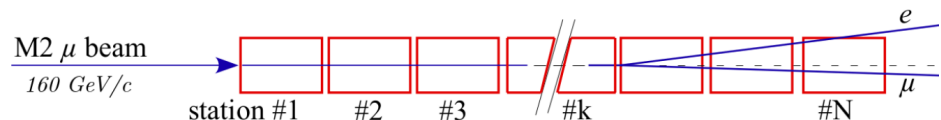
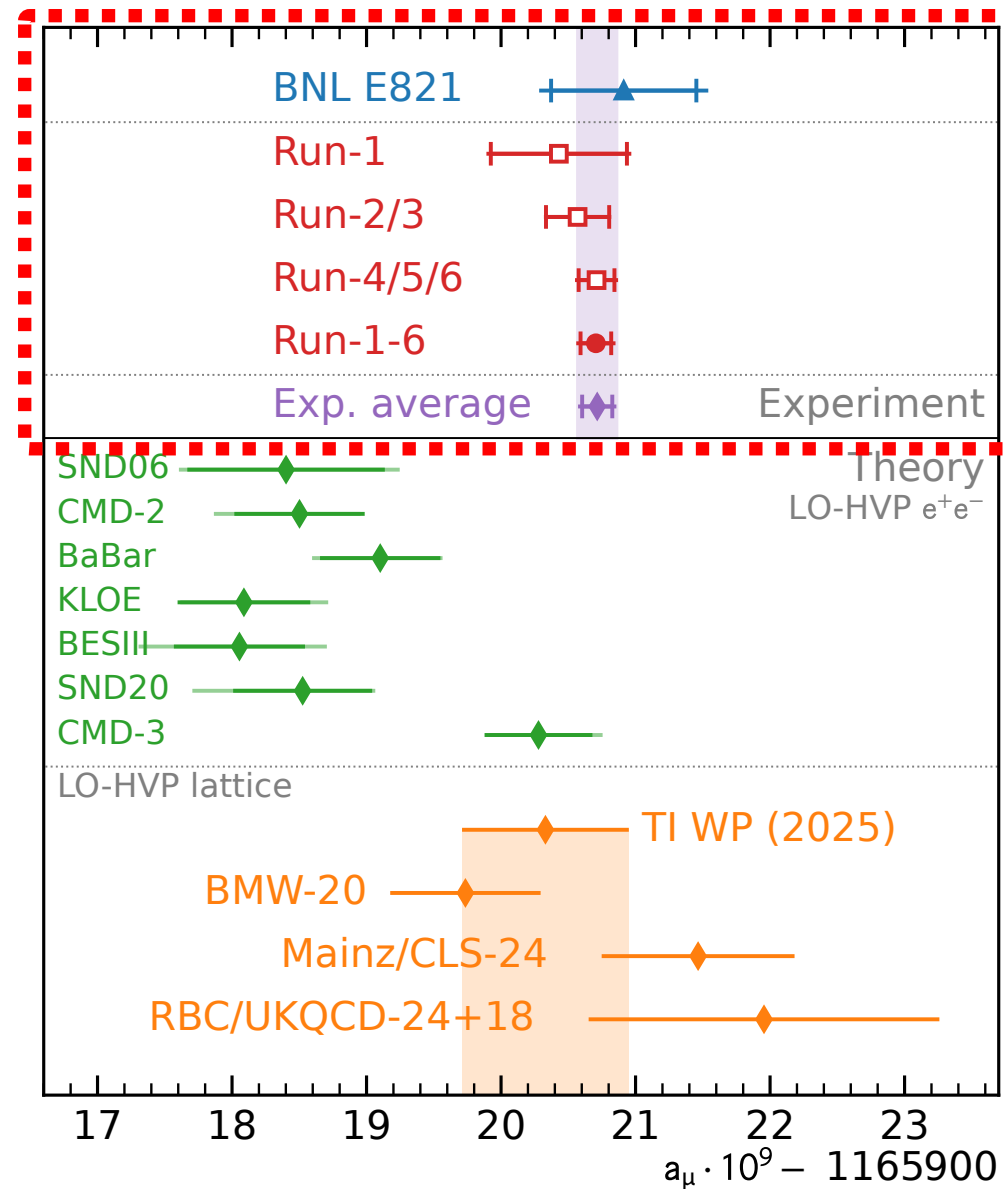



Figure 24: Schematic view of the MUonE experimental apparatus (not to







$$\frac{\omega_a}{\tilde{\omega}'_p} = \frac{\omega_a^m (1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{\langle \omega'_p \times M \rangle (1 + B_k + B_q)}$$

Run-4/5/6

Quantity		Correction (ppb)	Uncertainty (ppb)
$\omega_a^m$ (statistical)		...	114
$\omega_a^m$ (systematic)		...	30
$C_e$	Electric Field	347	27
$C_p$	Pitch	175	9
$C_{pa}$	Phase Acceptance	-33	15
$C_{dd}$	Differential Decay	26	27
$C_{ml}$	Muon Loss	0	2
$\langle \omega'_p \times M \rangle$ (mapping, tracking)		...	34
$\langle \omega'_p \times M \rangle$ (calibration)		...	34
$B_k$	Transient Kicker	-37	22
$B_q$	Transient ESQ	-21	20
$\mu'_p / \mu_B$		...	4
$m_\mu / m_e$		...	22
Total systematic for $\mathcal{R}'_\mu$		...	76
Total for $a_\mu$		572	139

$$a_\mu = \frac{\omega_a}{\tilde{\omega}'_p} \frac{\mu'_p}{\mu_B} \frac{m_\mu}{m_e}$$

Ratio of shielded proton magnetic moment to Bohr magneton

$\mu'_p / \mu_B$ :  $\pm 4$  ppb

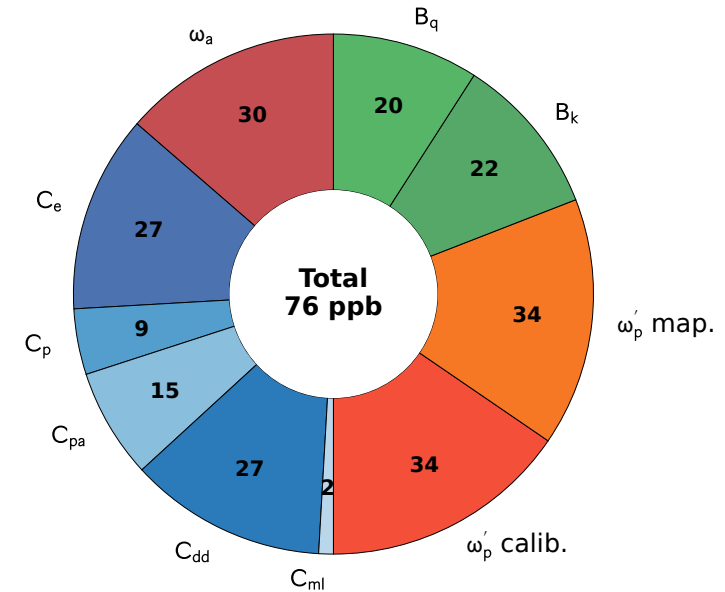
Mass ratio  $m_\mu / m_e$ :  $\pm 22$  ppb

both from CODATA

$$\begin{matrix} \text{⚙️} \end{matrix} \frac{\omega_a}{\tilde{\omega}'_p} = \frac{\omega_a^m (1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{\langle \omega'_p \times M \rangle (1 + B_k + B_q)}$$

Run-4/5/6

Quantity		Correction (ppb)	Uncertainty (ppb)
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$\mu'_p/\mu_B$		...	4
$m_\mu/m_e$		...	22
Total systematic for $\mathcal{R}'_\mu$		...	76
Total for $a_\mu$		572	139



“evenly” distributed

- No dominant source
- Further improving would require to reduce in many categories

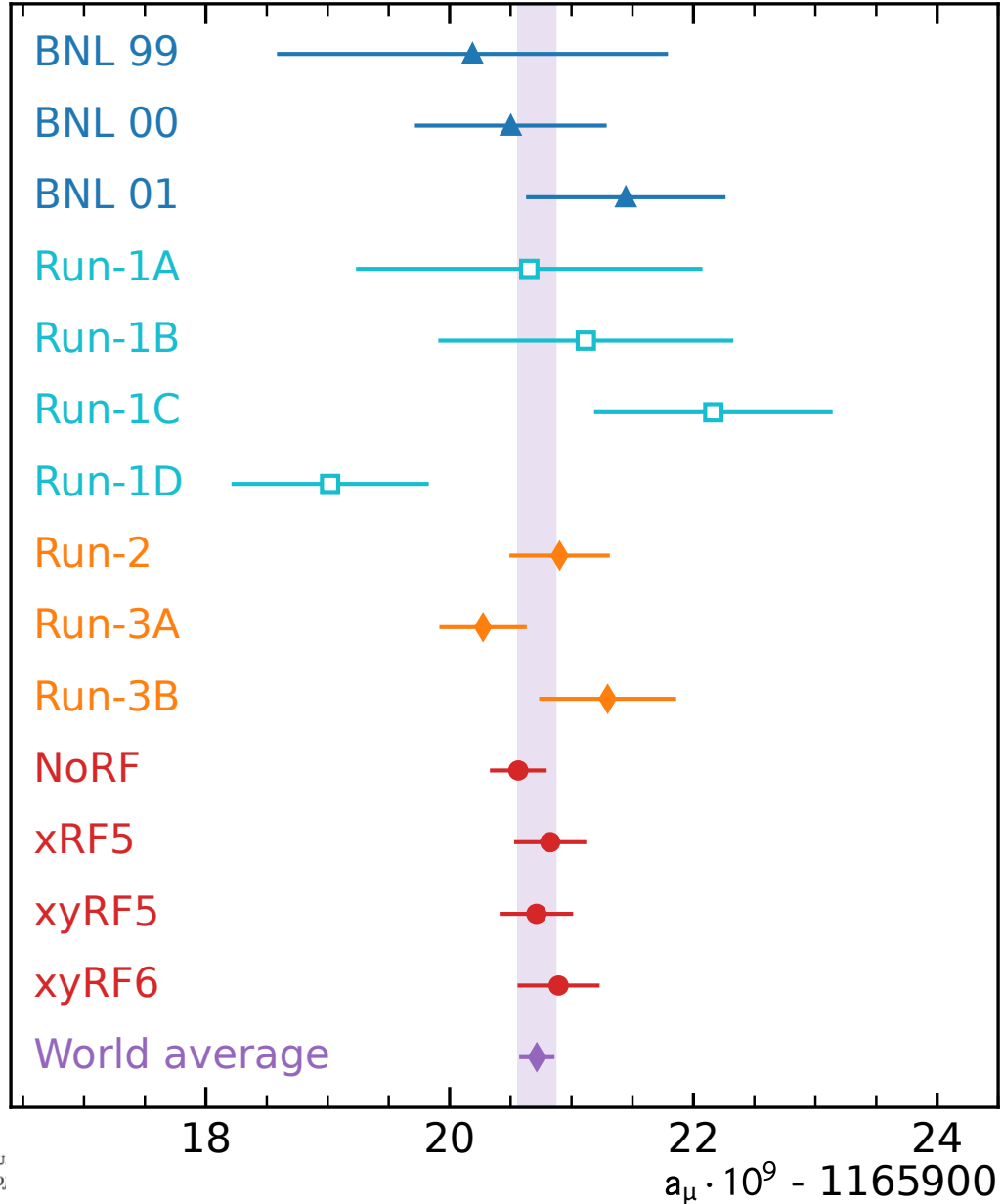
# Uncertainties

$\frac{\omega_a}{\tilde{\omega}'_p}$	Stat. Uncertainty (ppb)	Syst. Uncertainty (ppb)	Total Uncertainty (ppb)
Run-1	434	159*	462
Run-2/3	201	78*	216
Run-4/5/6	114	76	137
Run-1-6	98	78	125
	TDR goal 100 ppb ✓	TDR goal: 100 ppb ✓	TDR goal: 140 ppb ✓



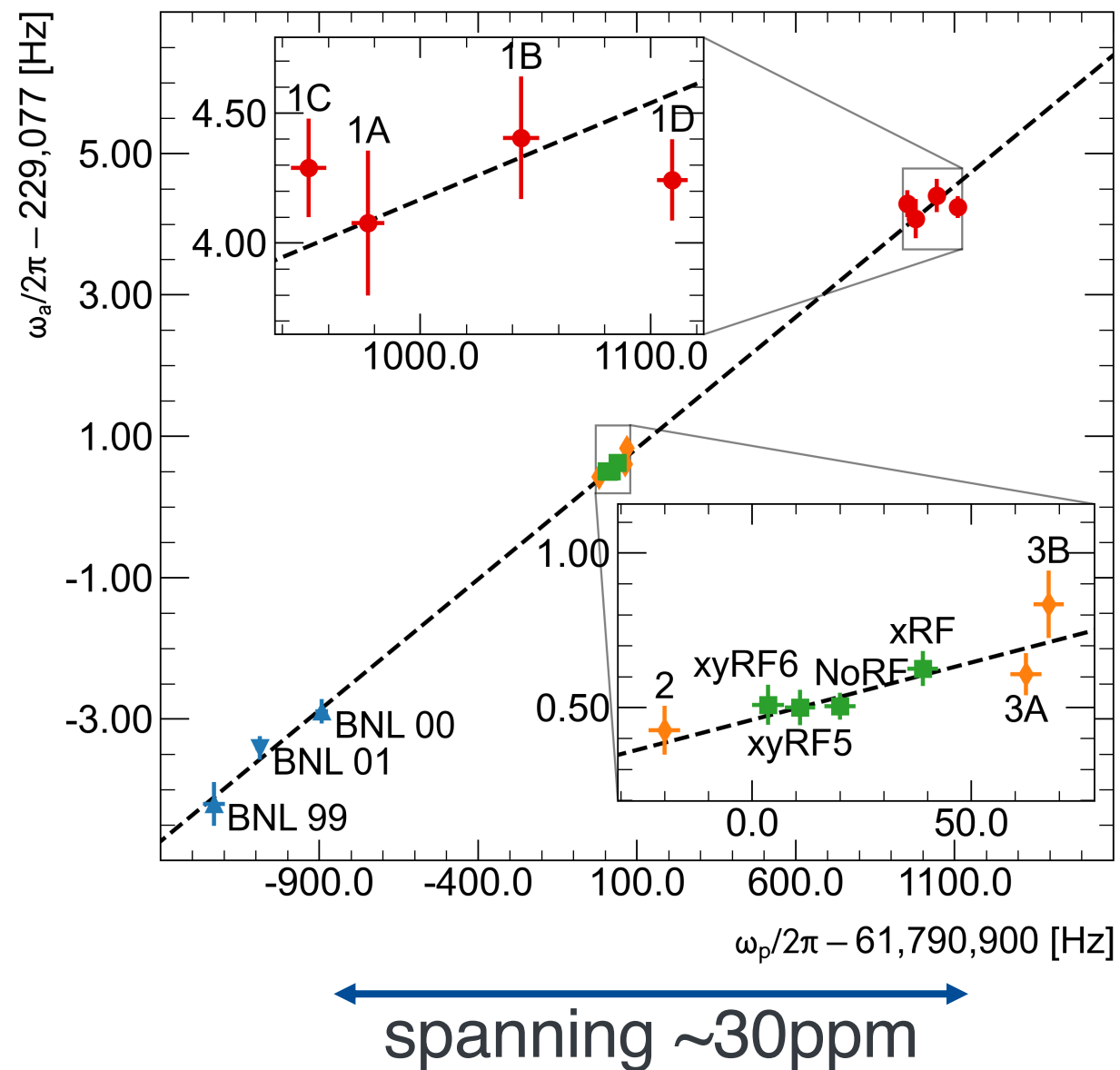


# Consistency Checks

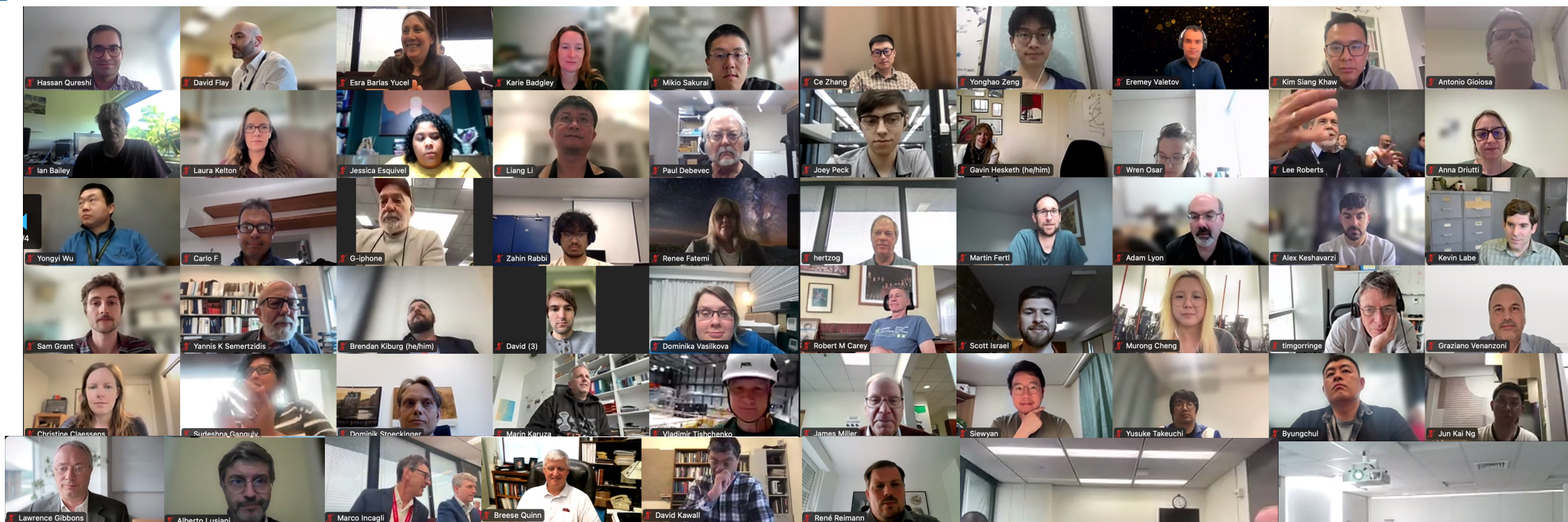


- Each dataset fitted separately
- Published data are averages of blue, orange, and red points

# Consistency Checks



# An incredible Team!



**The Muon g-2 Collaboration:**  
**176 collaborators, 34 institutes, 7 countries**  
**Particle-, Nuclear-, Atomic-, Optical-, Accelerator-, and Theoretical-Physicists and Engineers**





# Is there more?

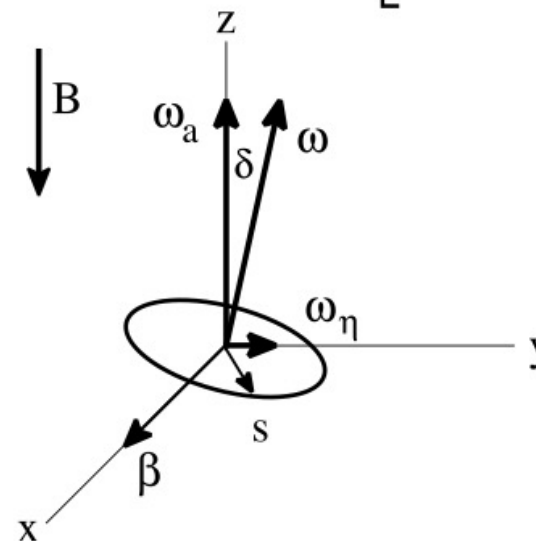
from **Muon g-2 at Fermilab**

- Muon EDM results
- More Beyond Standard Model Analysis:
  - CPT/Lorenz-violating
  - Ultra light Dark Matter

## Muon EDM

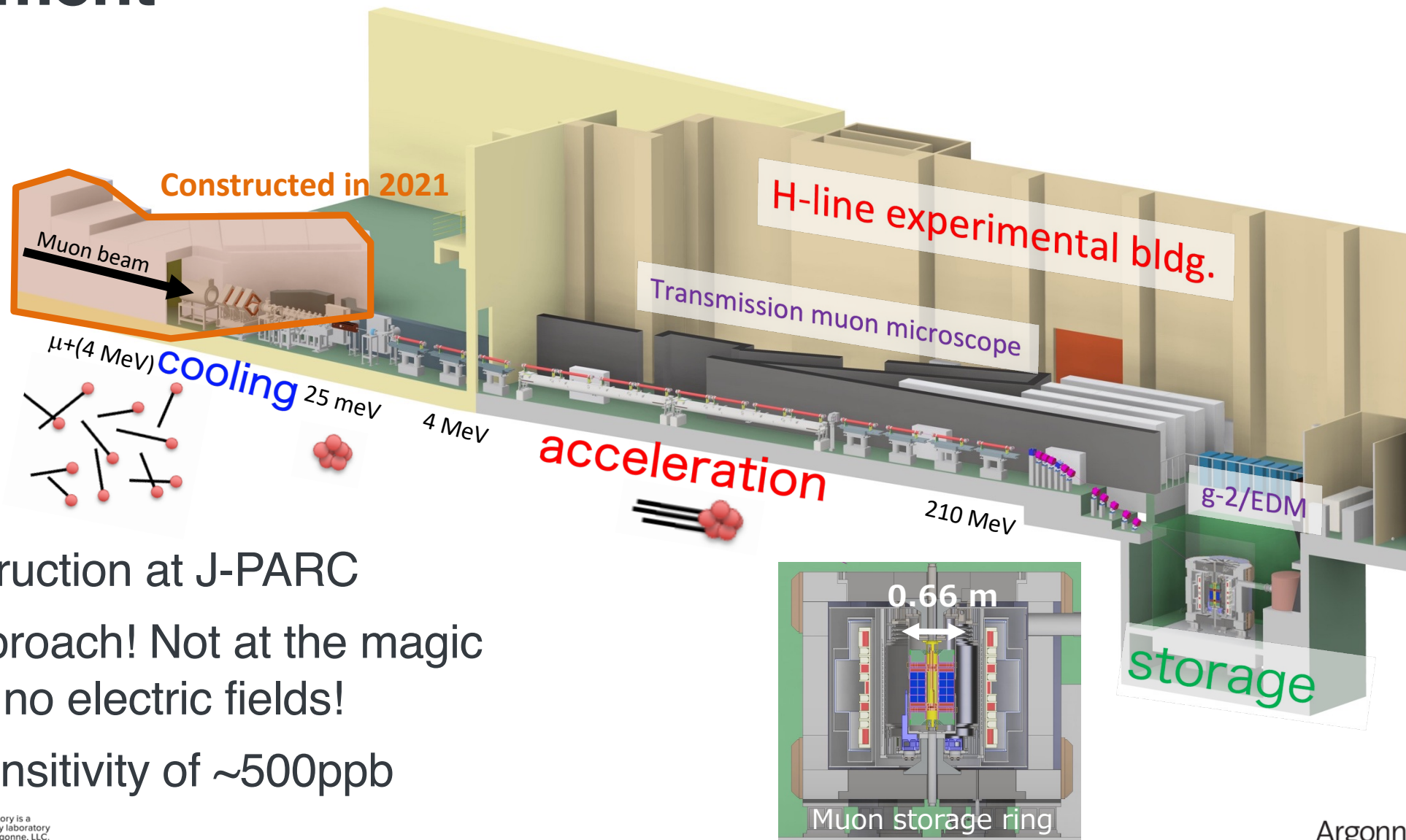
non-zero EDM ( $\eta$ ) modifies the spin equation

$$\vec{\omega}_{a\eta} = a_\mu \frac{e}{m} \vec{B} + \eta \frac{e}{2m} \left[ \frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right]$$



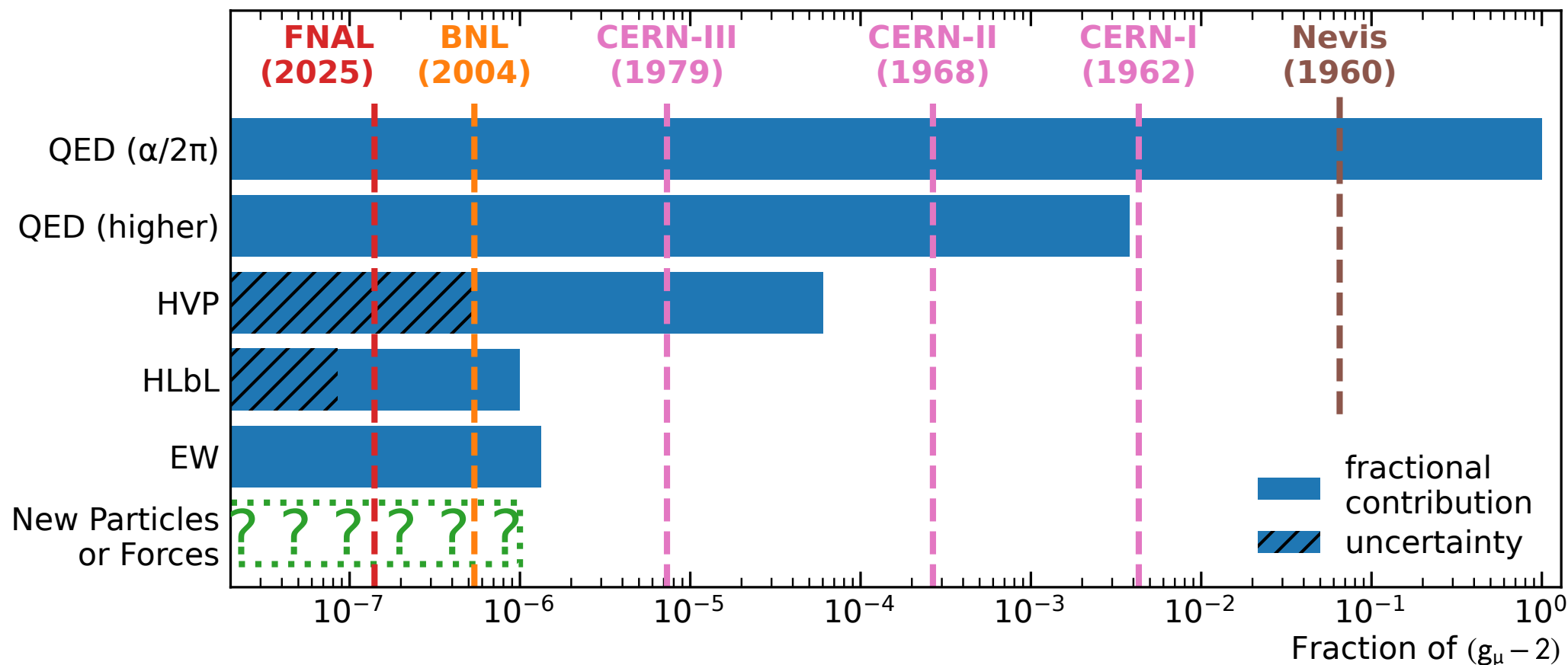
Search for an up/down asymmetry  
out of phase with  $\omega_a$

# Is there more? J-PARC Muon g-2/EDM experiment



- Under construction at J-PARC
- Different approach! Not at the magic momentum/ no electric fields!
- Expected sensitivity of  $\sim 500\text{ppb}$

# Measuring Muon $g-2$ to Test the Standard Model







U.S. DEPARTMENT  
*of* **ENERGY**

This document was prepared by the Muon  $g-2$  Collaboration using the resources of the Fermi National Accelerator Laboratory (Fermilab), a U.S. Department of Energy, Office of Science, Office of High Energy Physics HEP User Facility. Fermilab is managed by FermiForward Discovery Group, LLC, acting under Contract No. 89243024CSC000002.



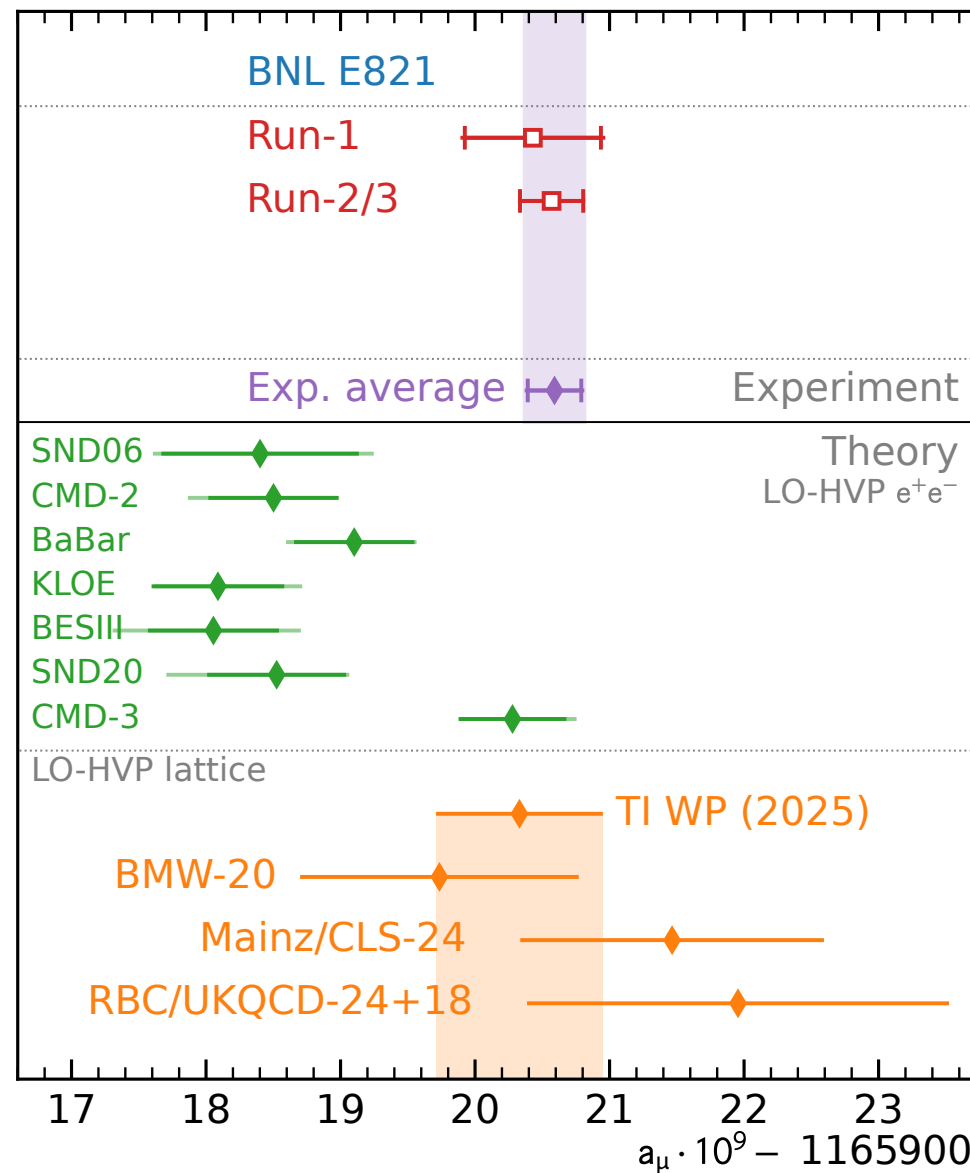
# Muon $g-2$ Theory

# TI White Paper 2025

Last week:

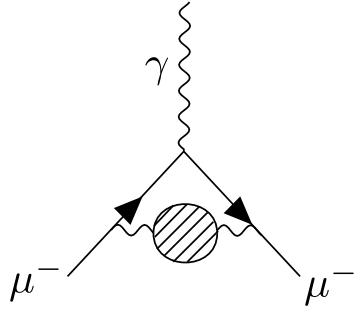
New **TI White Paper (2025)** using only  
lattice-QCD based LO-HVP determination

All the details in  
**TI White Paper 2025**  
arXiv:2505.21476





# LO-HVP: dispersive $e^+e^-$



$$\text{Im} \text{ had.} \sim \left| \text{had.} \right|^2 \longrightarrow a_{\mu}^{\text{HVP,LO}} = \frac{\alpha^2}{3\pi^2} \int_{s_{th}}^{\infty} \frac{K(s)}{s} R(s) ds$$

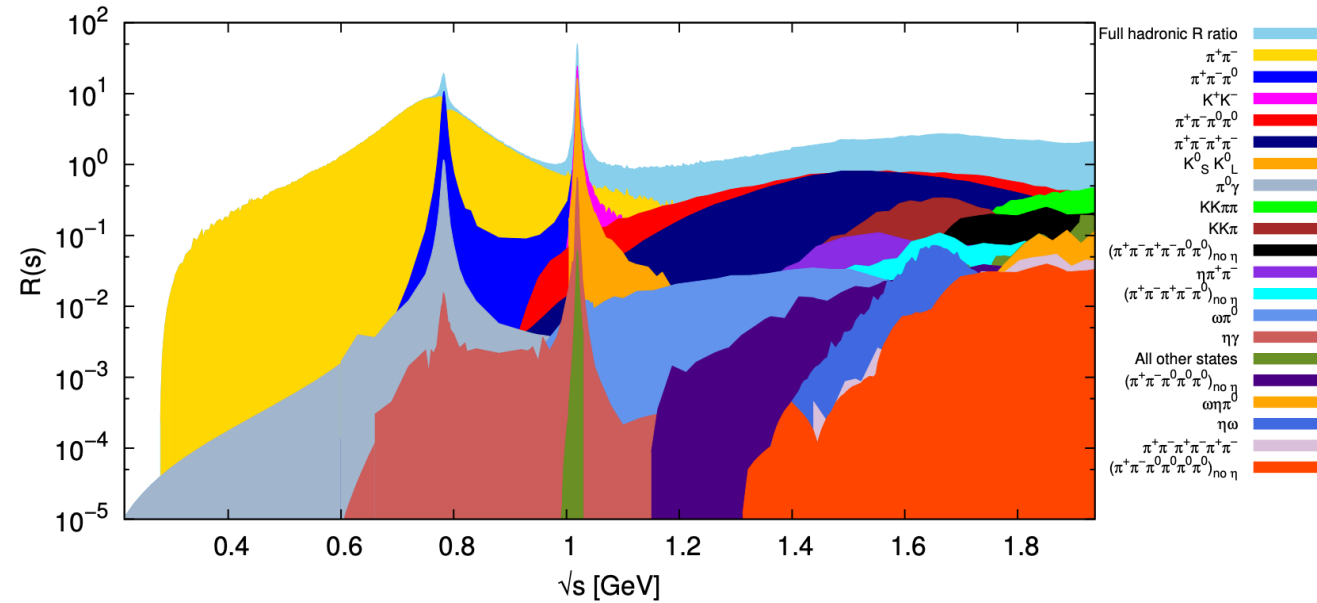


Figure 16: Contributions to the KNT data compilation of the total hadronic  $R$ -ratio from the different hadronic final states below 1.937 GeV [30, 265]. The full  $R$ -ratio is shown in light blue. Each final state is included as a new layer on top in decreasing order of the size of its contribution to  $a_{\mu}^{\text{HVP,LO}}$ .

<https://arxiv.org/pdf/2505.21476>

# WP 2025 – Dispersive LO-HVP [pipi]

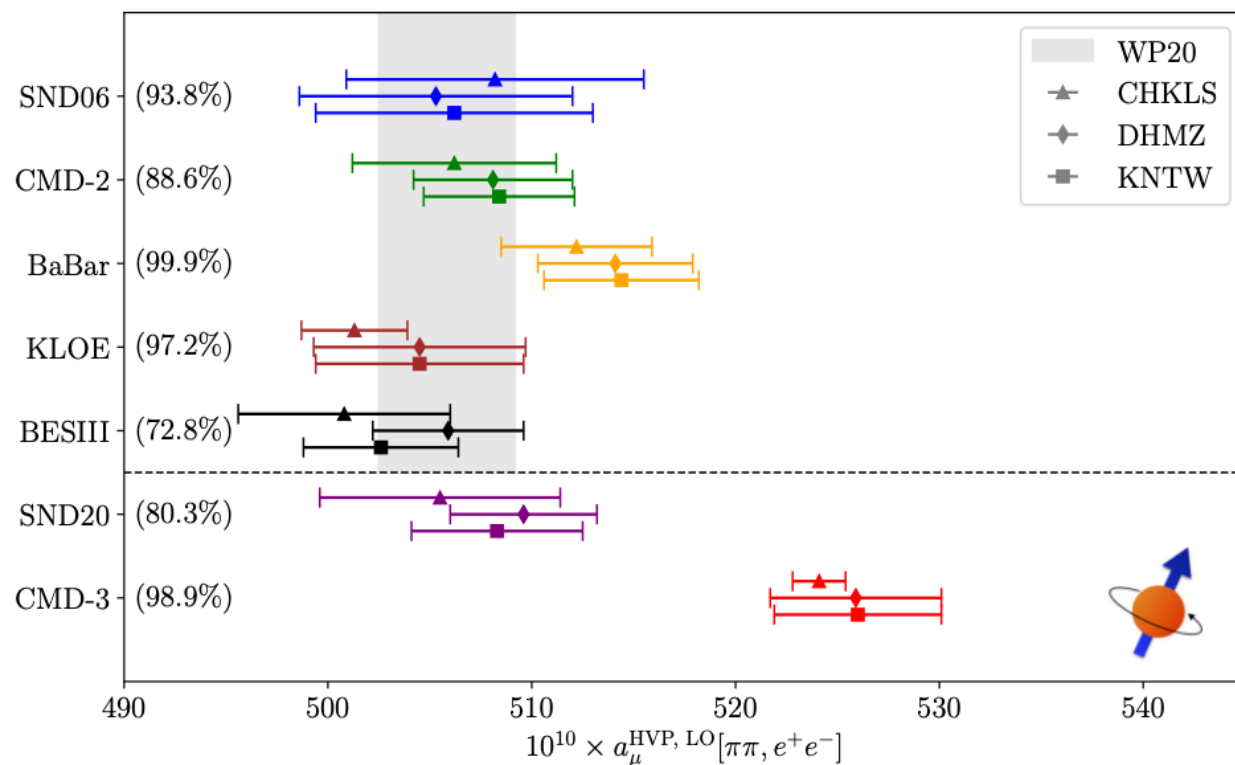


Figure 26: Dispersive theoretical predictions for  $a_\mu^{\text{HVP, LO}}[\pi\pi]$ , based on various measurements of  $e^+e^- \rightarrow \pi^+\pi^-$ , fit/interpolated and complemented for the uncovered mass ranges (percentages of the integral covered by each measurement are shown), for the three approaches “CHKLS,” “DHMZ,” and “KNTW” as detailed in the main text. The gray band indicates the result from WP20, including the error inflation due to the BaBar–KLOE tension. The experiments above the dashed line entered the result for WP20, whilst those below are new measurements since then. The numerical values shown are reproduced in Table 5.

# WP 2025 – Dispersive $a_\mu$

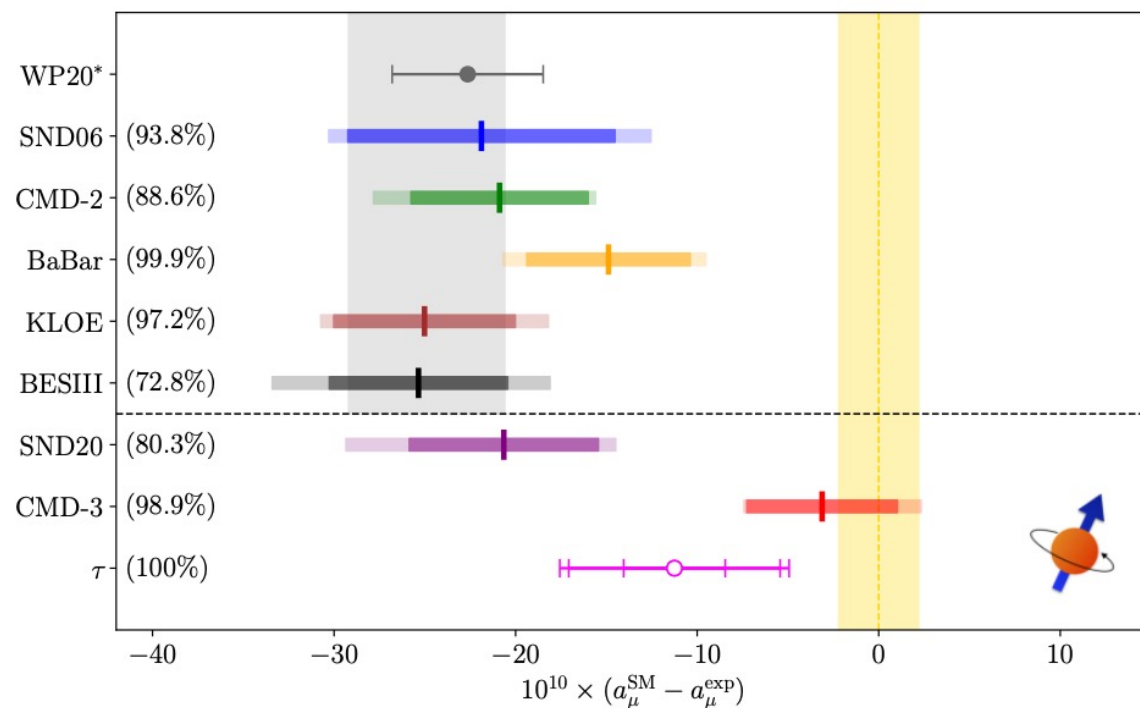


Figure 27: Summary of current data-driven evaluations of HVP, propagated to  $a_\mu^{\text{SM}}$  (the yellow band indicates  $a_\mu^{\text{exp}}$ , the gray band the WP20 SM prediction based on the  $e^+e^-$  data sets above the dashed line and the remainder from WP20, in particular, the WP20 HLbL value; the data point labeled WP20\* indicates the shift upon using WP25 input for the other contributions besides LO HVP). The  $\tau$  point corresponds to WP25 in Fig. 13, with the third, outmost error including the additional uncertainties beyond the  $2\pi$  channel (the remainder of HVP is taken from WP20, the other contributions from WP25). The other points use input from the various  $e^+e^- \rightarrow \pi^+\pi^-$  experiments according to Fig. 26 (again with HVP remainder from WP20 and the other contributions from WP25), where for each experiment the central values are obtained as simple average of the three combination methods, the inner ranges as simple average of the uncertainties obtained in each method, and the outer ranges reflect the maximal range covered by all methods (the percentages indicate how much of the  $2\pi$  contribution to the HVP integral is covered by each measurement). We emphasize that these ranges are merely meant to illustrate the current spread, they cannot be interpreted as uncertainties with a proper statistical meaning. The numerical values follow from Tables 1 and 5.



# WP 2025 – $a_\mu$

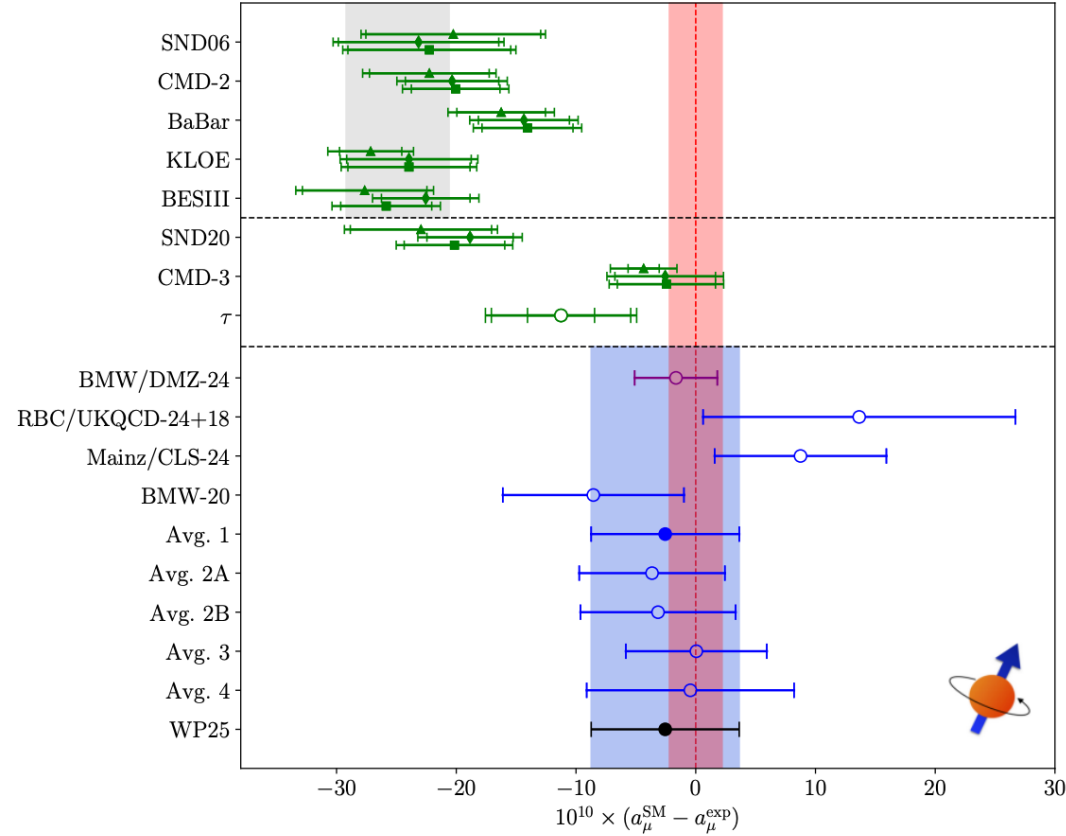


Figure 40: Final summary of various determinations of  $a_\mu^{\text{HVP,LO}}$  discussed in Secs. 2 and 3, propagated to  $a_\mu^{\text{SM}}$ . The first two panels refer to data-driven determinations, where the three points for each  $e^+e^-$  experiment reflect the “CHKLS,” “DHMZ,” and “KNTW” methods, see Figs. 26 and 27 for more details. The gray band indicates the WP20 result, based on the  $e^+e^-$  experiments above the first dashed line. The  $\tau$  point corresponds to Eq. (2.23). The last panel summarizes lattice-QCD determinations, including the hybrid evaluation [23], the three individual lattice-QCD calculations shown in Fig. 36, and the five lattice HVP averages from Fig. 37. The blue band refers to the final WP25 result, which coincides with “Avg. 1.” In all cases, except for the gray WP20 band, the remaining contributions to  $a_\mu^{\text{SM}}$  beyond  $a_\mu^{\text{HVP,LO}}$  are taken from WP25, as given in Table 1. The red band denotes the experimental world average.

# WP 2025 – $a_\mu$

Contribution	Section	Equation	Value $\times 10^{11}$	References
Experiment (E989)		Eq. (9.5)	116 592 059(22)	Refs. [5–7, 9–12]
HVP LO (lattice)	Sec. 3.6.1	Eq. (3.37)	7132(61)	Refs. [13–29]
HVP LO ( $e^+e^-$ , $\tau$ )	Sec. 2	Table 5	Estimates not provided at this point	
HVP NLO ( $e^+e^-$ )	Sec. 2.9	Eq. (2.47)	–99.6(1.3)	Refs. [30, 31]
HVP NNLO ( $e^+e^-$ )	Sec. 2.9	Eq. (2.48)	12.4(1)	Ref. [32]
HLbL (phenomenology)	Sec. 5.10	Eq. (5.69)	103.3(8.8)	Refs. [33–56]
HLbL NLO (phenomenology)	Sec. 5.10	Eq. (5.70)	2.6(6)	Ref. [57]
HLbL (lattice)	Sec. 6.2.8	Eq. (6.34)	122.5(9.0)	Refs. [58–62]
HLbL (phenomenology + lattice)	Sec. 9	Eq. (9.2)	112.6(9.6)	Refs. [33–56, 58–62]
QED	Sec. 7.5	Eq. (7.27)	116 584 718.8(2)	Refs. [63–69]
EW	Sec. 8	Eq. (8.12)	154.4(4)	Refs. [50, 70–72]
HVP LO (lattice) + HVP N(N)LO ( $e^+e^-$ )	Sec. 9	Eq. (9.1)	7045(61)	Refs. [13–32]
HLbL (phenomenology + lattice + NLO)	Sec. 9	Eq. (9.3)	115.5(9.9)	Refs. [33–62]
Total SM Value	Sec. 9	Eq. (9.4)	116 592 033(62)	Refs. [13–72]
Difference: $\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}}$	Sec. 9	Eq. (9.6)	26(66)	

Table 1: Summary of the contributions to  $a_\mu^{\text{SM}}$ . The experimental number refers to the world average completely dominated by E989. The subsequent block summarizes the pertinent hadronic contributions from Secs. 2, 3, 5, and 6 as well as the combination of data-driven and lattice-QCD evaluations of HLbL scattering from Sec. 9. The second block summarizes the quantities entering our recommended SM value, in particular, the total HVP contribution (using lattice QCD for LO and  $e^+e^-$  for higher-order iterations) and the total HLbL number. The construction of the total HLbL contribution takes into account correlations among the terms at different orders, and the final rounding includes subleading digits at intermediate stages.

<https://arxiv.org/pdf/2505.21476>

# WP 2020 – Lattice

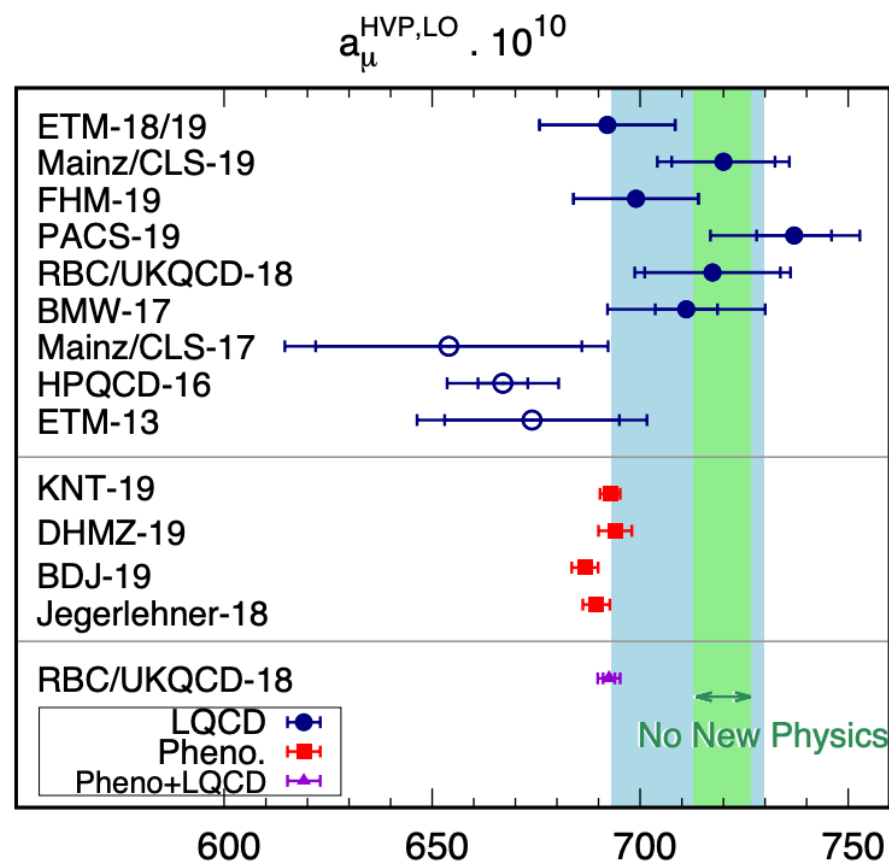


Figure 44: Compilation of recent results for  $a_\mu^{\text{HVP,LO}}$  in units of  $10^{-10}$ . The filled dark blue circles are lattice results that are included in the “lattice world average”. The average, which is obtained from a conservative averaging procedure in Sec. 3.5.1, is indicated by a light blue band, while the light-green band indicates the “no new physics” scenario, where  $a_\mu^{\text{HVP,LO}}$  results are large enough to bring the SM prediction of  $a_\mu$  into agreement with experiment. The unfilled dark blue circles are lattice results that are older or superseded by more recent calculations. The red squares indicate results obtained from the data-driven methods reviewed in Sec. 2. See Table 8 for more information on the results included in the plot. Adapted from Ref. [443].



# Beam Dynamics

# Momentum Distribution

## Trackers

**Parasitic:** Dispersion & Beam Dynamics  
(Improved uncertainties from MiniSciFi)

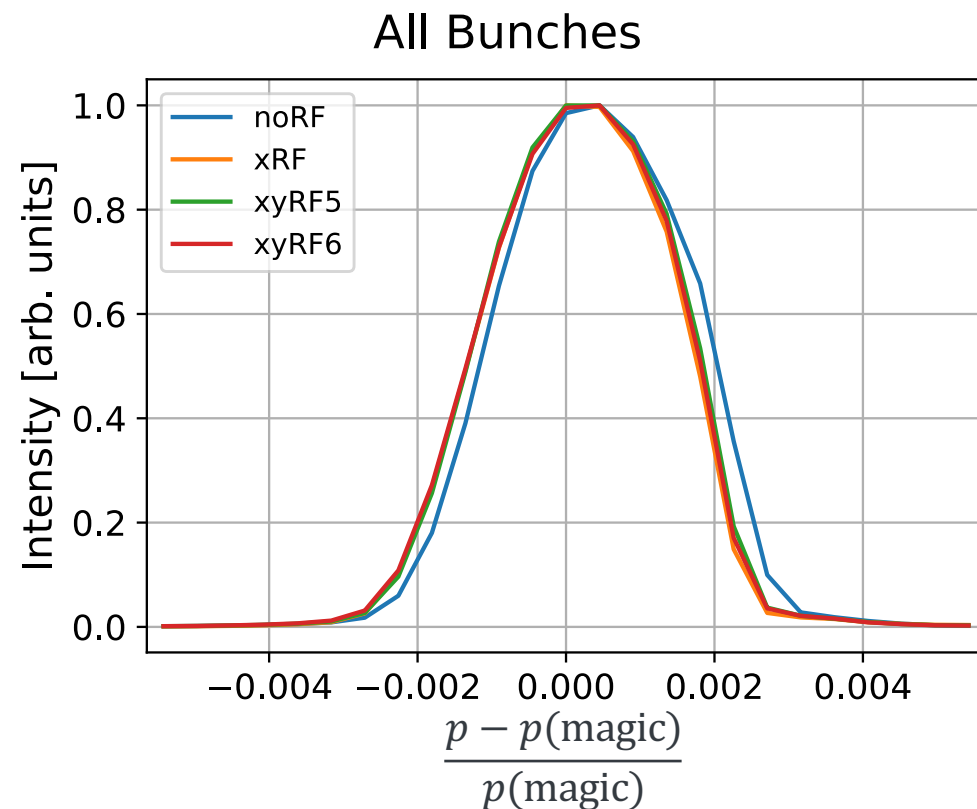
## Calorimeters

**Parasitic:** Muon Dephasing  
taking time-in-bunch into account  
(improved robustness of method)

## **NEW!** Minimally Intrusive Scintillating Fiber Detector (MiniSciFi)

Vertical and Horizontal versions

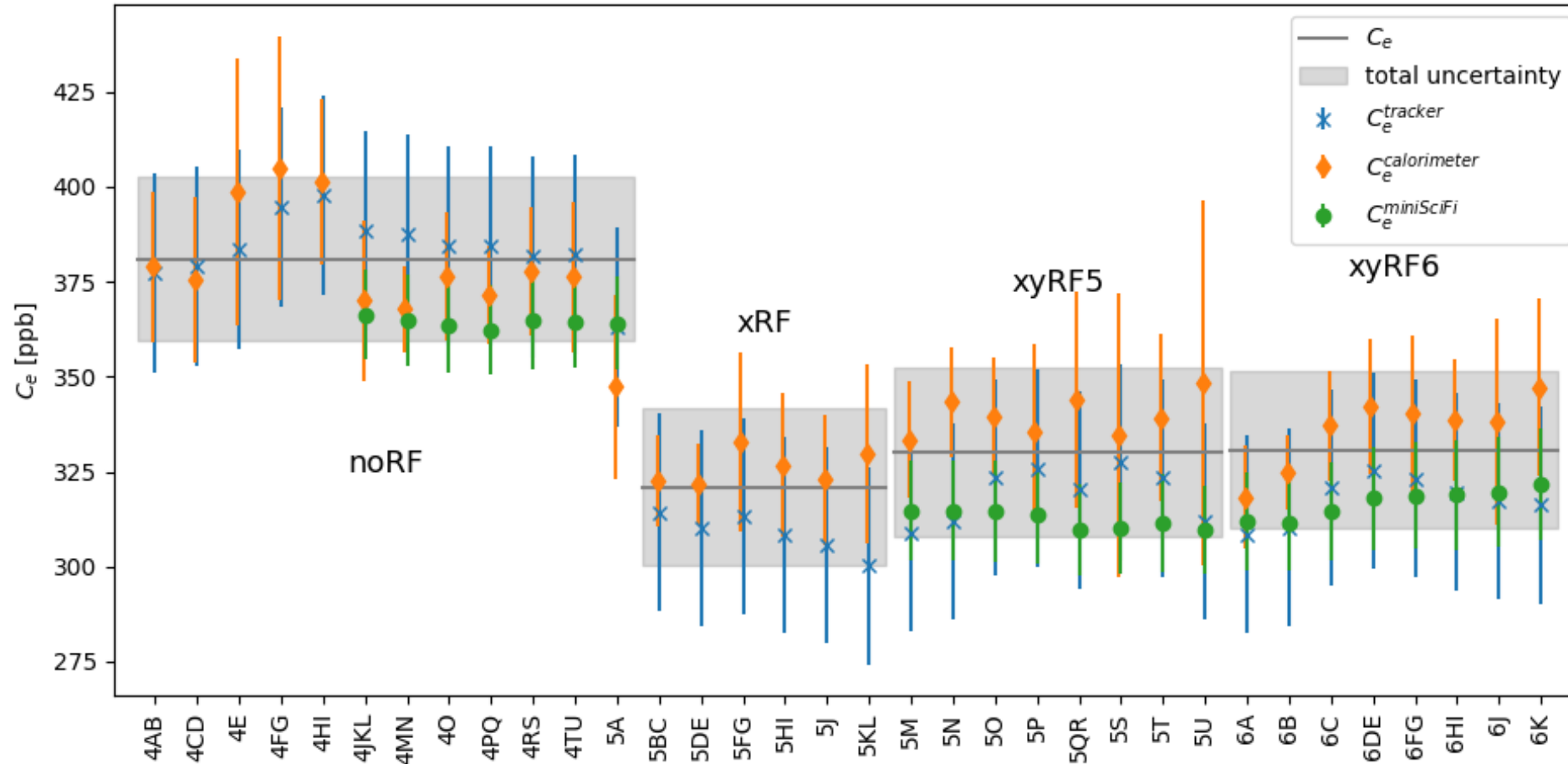
**Dedicated studies:** Cross-checks and  
uncertainty determination (tracker)





# Electric-Field Correction: $C_e$

The largest correction



Increased confidence and small reduction of uncertainties to total of **27 ppb**.



# Momentum Spectrum

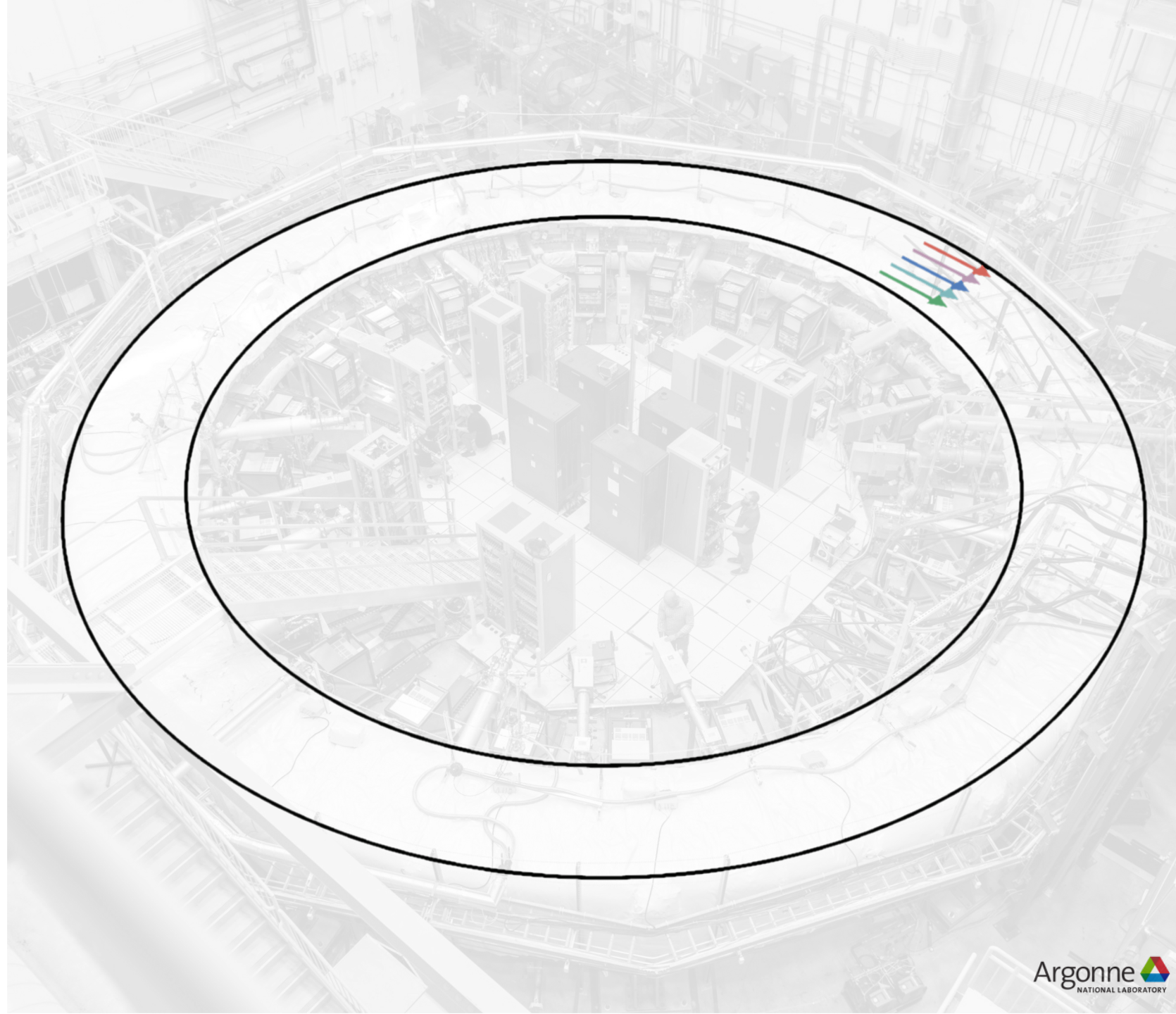
**Higher momentum** muons:

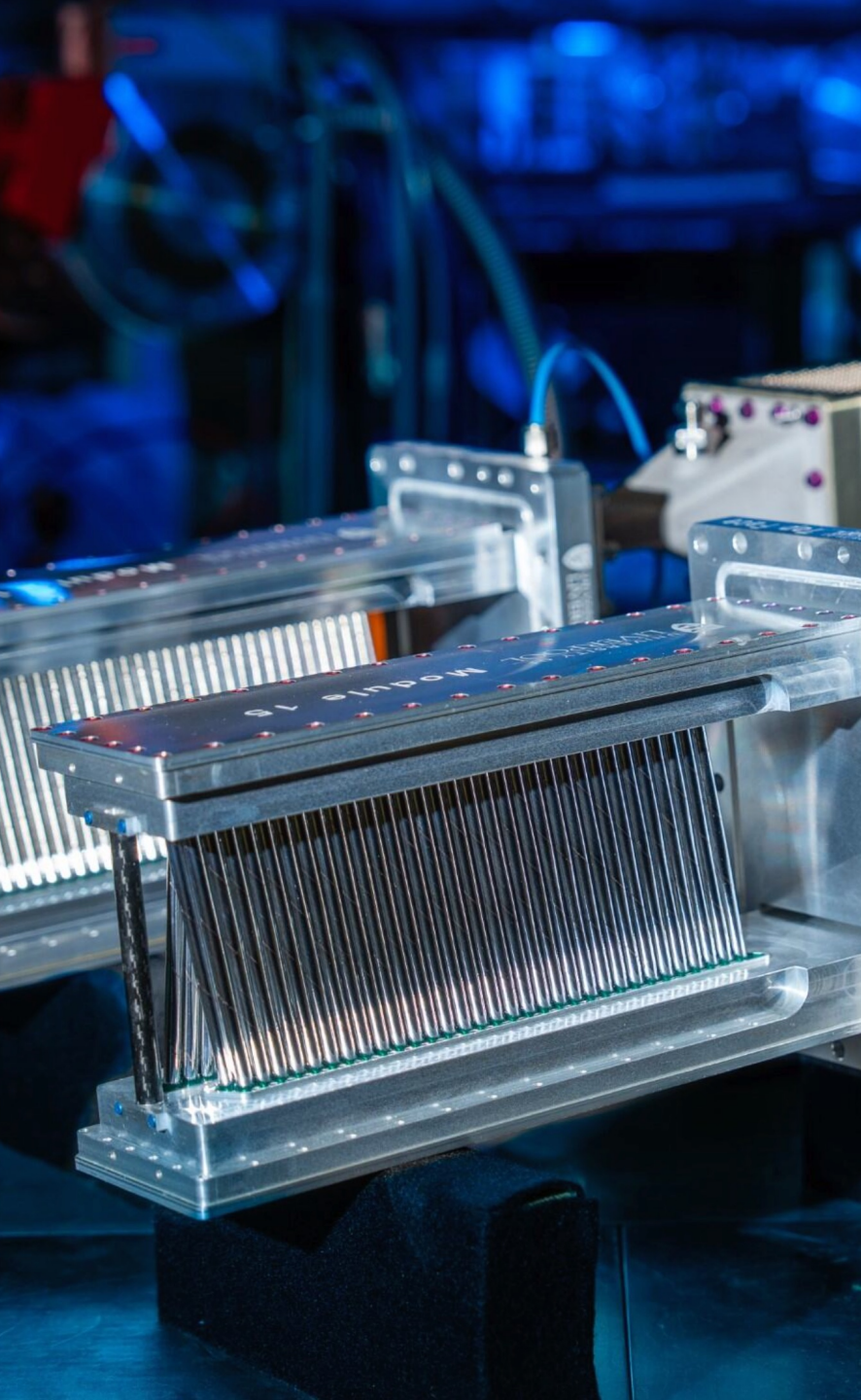
- stored at **larger radii**
- take **longer** to go around

**Lower momentum** muons:

- stored at **smaller radii**
- take **shorter** to go around

**Dephasing and radial position** used to extract the stored momentum spectrum





# Pitch Correction $C_p$

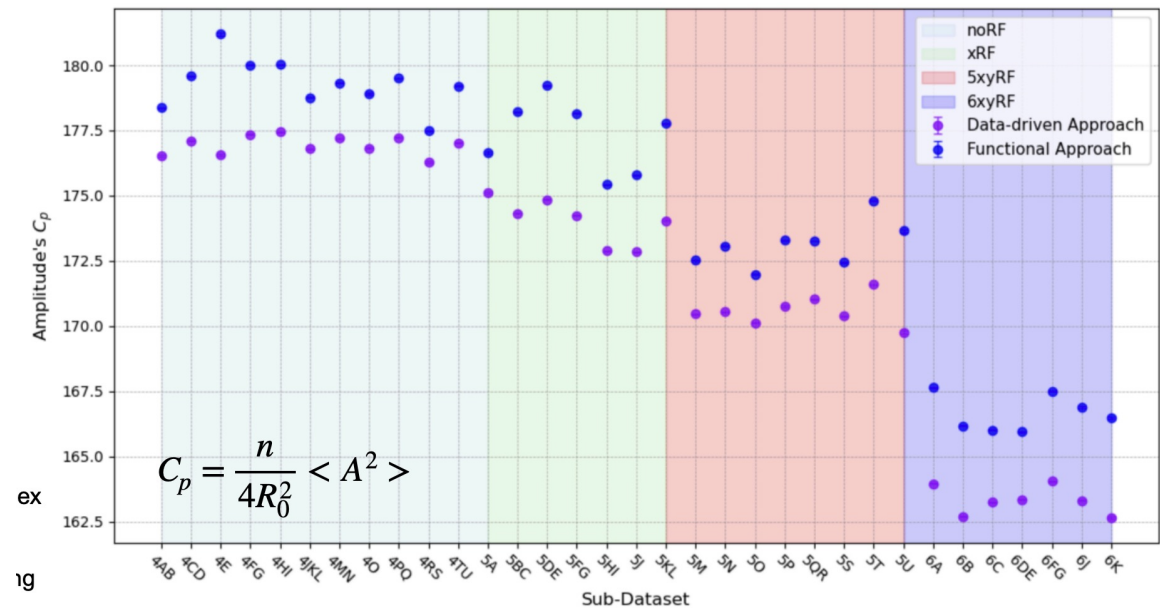
A pitch reduces the measured spin precession

## Trackers

Measure muon's vertical position,  
derive **vertical oscillation amplitudes**

## Simulation Frameworks

Extrapolate from trackers to around the ring  
(also user for other analysis parts)







# Corrections: Time-Dependent Mean Phase

Time-dependent phase changes of the muon ensemble bias  $\omega_a^m$

## Phase Acceptance $C_{pa}$

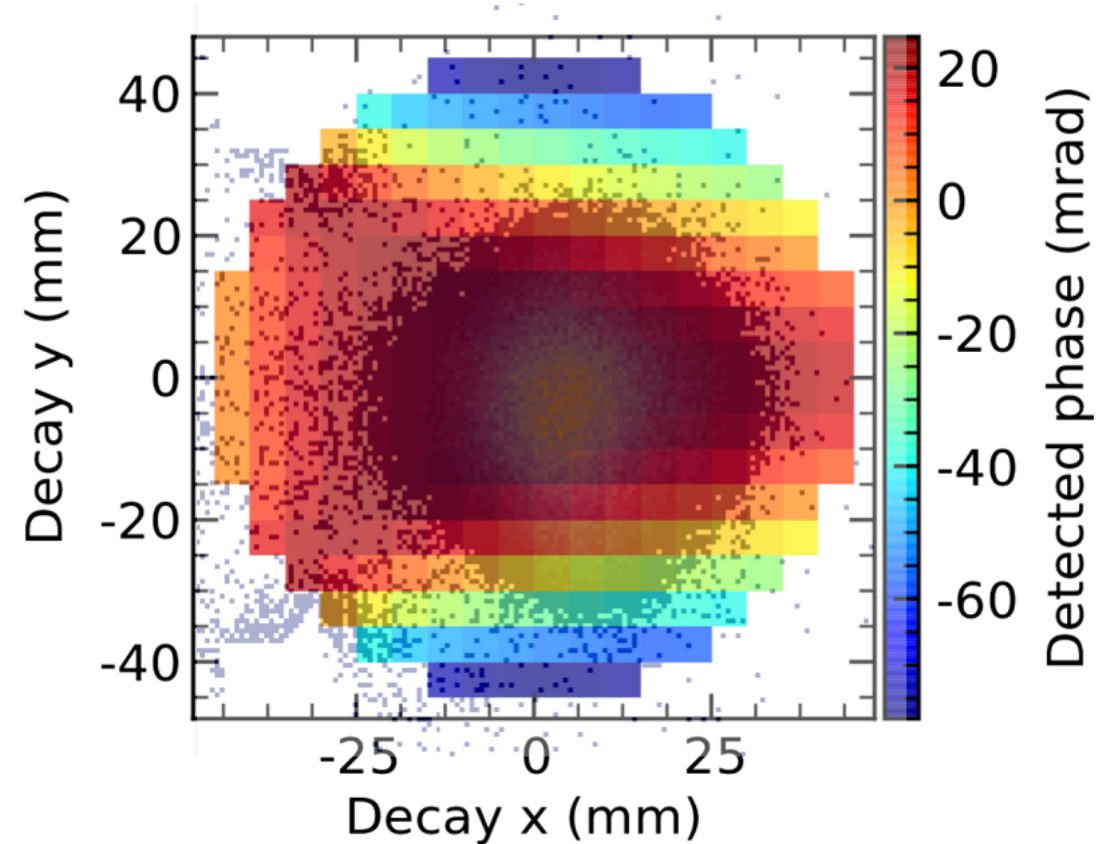
Detector Acceptances x Beam Motion

## Differential Decay $C_{dd}$

Momentum-dependent muon lifetime x  
phase-momentum correlations

## Muon Loss $C_{ml}$

Mechanical muon losses







# Corrections: Time-Dependent Mean Phase

Time-dependent phase changes of the muon ensemble bias  $\omega_a^m$

## Phase Acceptance $C_{pa}$

Detector Acceptances x Beam Motion

## Differential Decay $C_{dd}$

Momentum-dependent muon lifetime x  
phase-momentum correlations

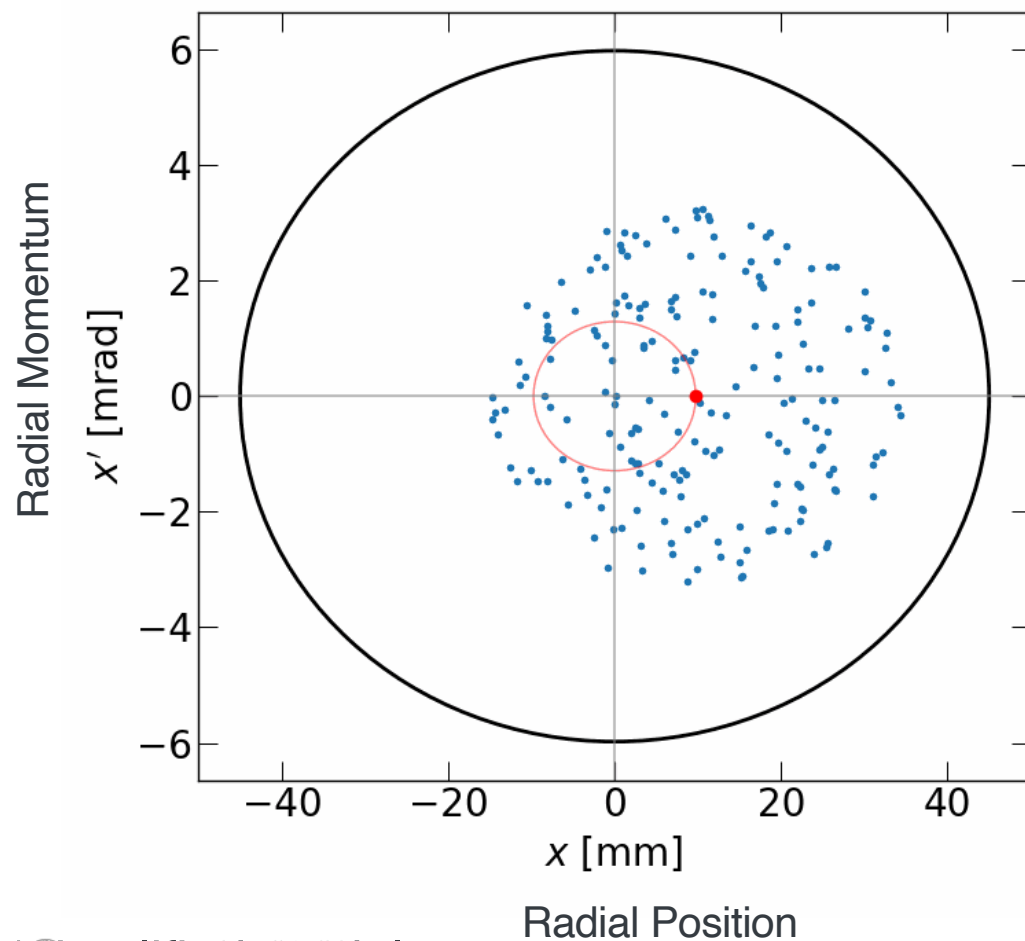
## Muon Loss $C_{ml}$

Mechanical muon losses

- 2 components: **Injection** and **longitudinal** components
- **New!** **Injection component** from simulation frameworks
  - Before: split into 2 components
  - Before: Sign mistake in one contribution  $C_{dd}^{beamline}$   
+32 ppb shift in Run-2/3 results

# How does the RF work?

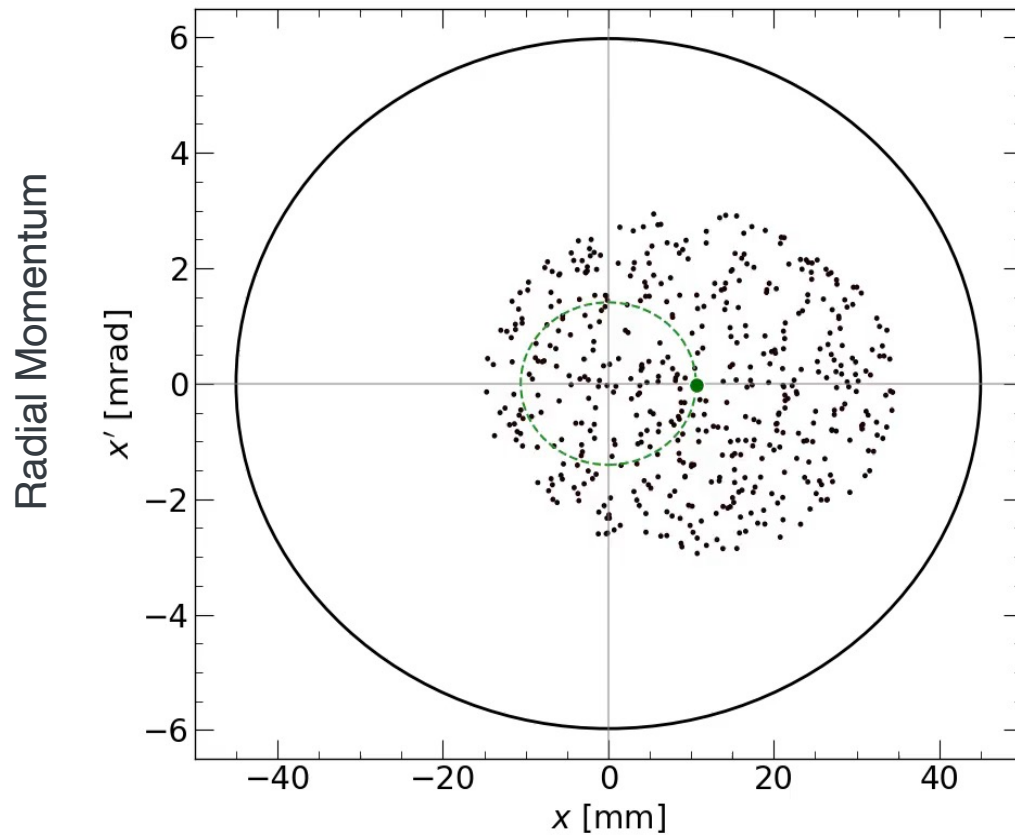
Beam oscillation: average of all muons





# How does the RF work?

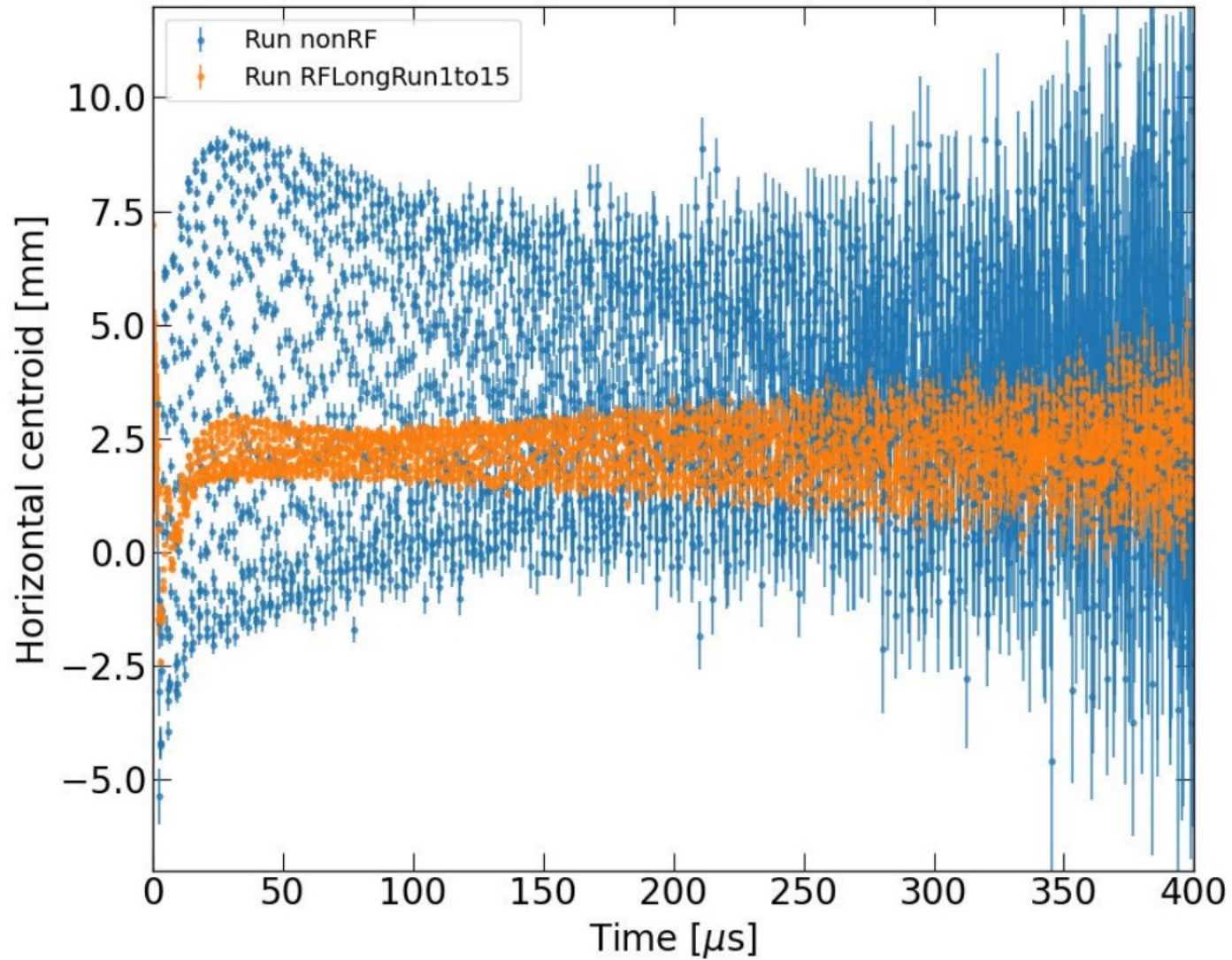
Beam oscillation: average of all muons



- RF acts like a forced harmonic oscillator (for 6  $\mu$ s)
- If tuned correctly to the CBO frequency:
  - Phase-shifts different muon distributions
  - Reduces the oscillation of the **mean** of the particle ensemble (reduces the coherence)

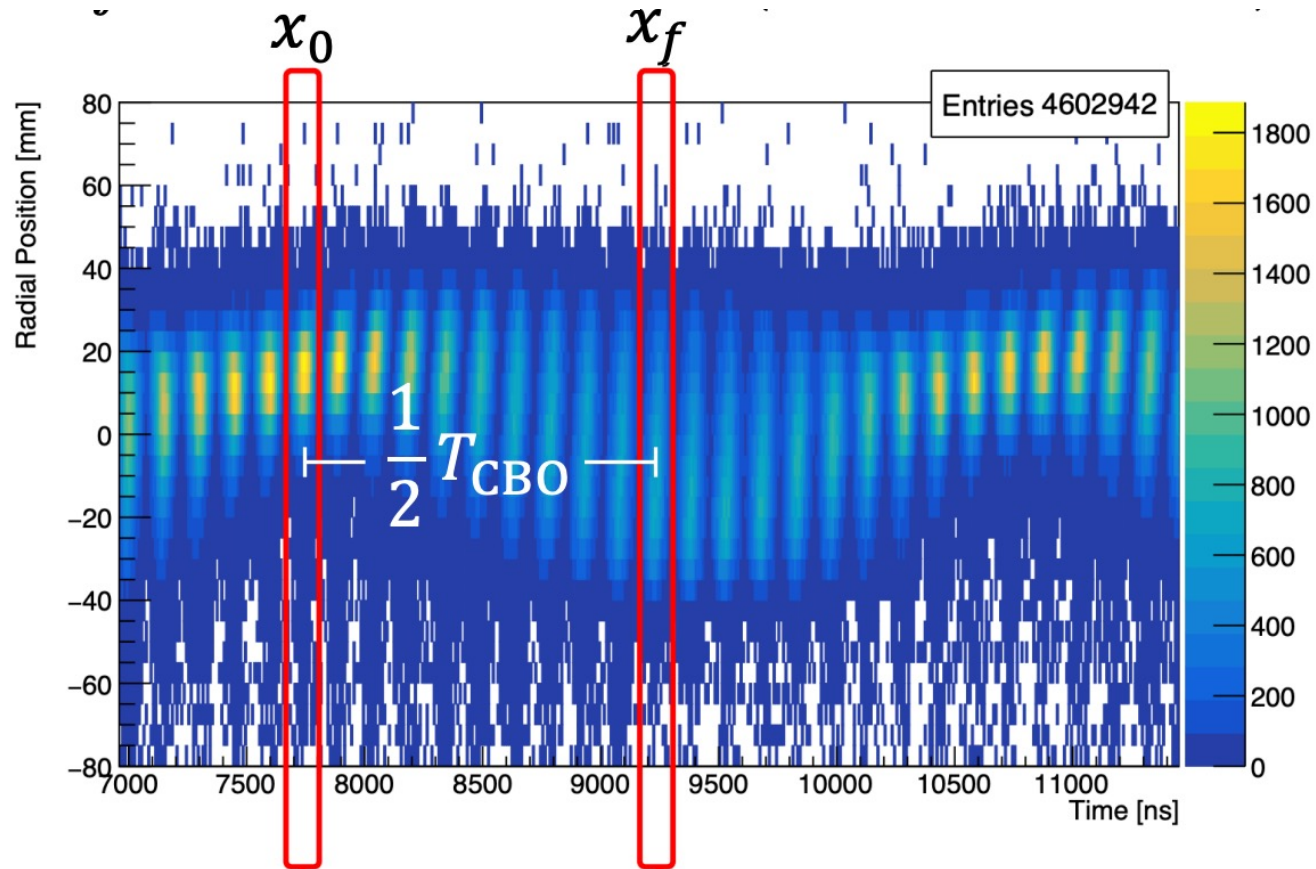


# RF effect on CBO



# ⚙ Electric-Field trackers

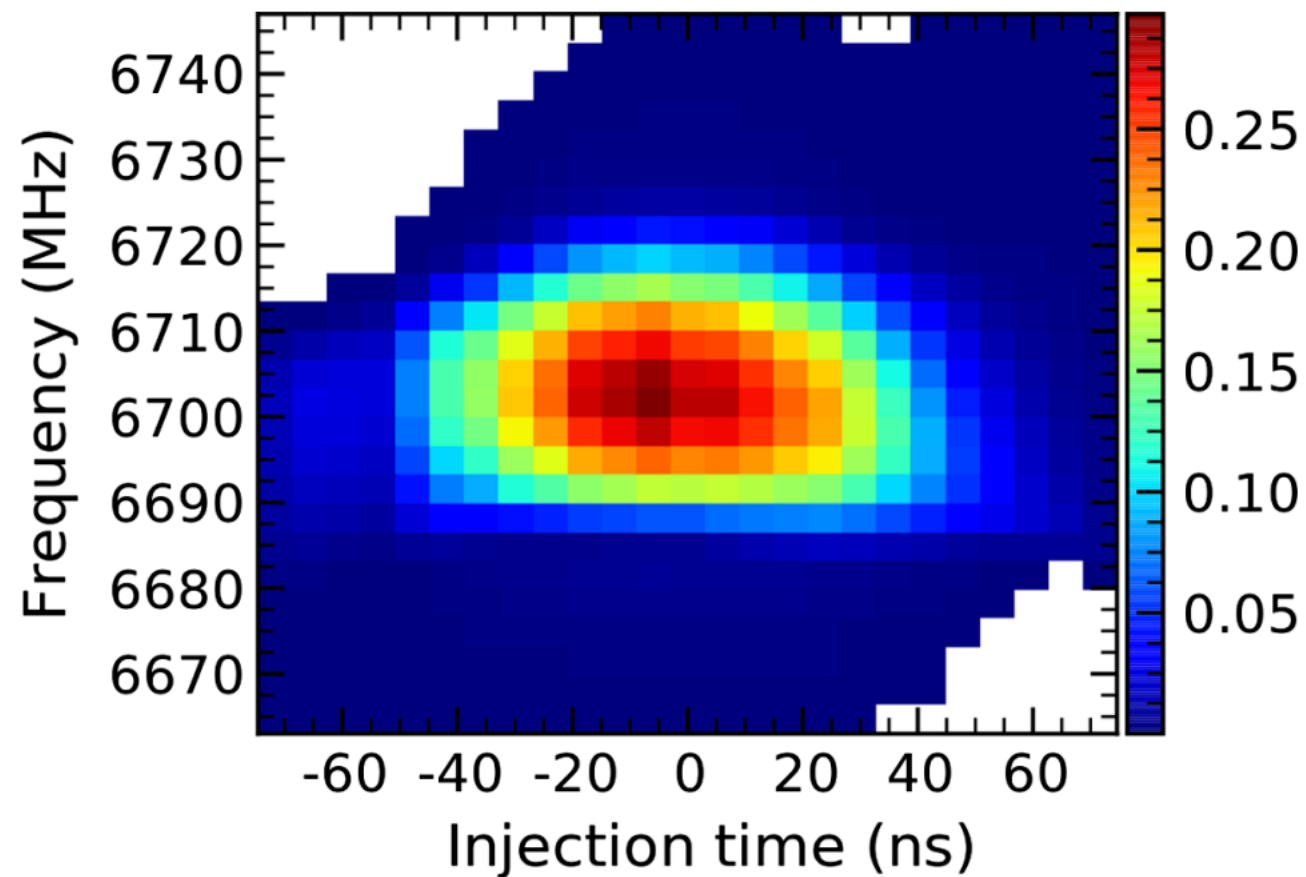
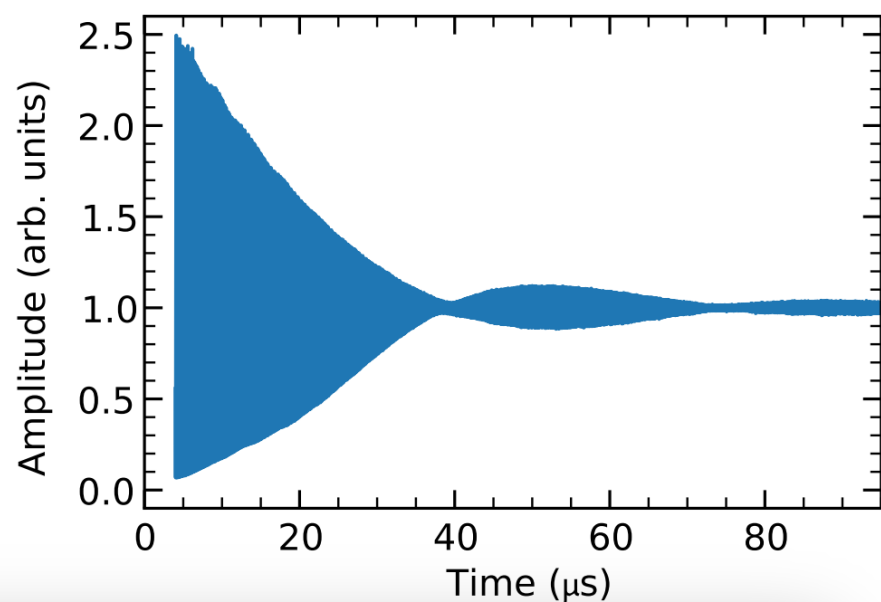
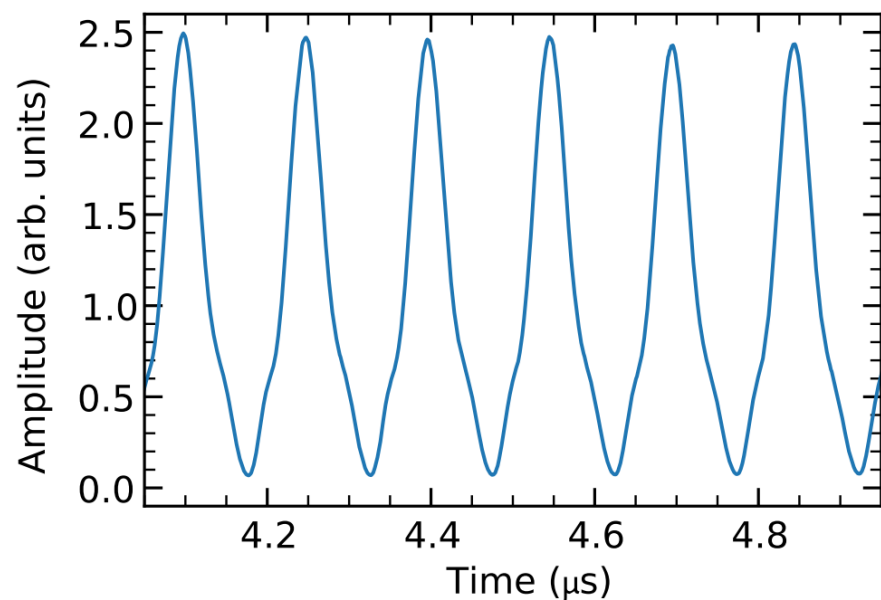
$$x_0 = D\delta + A \cos(\omega_{\text{CBO}}t_0 + \phi) \quad x_f = D\delta - A \cos(\omega_{\text{CBO}}t_0 + \phi)$$



$$\langle \delta^2 \rangle = \frac{1}{2D_x^2} \left[ \langle x_0^2 \rangle + \langle x_f^2 \rangle - \langle A^2 \cos(2\omega_{\text{CBO}}t_0 + 2\phi) \rangle - \langle A^2 \rangle \right]$$



# Electric-Field Calorimeters

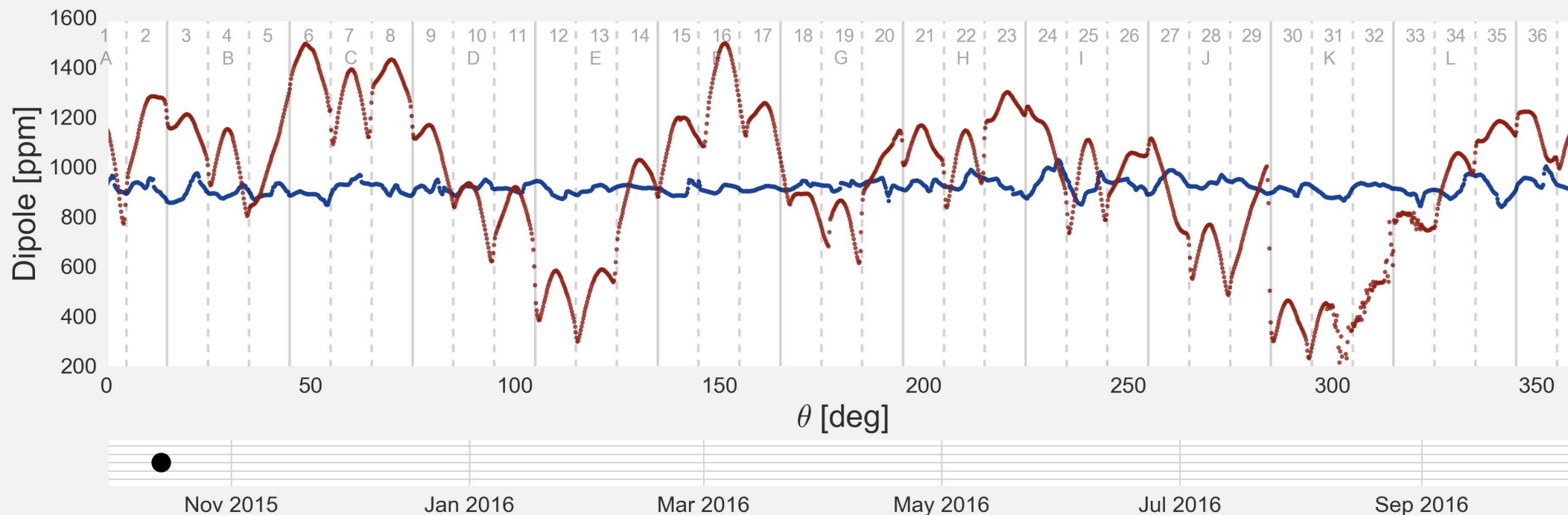
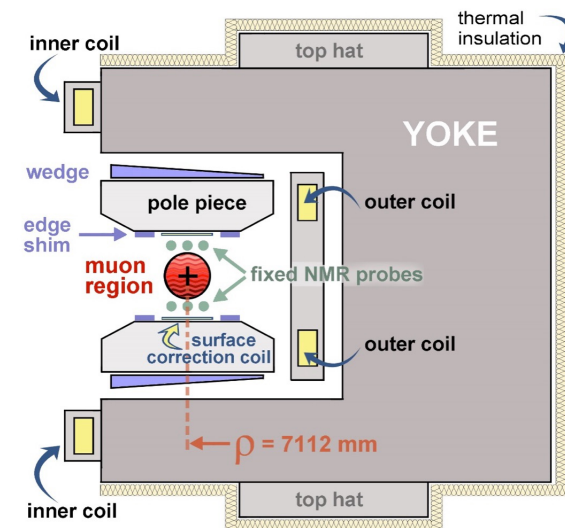




# Magnetic Field

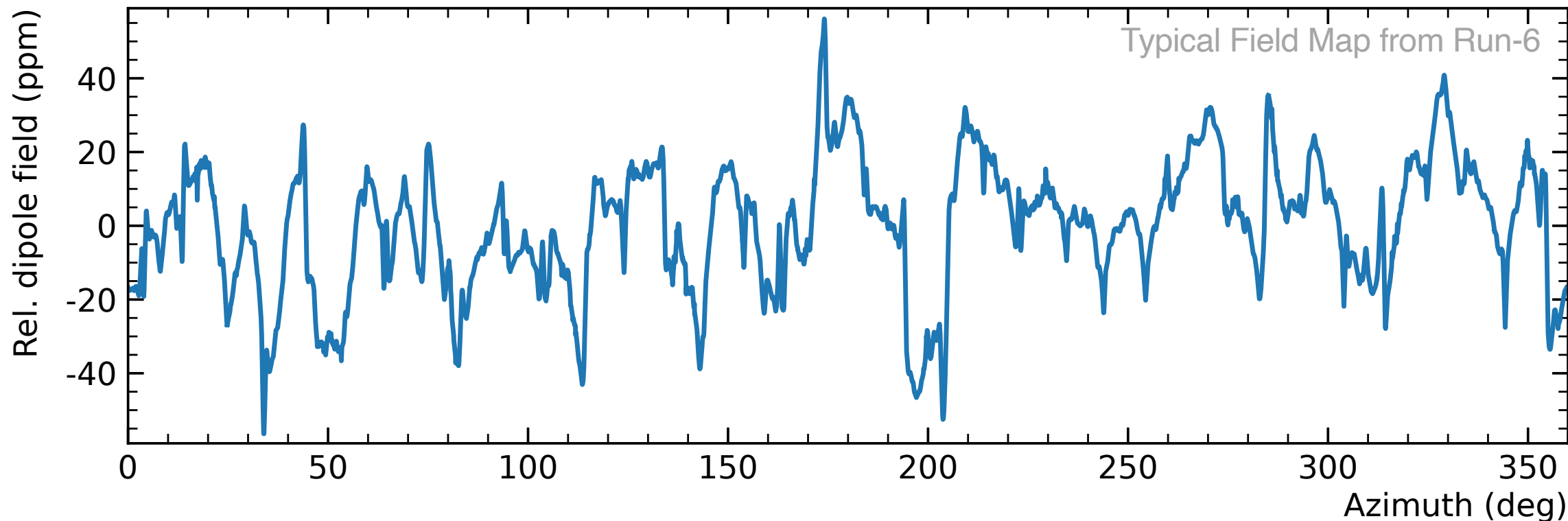
# Magnetic Field Shimming

- Many “knobs” for shimming:
  - 72 Poles: Shaping & homogeneity
  - 864 Wedges: Quadrupole asymmetry
  - 48 Iron Top Hats: Change effective  $\mu$
  - 144 Edge Shims: Quad/sextapole asymmetry
  - 8000 Surface Iron Foils: Local changes of effective  $\mu$
  - 100 Active Surface Coils: Control current to add ring-wide average field moments



# Magnetic Field Mapping & Tracking

The field between field maps (trolley runs) is tracked by the fixed NMR probes.



Take field maps every 3 to 7 days

For the Run-4/5/6 result we use 194 field (Run-1/6 total: 279)

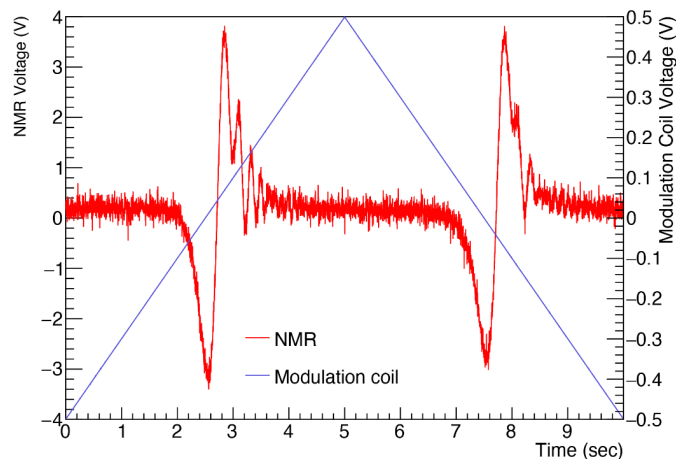
*Overall, the trolley traveled more than 100km!*



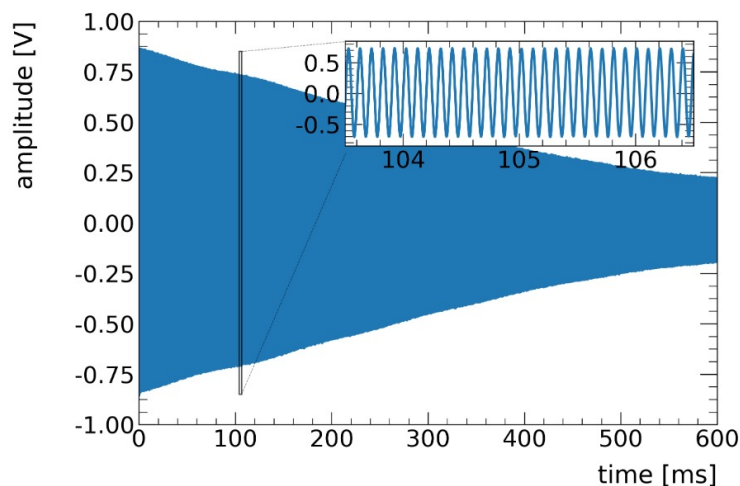
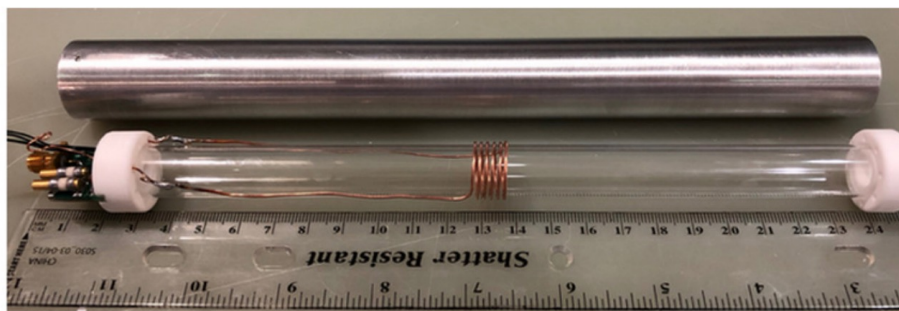


# Magnetic Field Calibration – Cross-Calibrations

## J-PARC Continuous Wave



## Water-Based Calibration Probe



## <sup>3</sup>He-based Calibration Probe



- 2019 (1.45T), 2019 (1.7T) campaigns: some inconsistencies
- 2022 (3T), 2023 (1.45T) campaigns, in good agreement

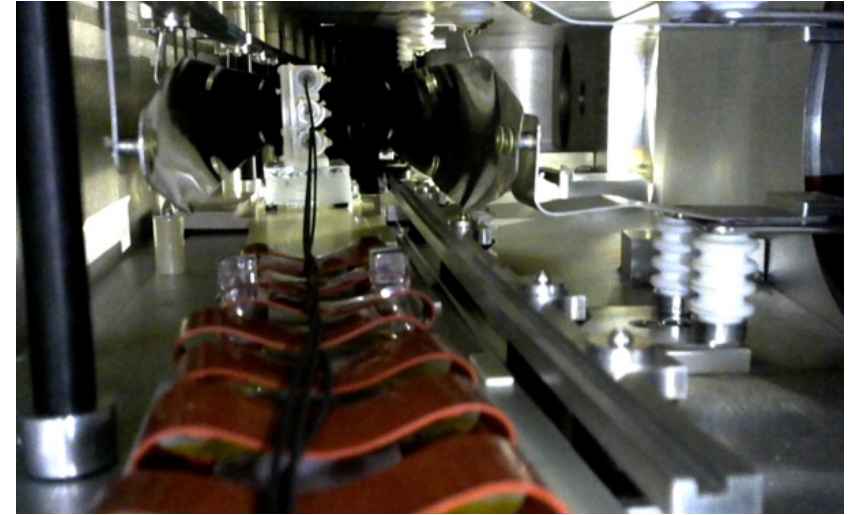
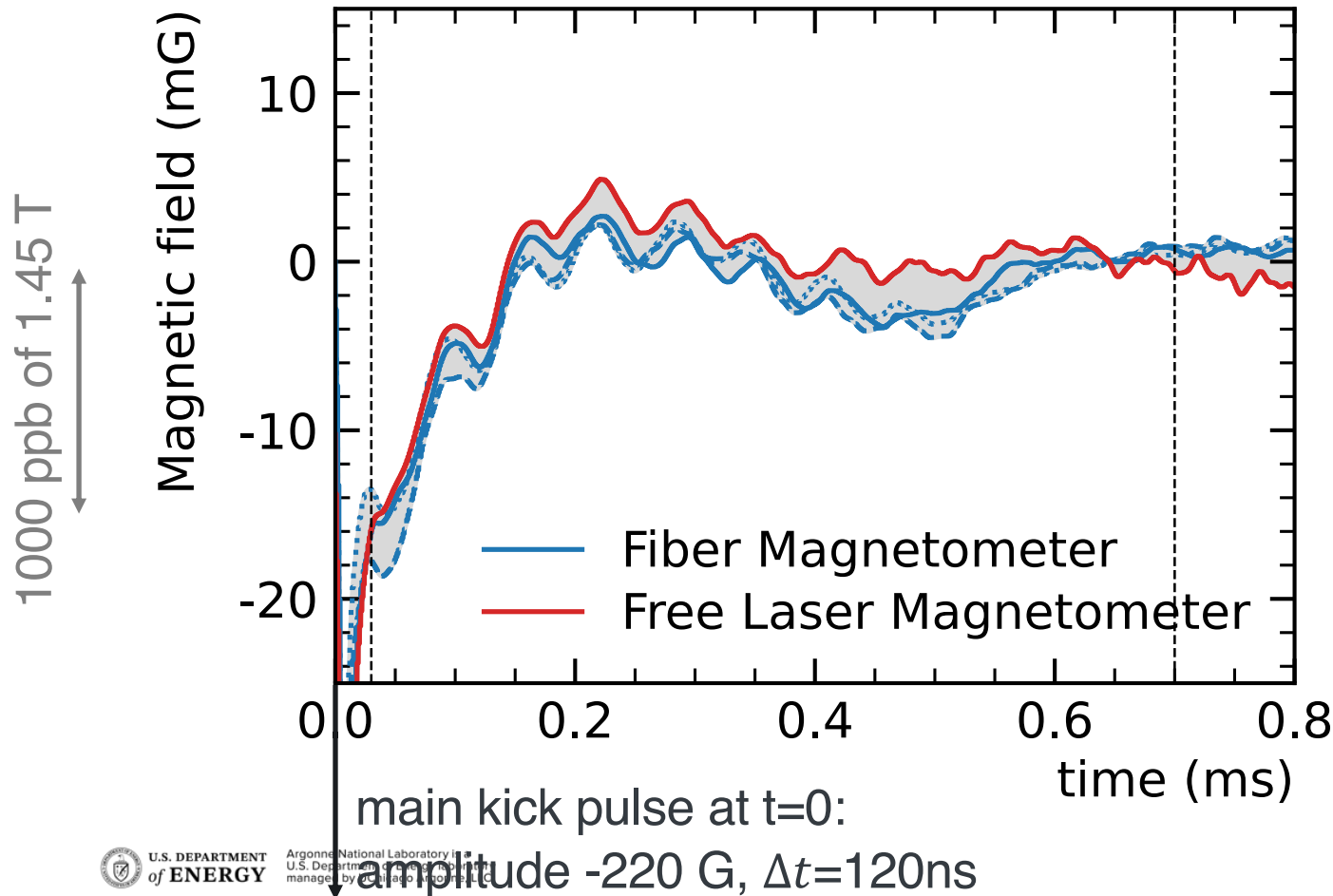
- Agreement on the 1.7  $\sigma$ -level



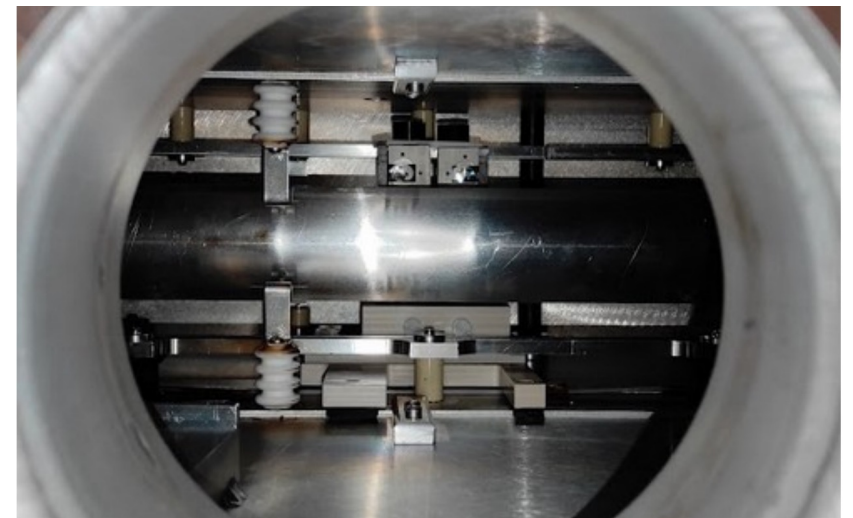
# Magnetic Transients: Kicker

Kick causes **eddy currents** → **transient** magnetic field

Measured **newly** with **two different magnetometers**  
both based on Faraday effect in TGG crystals



Fiber magnetometer



Free laser magnetometer

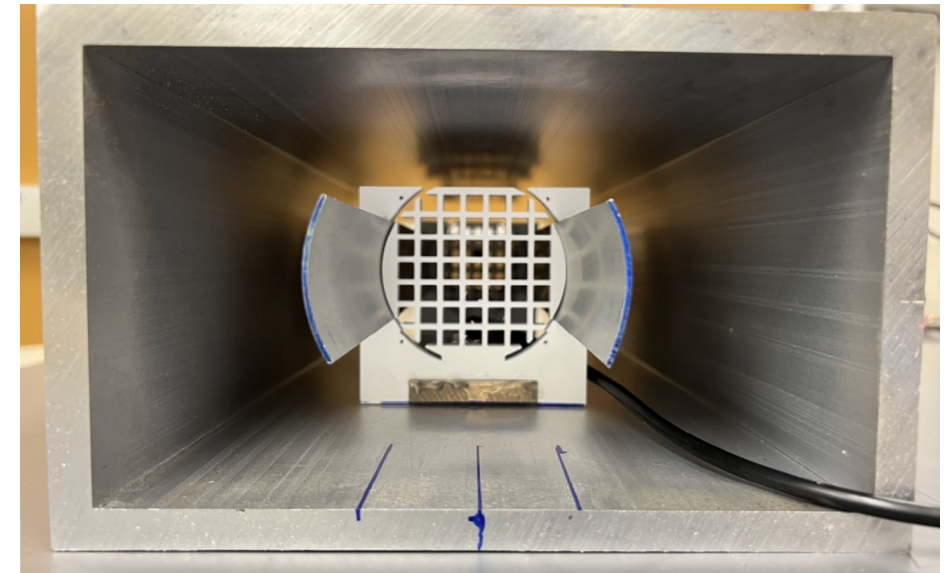
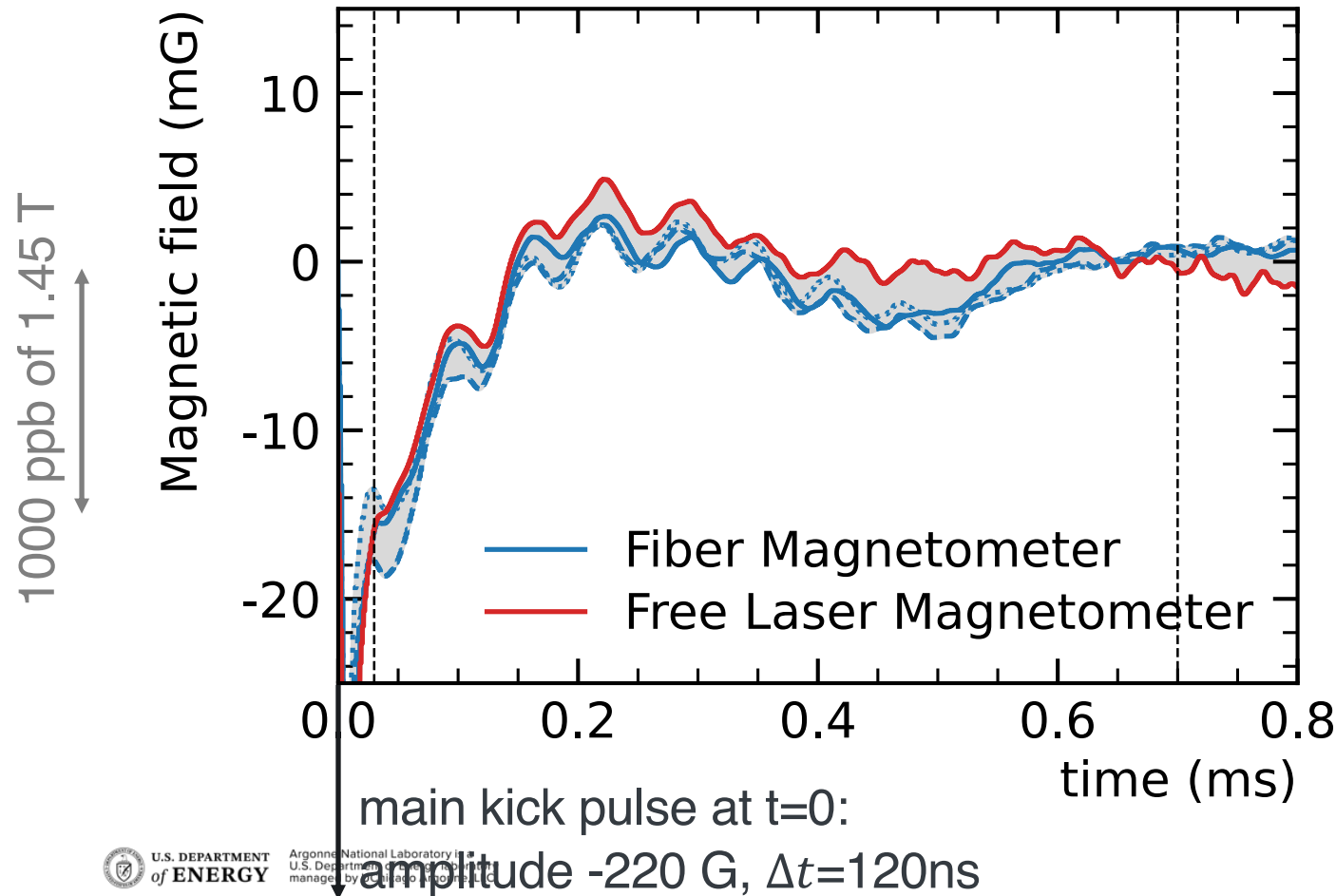


# Magnetic Transients: Kicker

Kick causes **eddy currents** → **transient** magnetic field

Measured **newly** with **two different magnetometers** both based on Faraday effect in TGG crystals

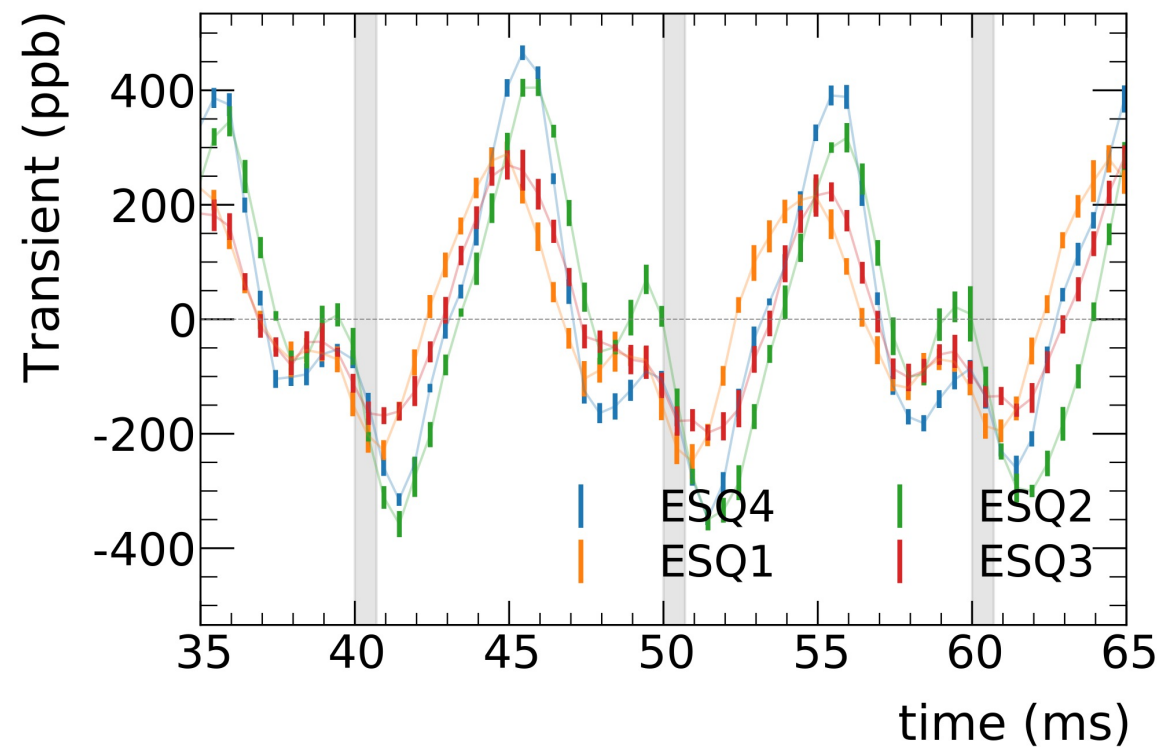
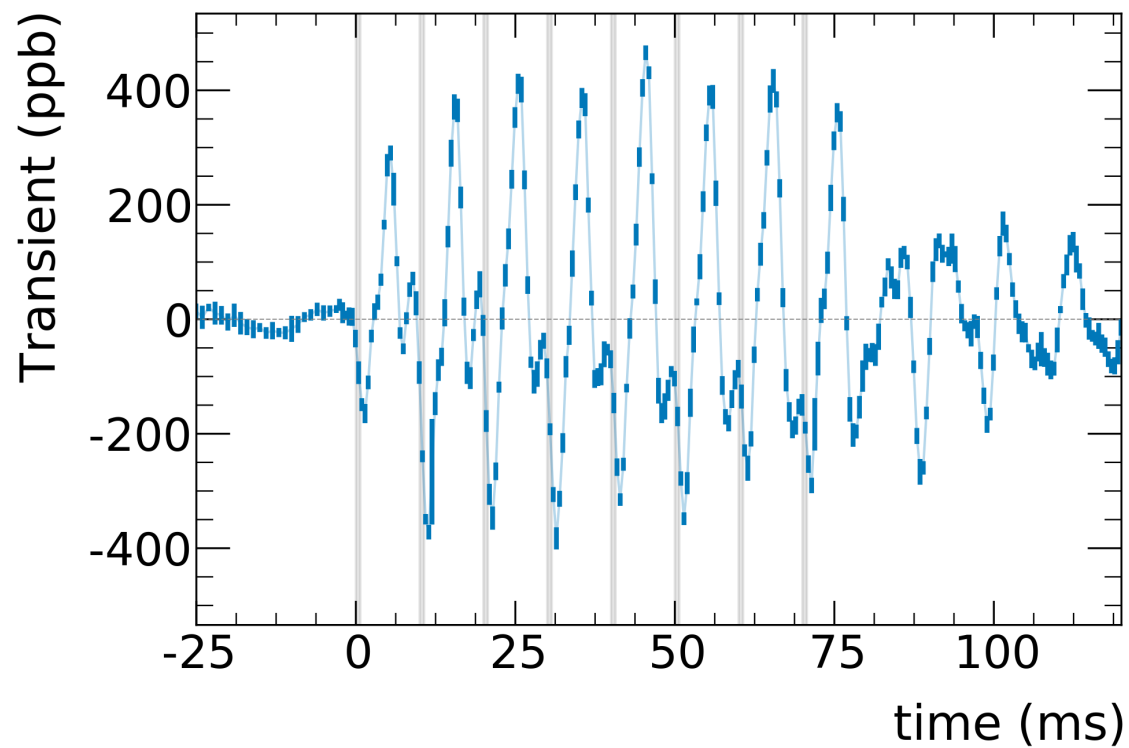
Measurement on a **Mock-Up** in the lab to refine modeling of transverse dependence



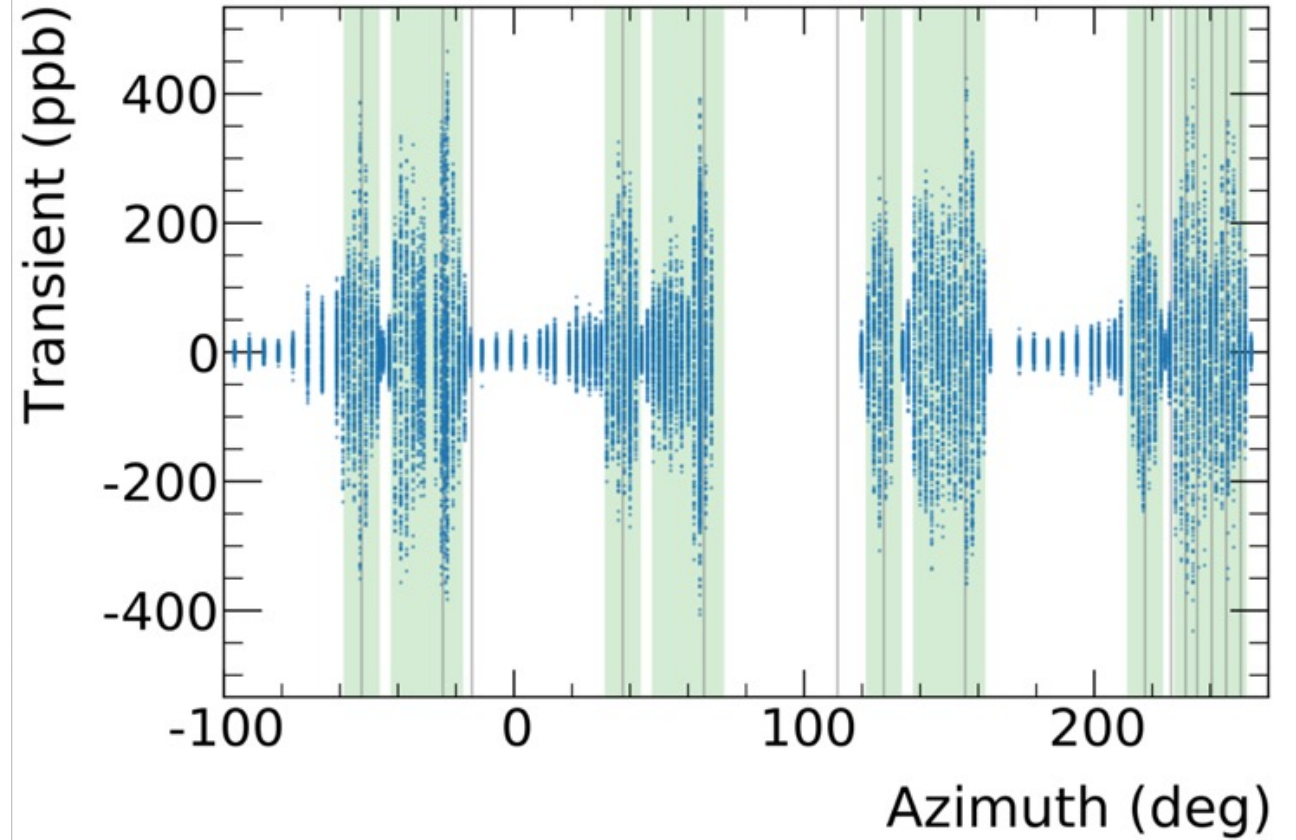
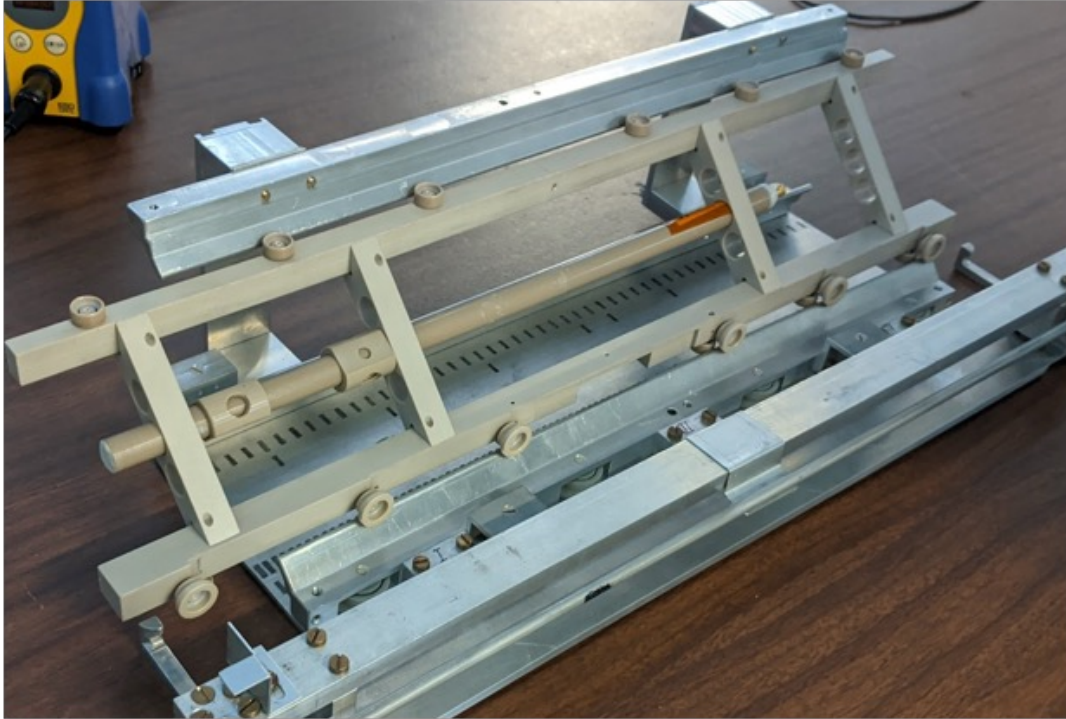
Kicker mock-up



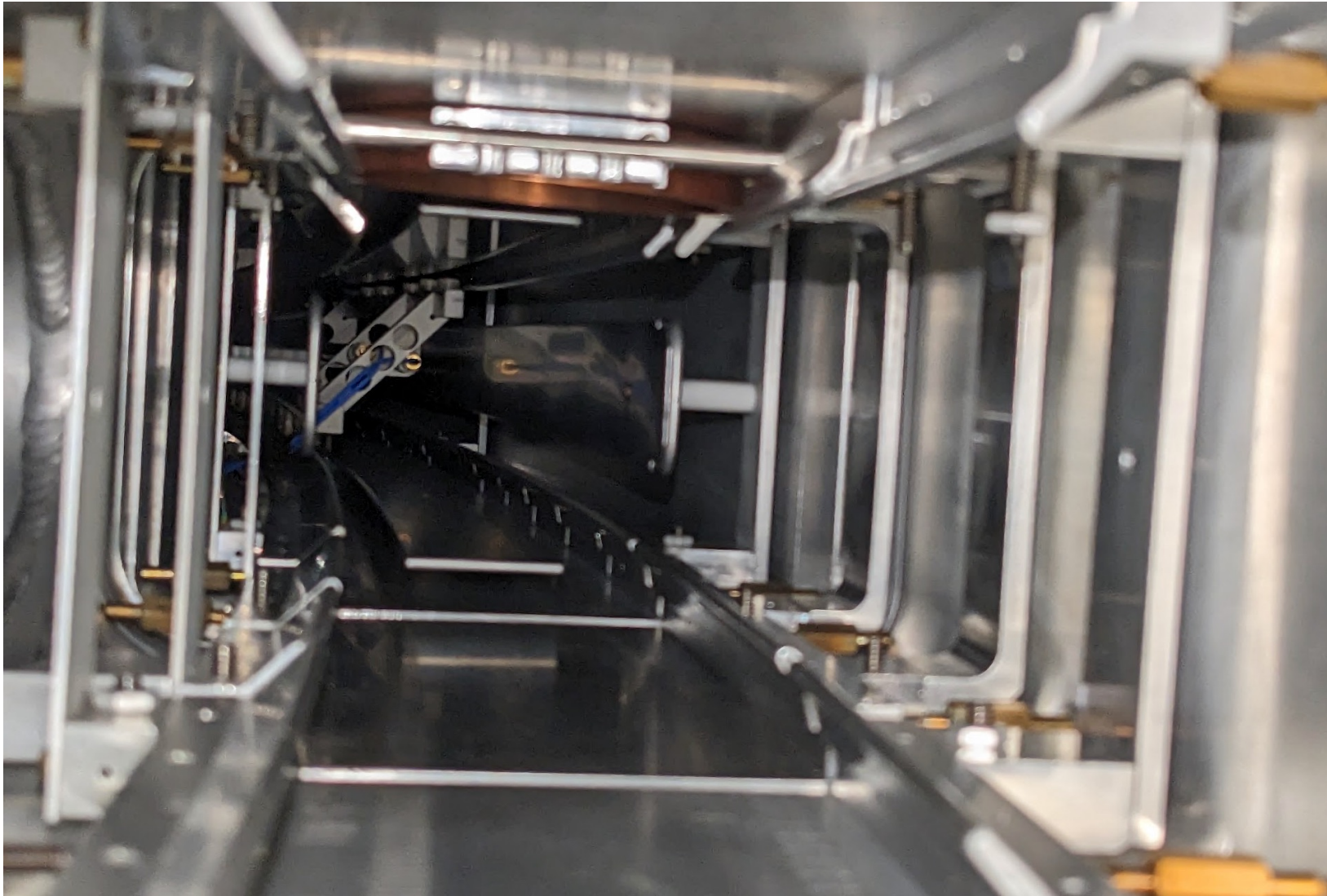
# Transient from ESQ $B_q$



# Transient from ESQ $B_q$

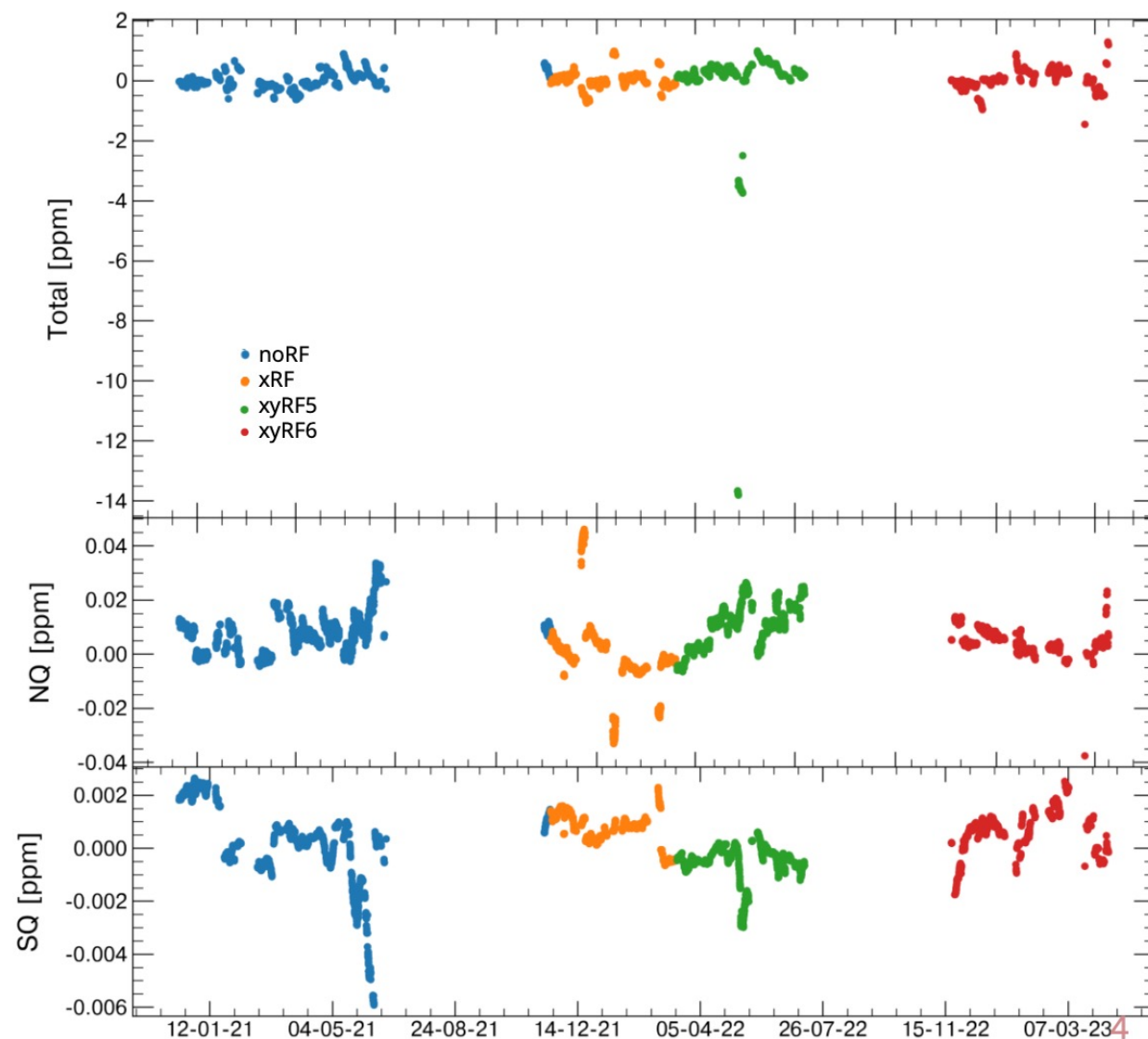


# ESQ Transient mapping

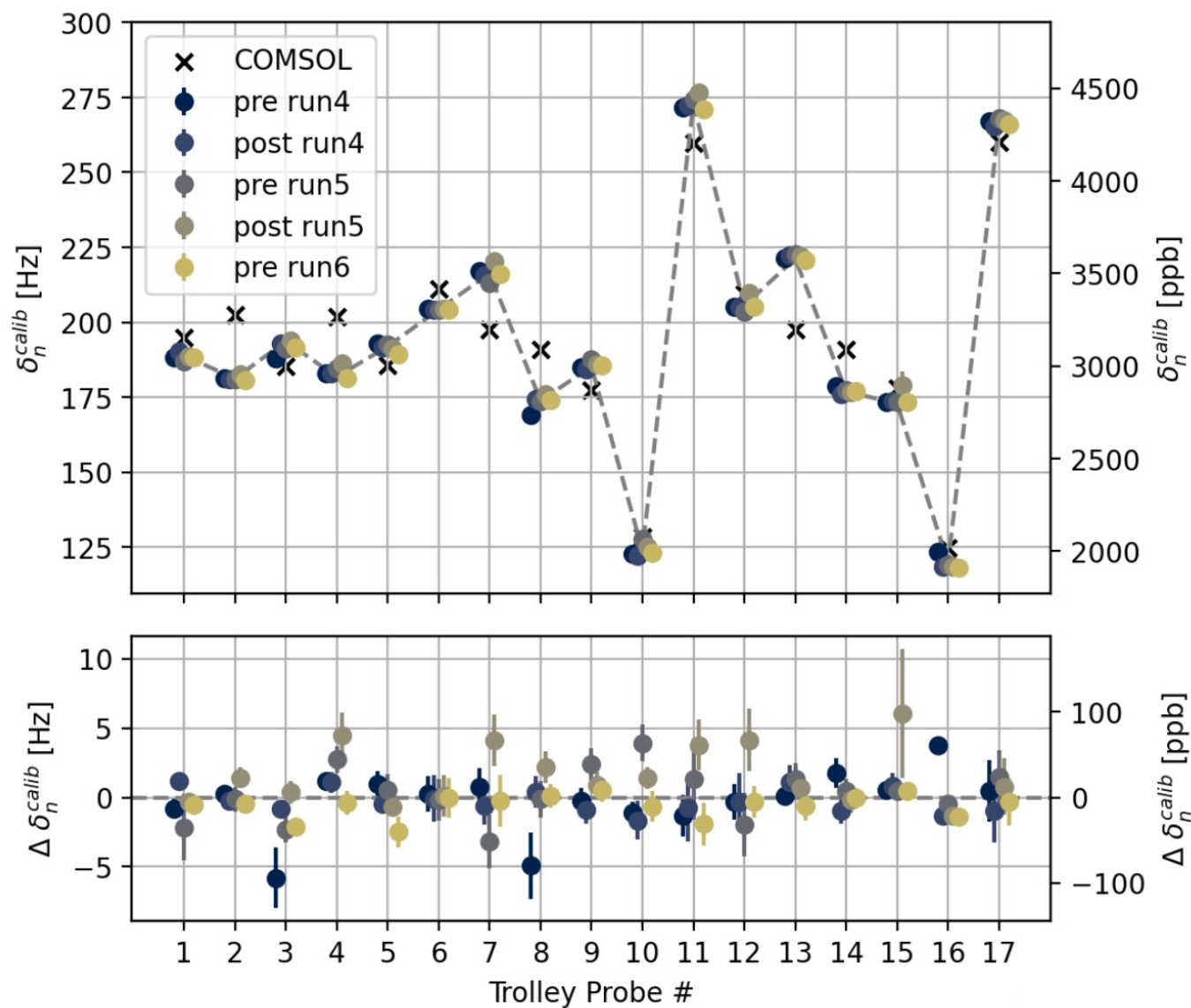




# Magnetic Field



# Trolley Calibration





$\omega_a$



U.S. DEPARTMENT  
of ENERGY

Argonne National Laboratory is a  
U.S. Department of Energy laboratory  
managed by UChicago Argonne, LLC.

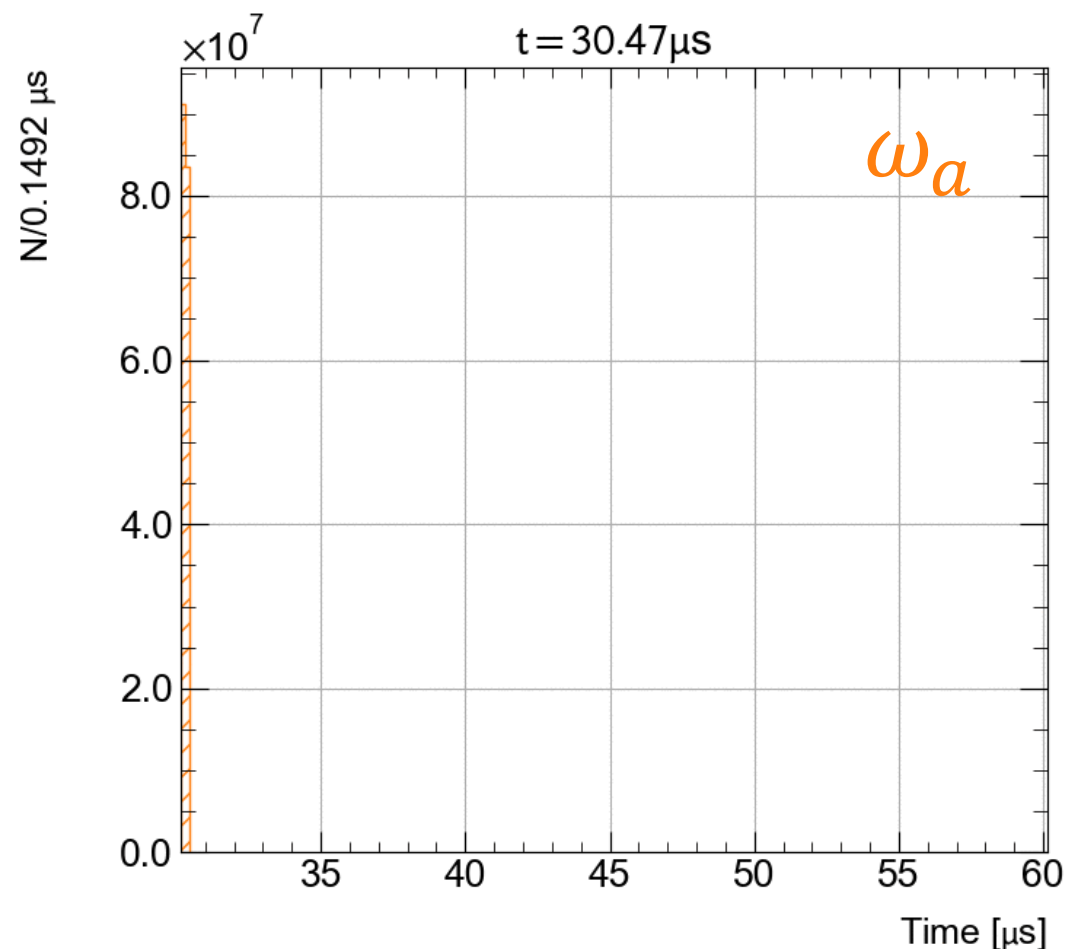
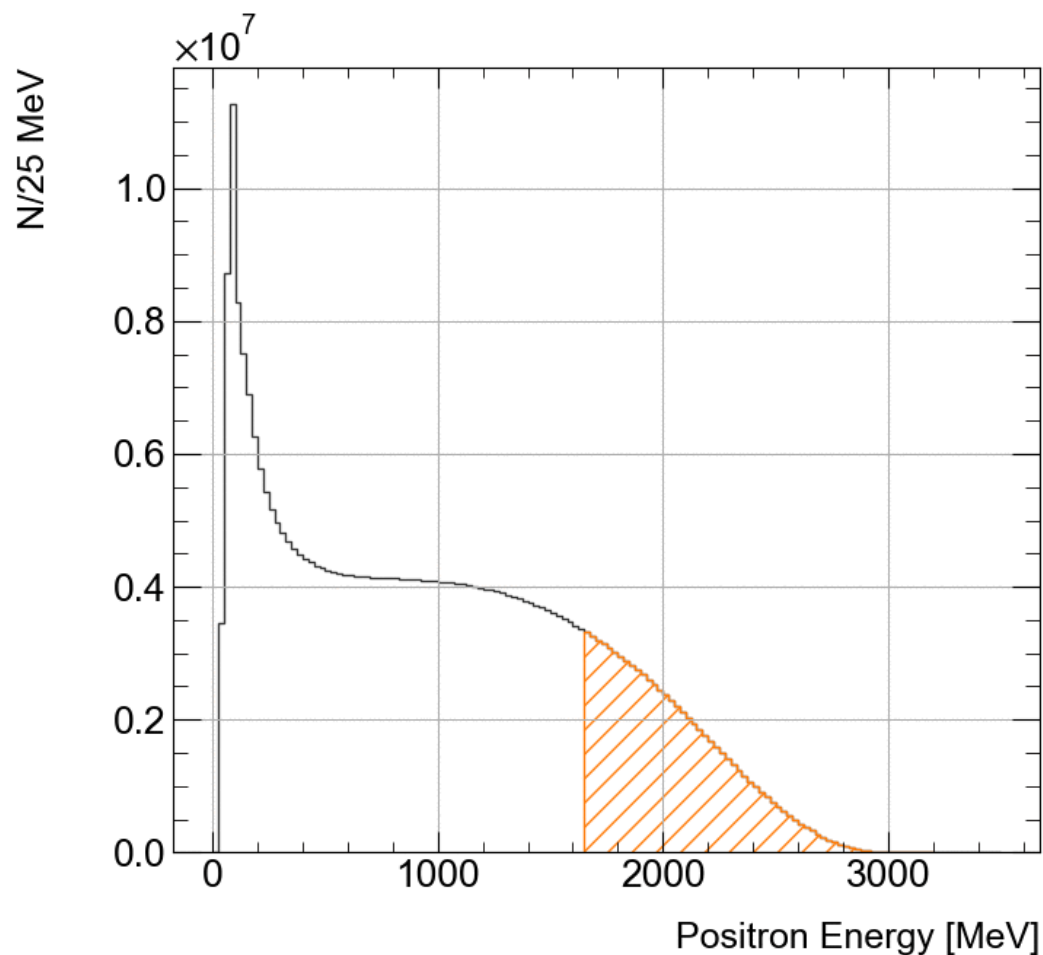
Argonne  
NATIONAL LABORATORY



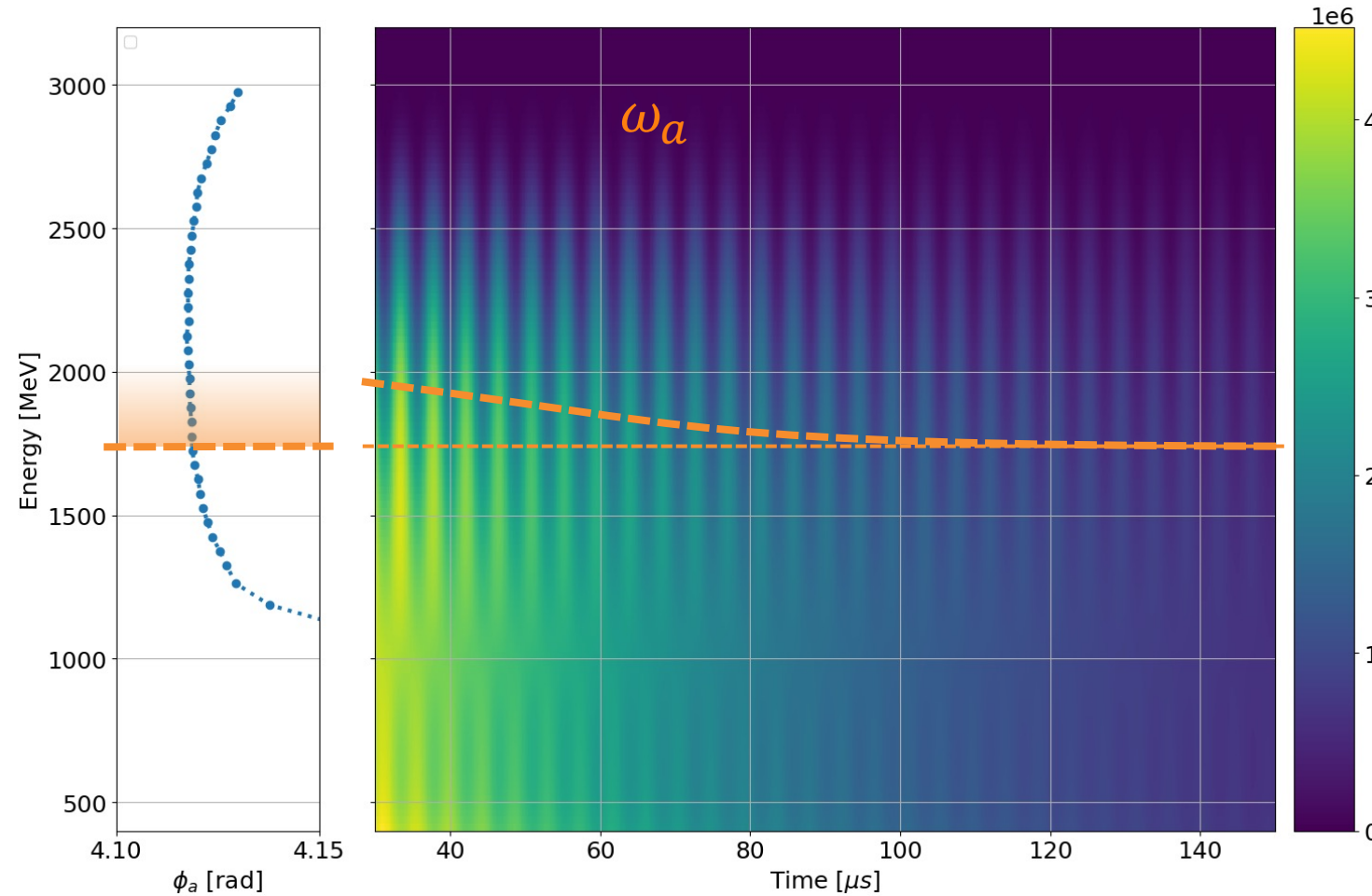
# ⚙ Measuring the Spin Precession $\omega_a$

Due to parity violation, “self-analyzing”,  
the number of **high energy  $e^+$**  oscillates as  
the  **$\mu^+$  spin** rotates

Count  **$e^+$  above threshold**  
(or weight)

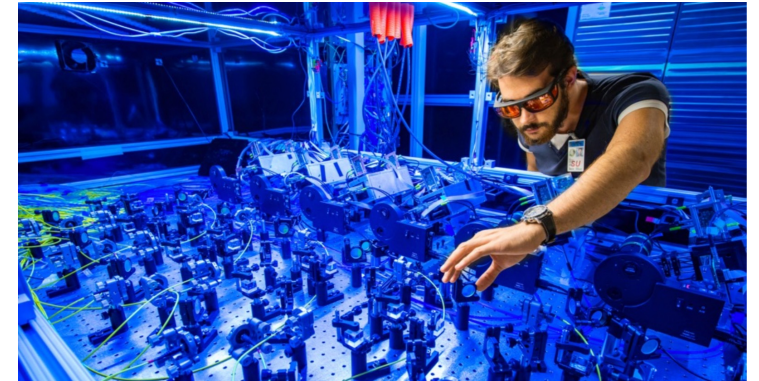


# Gain-Like Detector Effects

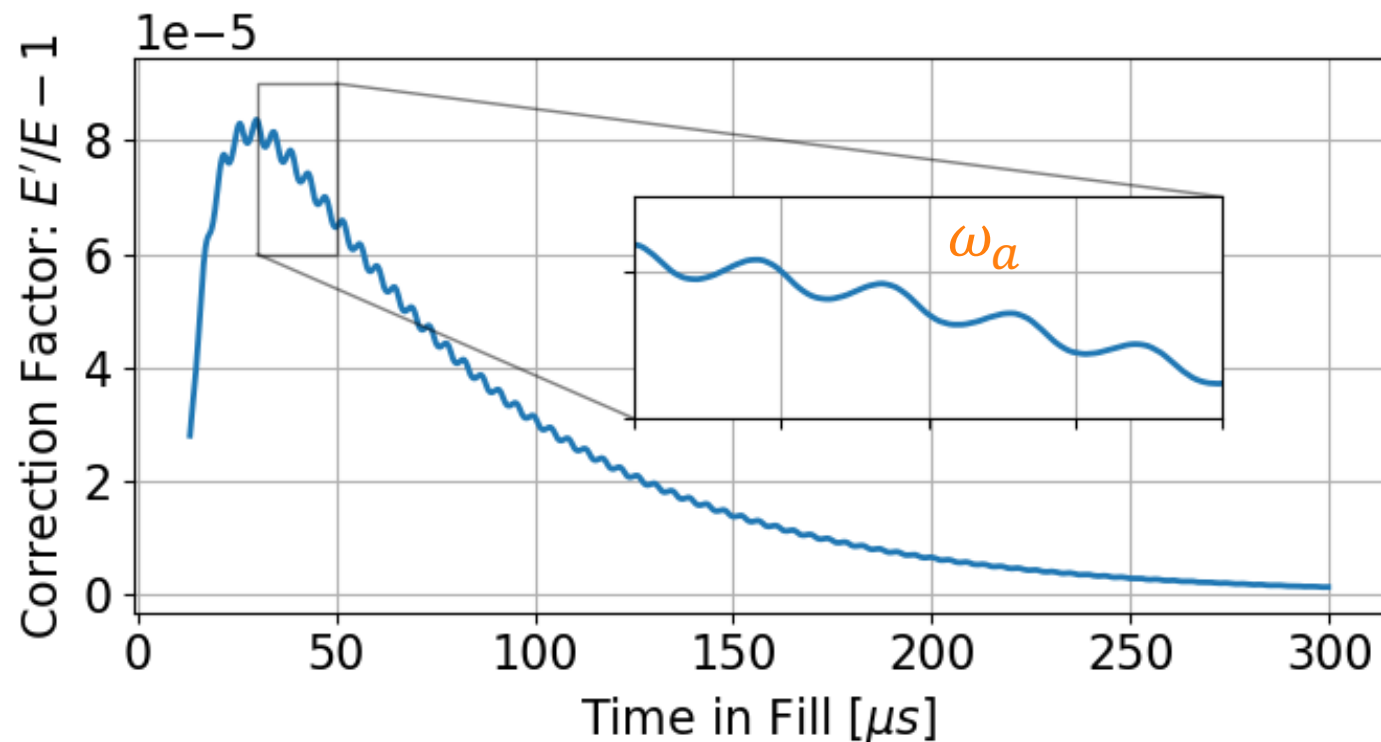


Effective **threshold** changes over time

Laser system to correct the gain on  $10^{-4}$  –level



# Gain-Like Detector Effects



\*noRF dataset

**New!** Sensitive also below  $10^{-4}$  if

- Rate & Energy dependent
- Time constant  $\sim 1/\omega_a$
- Correction shows  $\omega_a$ -behavior but **out of phase**
- Time-dependent phase-change
- Fitted  $\omega_a$  sensitive to such effects



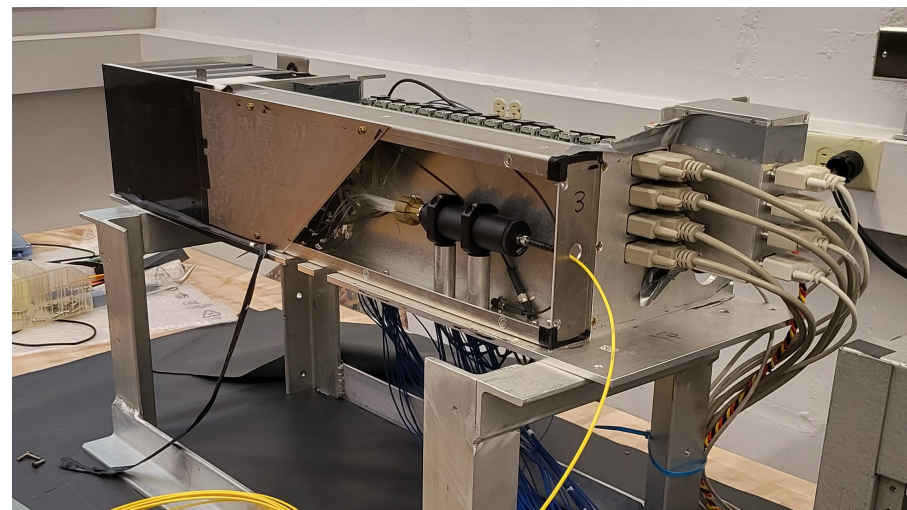
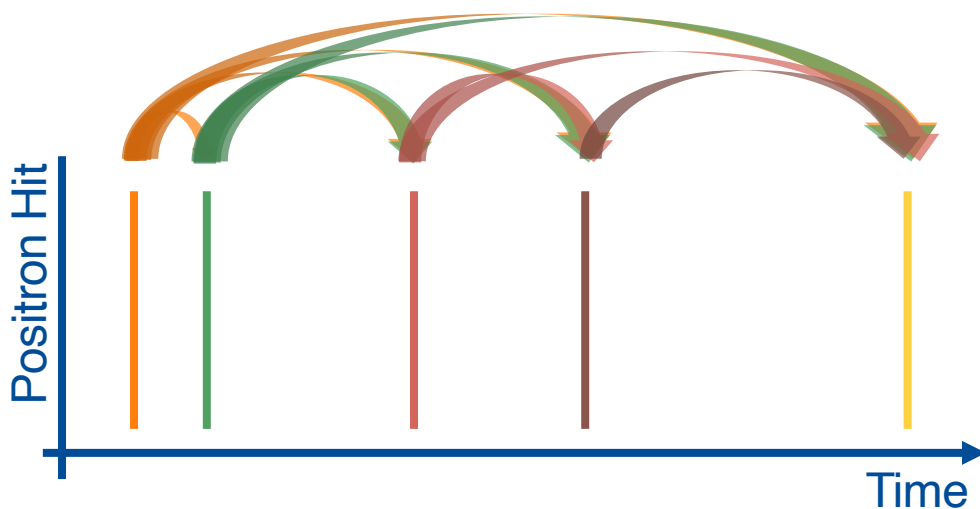


# Residual Slow Term

- known in Run-1: “early-to-late effects” 10-22 ppb uncertainty
- better understood in Run-2/3: split into reconstruction & detector part with  
“Possible sources [...] changes in gain, acceptance, or reconstruction over the duration of a fill.” 5-14 ppb uncertainty

# ⚙️ Residual Slow Term

- known in Run-1: “early-to-late effects” 10-22 ppb uncertainty
- better understood in Run-2/3: split into reconstruction & detector part with  
“Possible sources [...] changes in gain, acceptance, or reconstruction over the duration of a fill.” ~~5-14 ppb uncertainty~~  
**New! 36 pbb uncertainty**
- **Run-4/5/6: New! Identified physical explanation**
  - Detector effect due to preceding positron hits (rate dependent):  
20-40 ppb effect, ~25ppb uncertainty

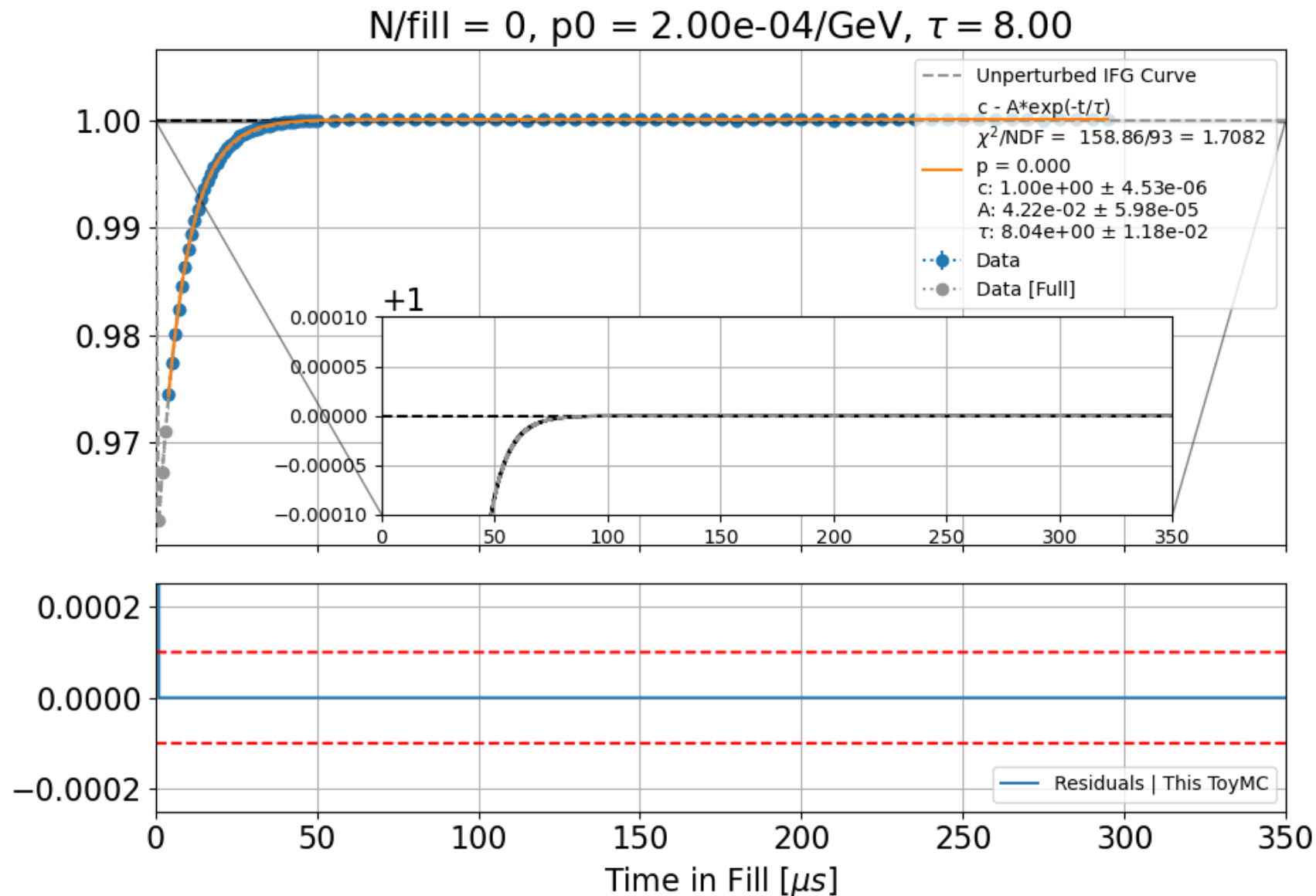


Calorimeter in lab for dedicated measurements

\* electronics board dependent



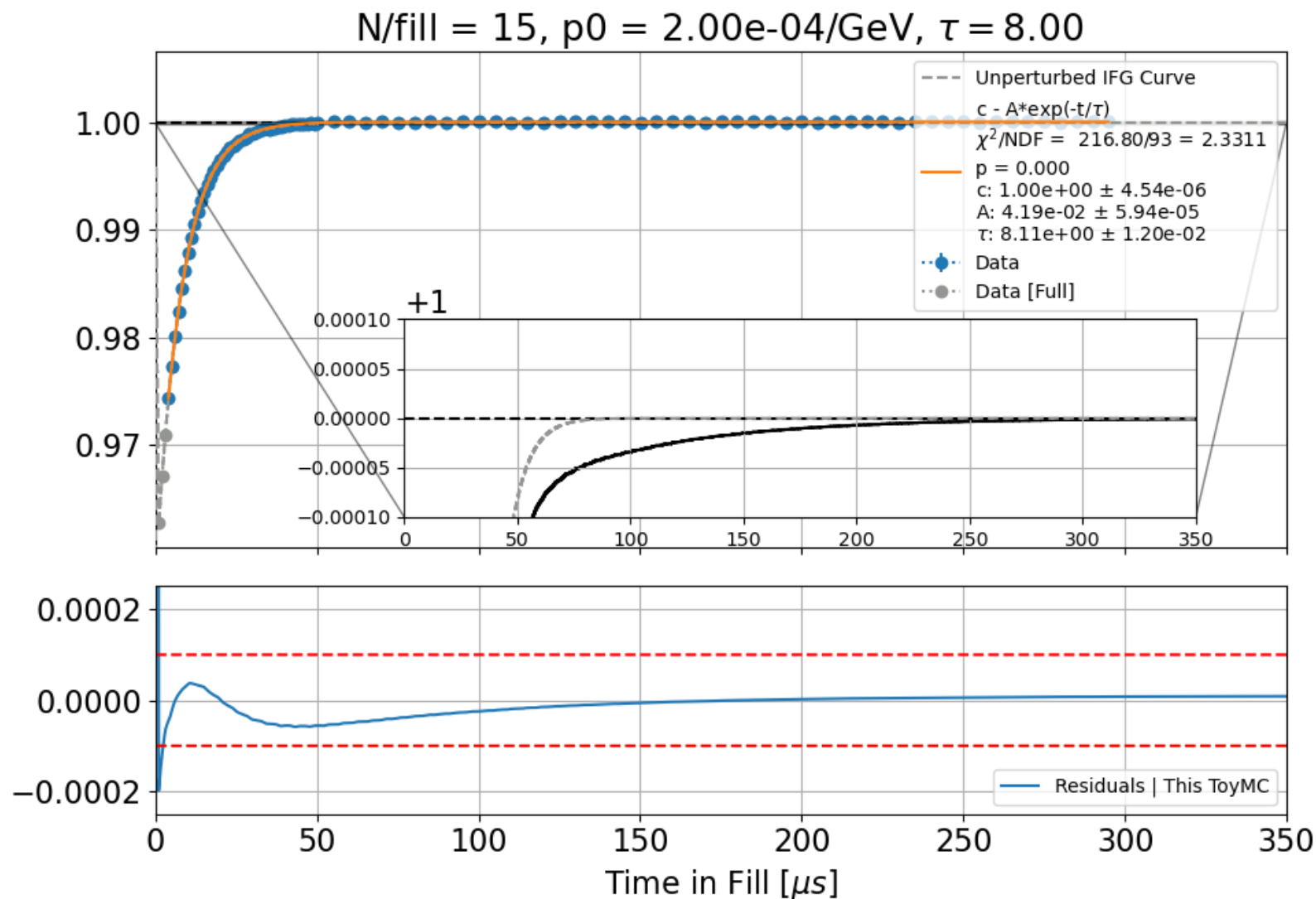
# Symptoms of Such An Effect I Toy MC Example





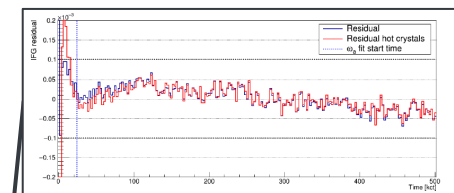
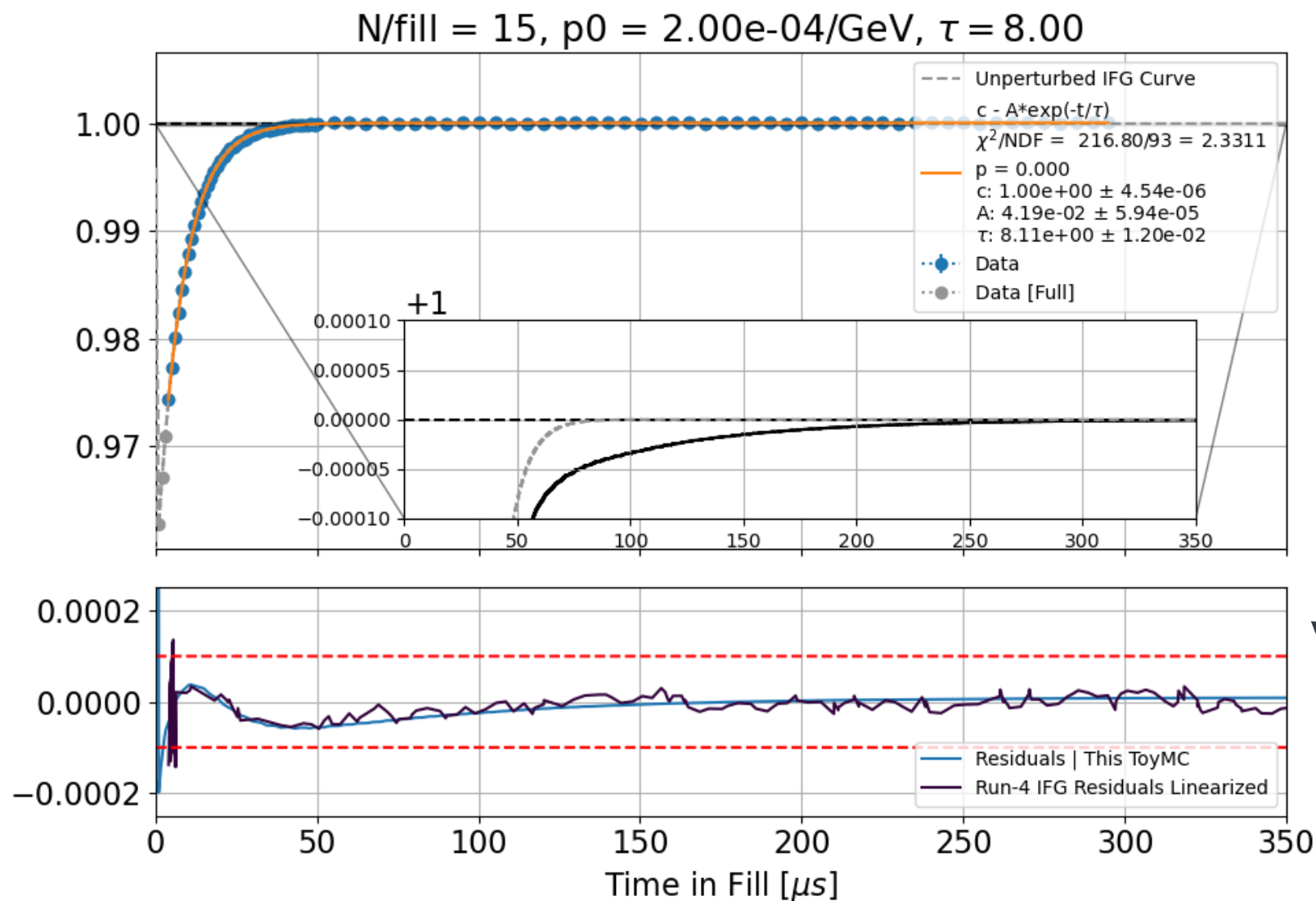


# Symptoms of Such An Effect I Toy MC Example





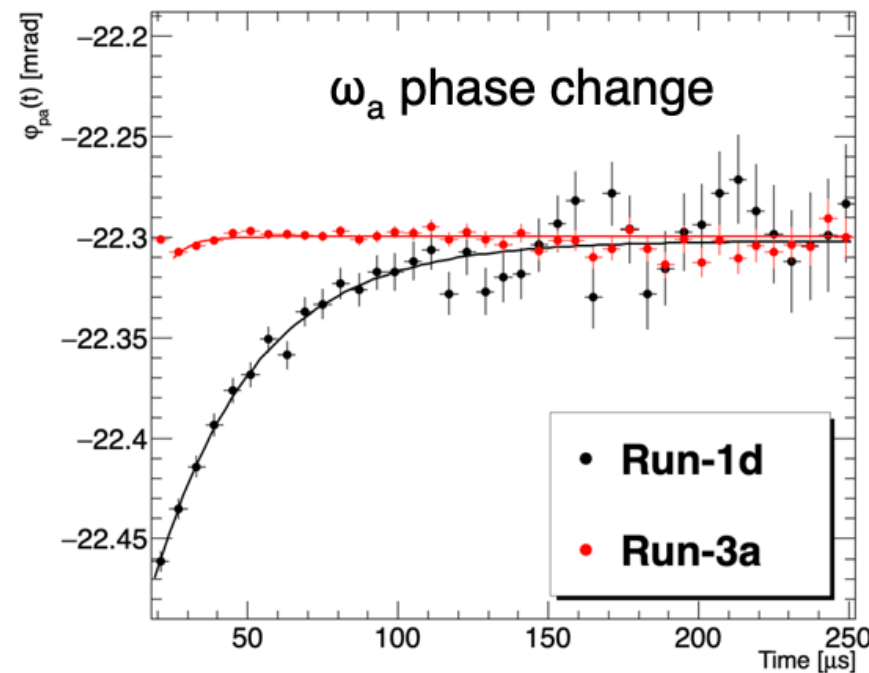
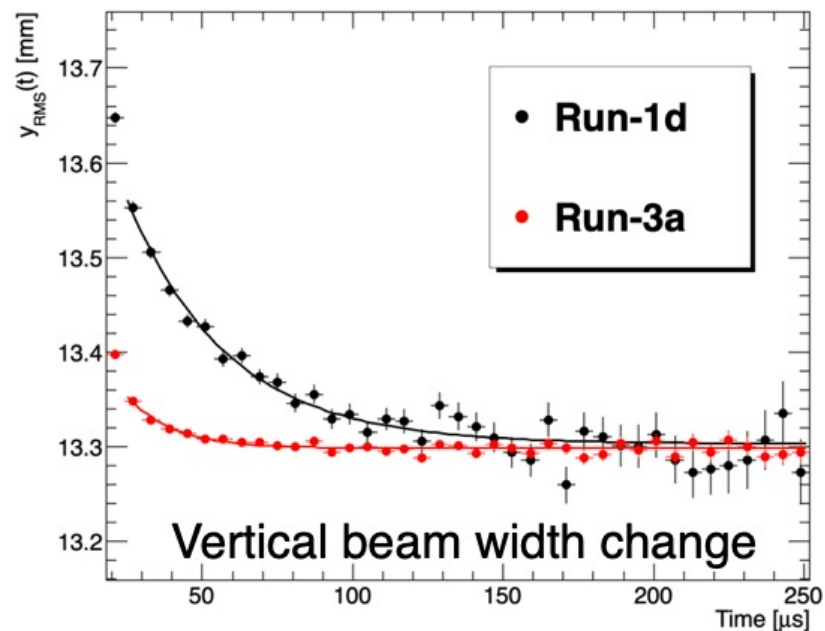
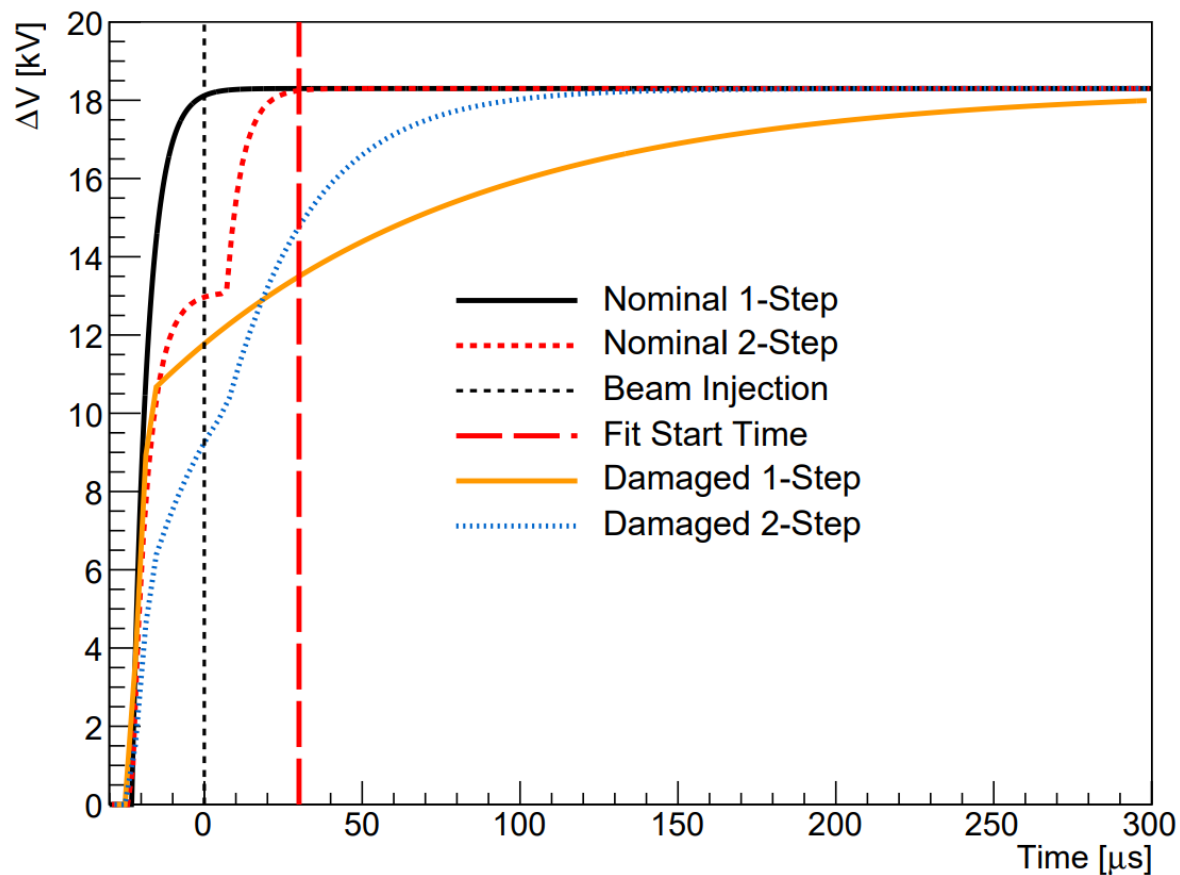
# Symptoms of Such An Effect I Toy MC Example



The shape induced by the ITDP effect matches the real IFG residuals



# Damaged Resistors





# Measuring the Spin Precession

Simplest fit model captures **exponential decay** & **g-2 oscillation**

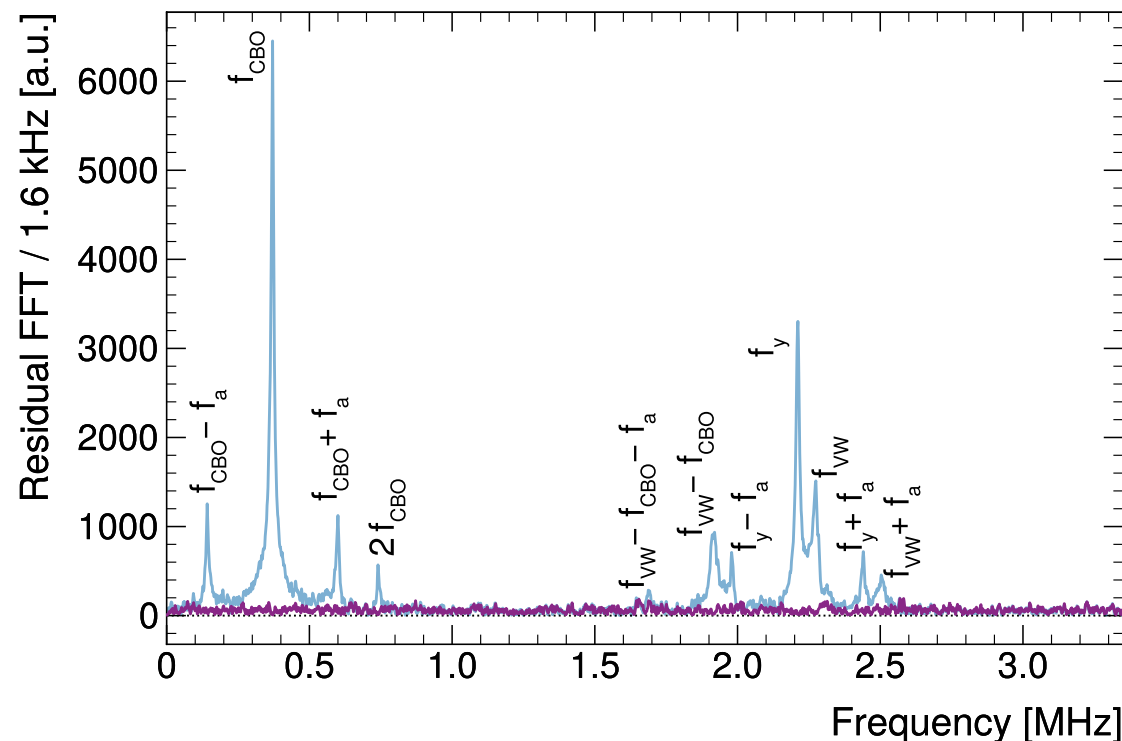
Must account for **beam oscillations**, **muons losses**, and **detector effects**

5 groups, 8 method using between  
7 and 50 parameters

## Example:

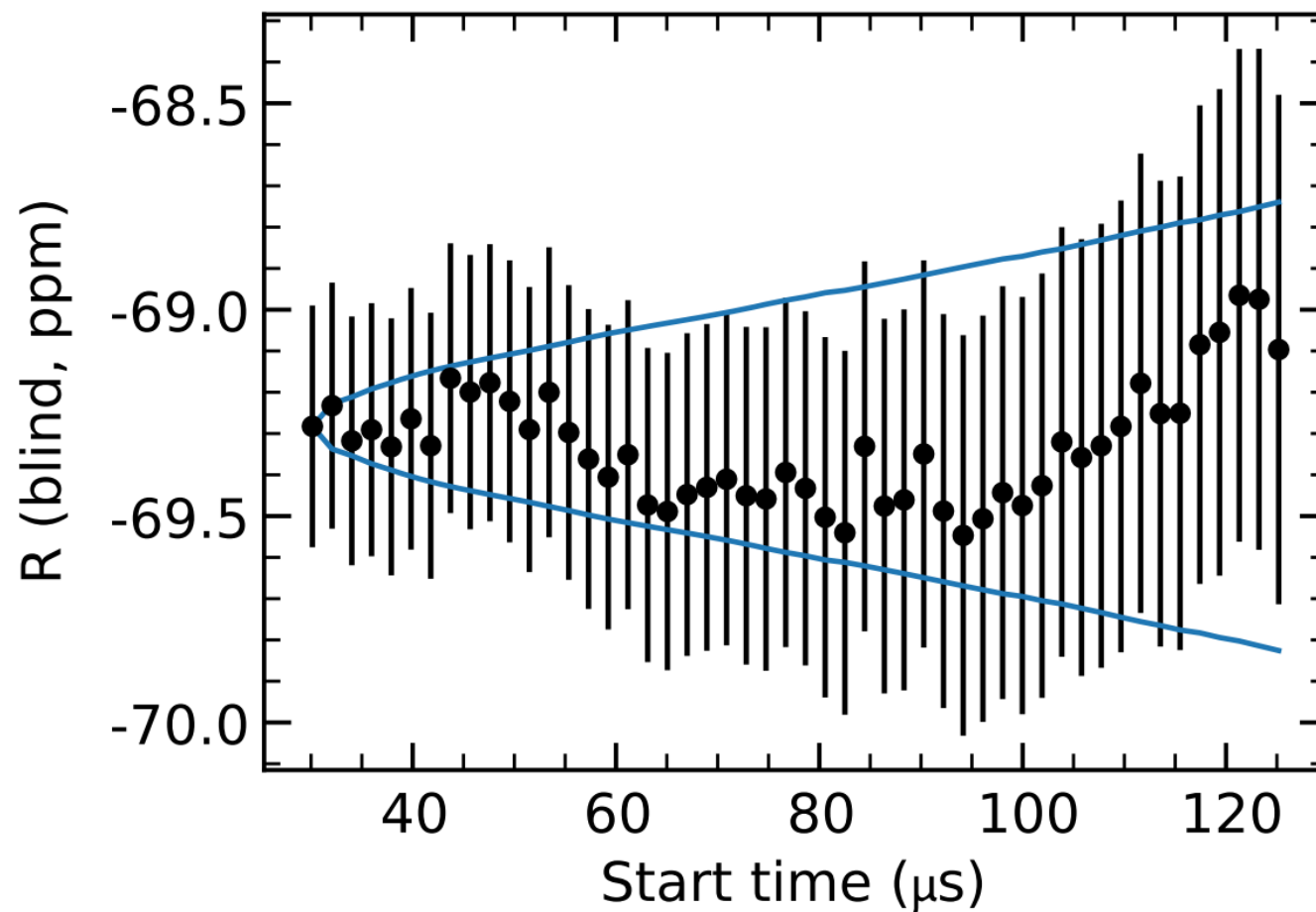
Beam dynamics modeling, such as CBO

- if not accounted for: ~800 ppb effect without the additional RF
- if not accounted for: ~80 ppb effect with the additional RF



The **large** Run-4/5/6 dataset, split into noRF, xRF, xyRF, allowed to demonstrate **consistency** between largely different conditions.

# Start Time Scan



# Numbers



# Statistics

$\frac{\omega_a}{\tilde{\omega}'_p}$	Analyzed Positrons (10 <sup>9</sup> )	Fraction (%)	Stat. Uncertainty (ppb)
Run-1	15.4	5	434
Run-2/3	70.9	23	201
Run-4/5/6	222.2	72	114
Run-1-6	308.5	...	98

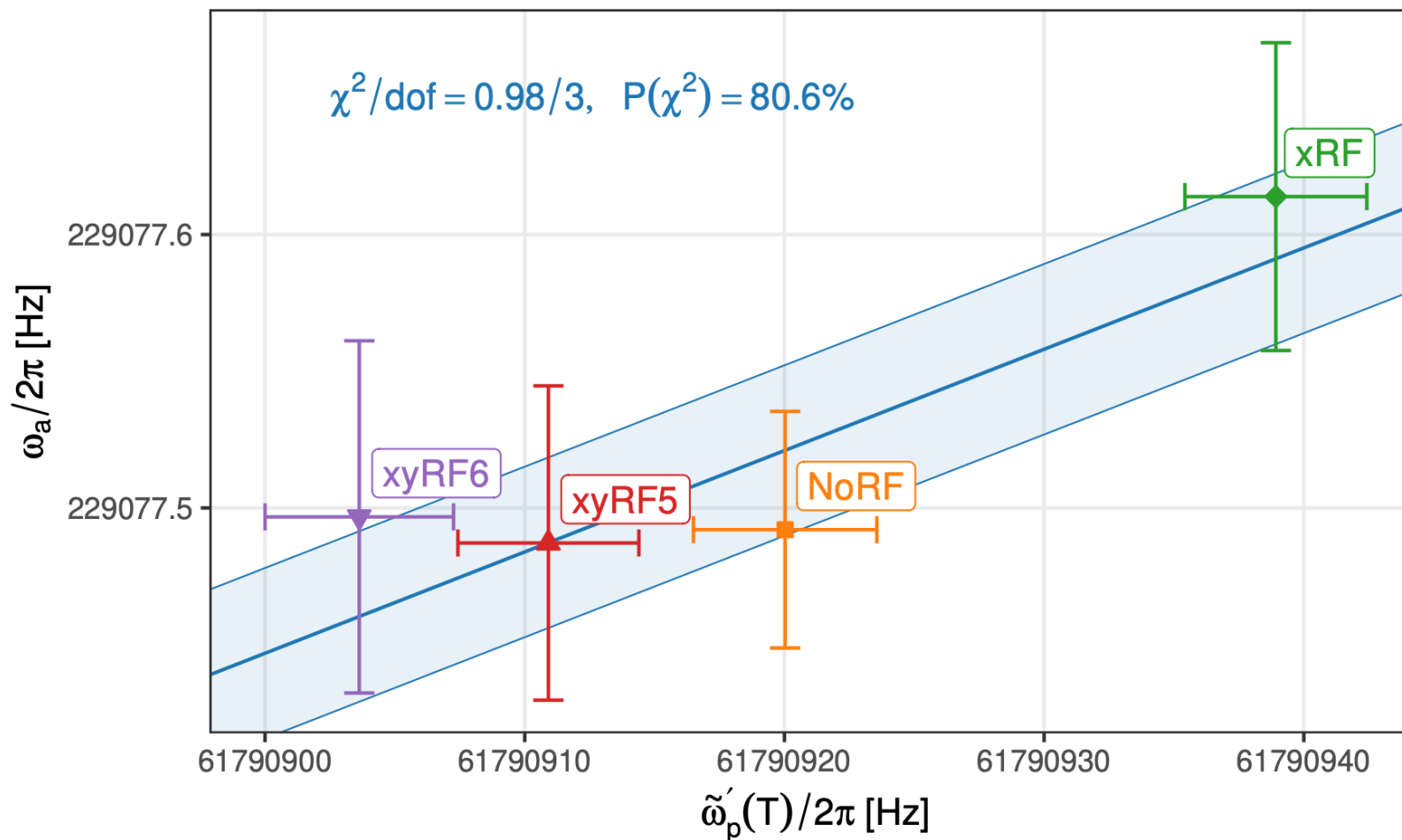
TDR goal: 100 ppb ✓

# Uncertainties

$\frac{\omega_a}{\tilde{\omega}'_p}$	Stat. Uncertainty (ppb)	Syst. Uncertainty (ppb)	Total Uncertainty (ppb)
Run-1	434	159*	462
Run-2/3	201	78*	216
Run-4/5/6	114	76	137
Run-1-6	98	78	125
	TDR goal 100 ppb ✓	TDR goal: 100 ppb ✓	TDR goal: 140 ppb ✓

# Consistency Checks

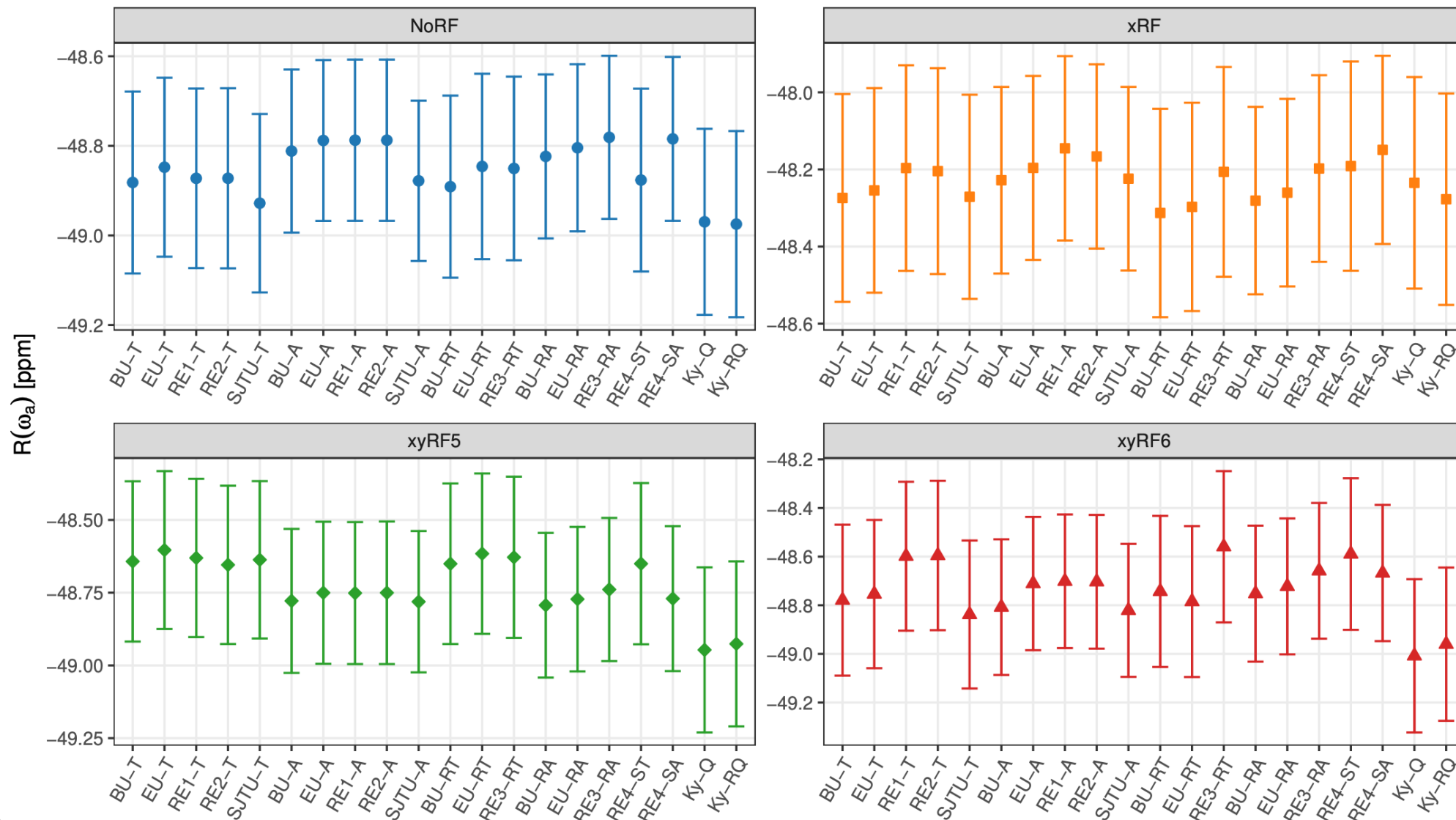
[blinded] Run 4+5+6  $R'_\mu(T) = \omega_a/\tilde{\omega}'_p(T)$  fit





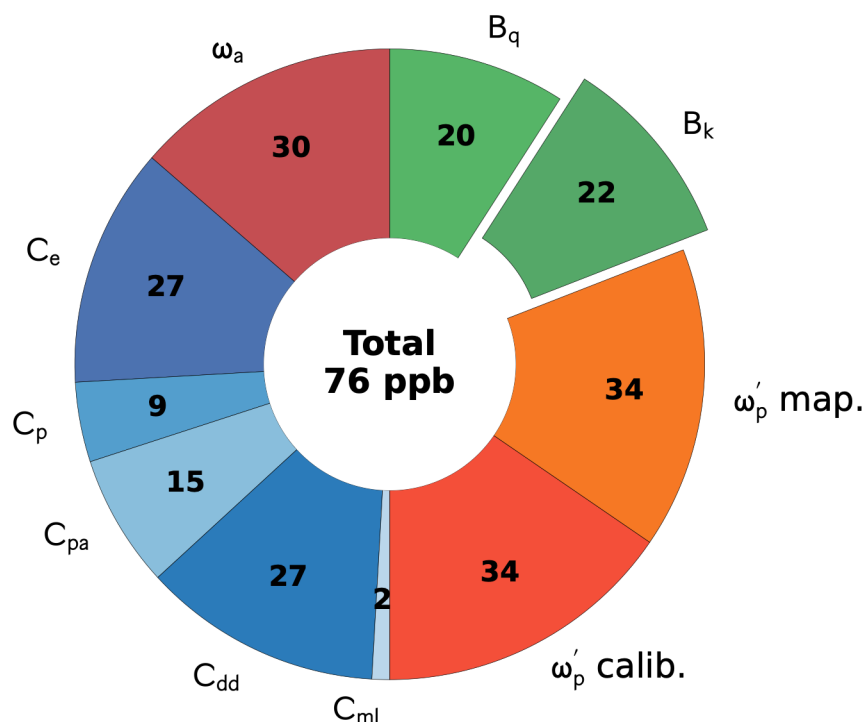


# Run-4/5/6 Analysis Overview



# Systematics

**New! Run-4/5/6**



- Run-2/3 with Run-4/5/6 knowledge
- Identified physical source for residual slow term effects
- Dedicated MiniSciFi detector and further improved methods
- Improved understanding, leading to more conservative uncertainty (sign error correction in one component)
- More conservative uncertainty motivated by additional cross-calibration
- Reduction of uncertainties due to additional measurement
- Additional measurement lead to refined spatial model

# ✚ Run-1, Run-2/3, Run-4/5/6 comparisons

Quantity	Run-1		Run-2/3		Run-4/5/6	
	Cor. (ppb)	Unc. (ppb)	Cor. (ppb)	Unc. (ppb)	Cor. (ppb)	Unc. (ppb)
$\omega_a^m$ (statistical)	...	434	...	201	...	114
$\omega_a^m$ (systematic)	+50	63	+47	35	...	30
$C_e$			451	32	347	27
$C_p$			170	10	175	9
$C_{pa}$			-27	13	-33	15
$C_{dd}$			17	22	26	27
$C_{ml}$			0	3	0	2
$f_{\text{calib}} \cdot \langle \omega'_p(\vec{r}) \times M(\vec{r}) \rangle$			...	46	...	48
$B_k$			-40	26	-37	22
$B_q$			-21	20	-21	20
Total systematic for $\mathcal{R}'_\mu$	...	158	...	78	...	77

Quantity	Run-1		Run-2/3	
	Cor. (ppb)	Add. Unc. (ppb)	Cor. (ppb)	Add. Unc. (ppb)
IDTP	+50	29	+47	24
$C_{dd}$	...	...	+32	17
$B_k$	...	...	-19	23
Total for $\mathcal{R}'_\mu$	+50	29	+98	33

corrections



# Why $a_\mu$ and not $a_e$ ?

- Coupling of virtual loops goes as  $m^2$  (dimensional analysis)
- Therefore, while  $a_\mu$  is measured  $\sim 20\times$  less precisely than the  $a_e$ , it has better sensitivity to heavy physics scales:

$$\left(\frac{m_\mu}{m_e}\right)^2 \simeq 43,000$$

- E.g. lowest-order hadronic contribution to  $a_e$  is  
 $a^{\text{had,LO}} = (1.875 \pm 0.017) \times 10^{-12}$  (1.5 ppb of  $a_e$ )
- By comparison, the muon's hadronic contribution is  $\sim 60$  ppm.

# BSM Analysis

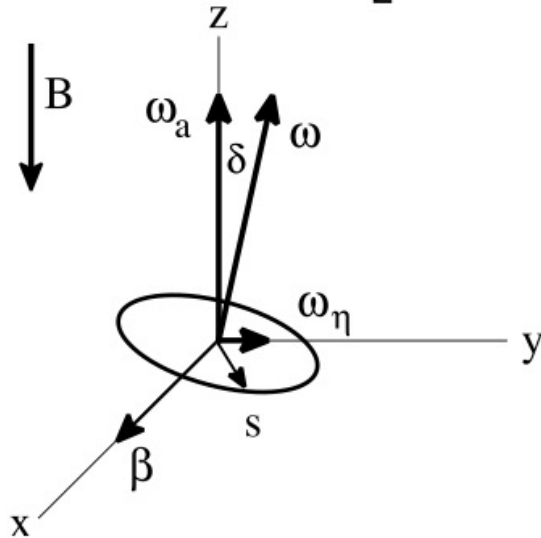


# Muon EDM

## Muon EDM

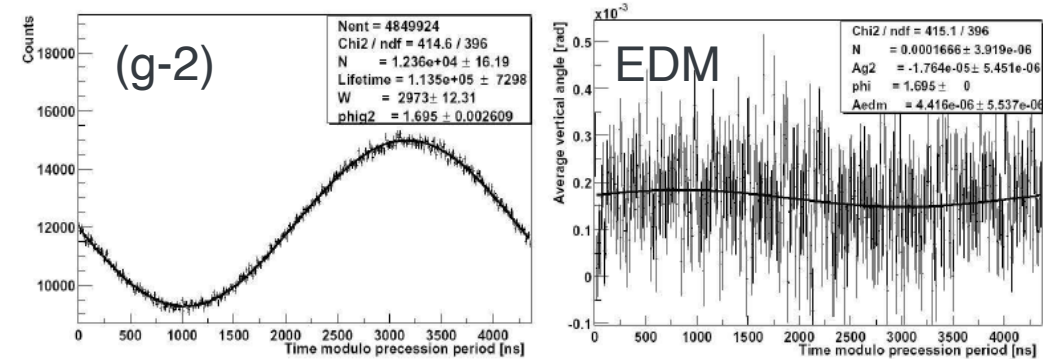
non-zero EDM ( $\eta$ ) modifies the spin equation

$$\vec{\omega}_{a\eta} = a_\mu \frac{e}{m} \vec{B} + \eta \frac{e}{2m} \left[ \frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right]$$



Search for an up/down asymmetry out of phase with  $\omega_a$

## BNL: tracker-based analysis



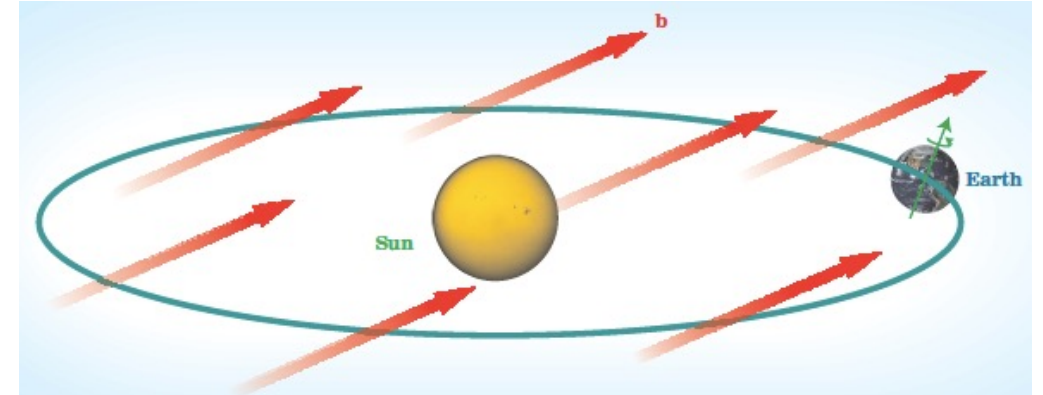




# CPT and Lorentz Violations

## Lorentz Violation – existence of a preferred direction

- Uniform background vector,  $b$
- What could it come from?  
Spontaneous Symmetry Breaking,
  - **SM**: In EWSB, scalar field gets non-zero vacuum expectation value, filling vacuum with *Lorentz Symmetric quantities*
  - **SME**: Can have Lorentz SB, where vector field gets non-zero vev, filling vacuum with *4-dimensionally oriented quantities* → preferred direction in space → LV!
  - Possibilities: string theory, loop-quantum gravity, etc.



## CPT Violation

- LV *allows* but does not *require* CPTV, because CPT Theorem no longer holds (but CPTV does require LV)

# ⚙️ Dark Matter - Physics Signature

Muon  $g - 2$  has a competitive sensitivity to the **ultralight (thus bosonic and wave-like field) muonic DM**. It is the first direct DM search with muons in a storage ring.

- **Scalar** field (Yukawa coupling)  $\phi = \phi_0 \cos(m_\phi t)$

- It induces oscillating  $m_\mu$ .

$$\mathcal{L} \supset -g\phi\bar{\mu}\mu - g'\phi^2\bar{\mu}\mu \Rightarrow m_\mu \rightarrow m_\mu + g\phi + g'\phi^2$$

- It leads  **$\omega_a$  to oscillate**:  $\omega_a \rightarrow \omega_a(1 + A_\phi \cos m_\phi t)$

- **Pseudoscalar** axion-like field  $a = a_0 \cos(m_a t)$

- EDM coupling induces oscillating EDM ( $d_\mu$ ).

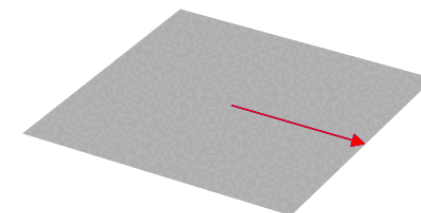
$$\mathcal{L} \supset -ig_{\text{EDM}}a\bar{\mu}\sigma^{\lambda\nu}\gamma_5\mu F_{\lambda\nu} \Rightarrow d_\mu \rightarrow d_\mu + g_{\text{EDM}}a$$

- Gradient coupling induces oscillating spin along the axis of the muon's motion.

$$\mathcal{L} \supset g_{a\mu}\partial_\lambda a\bar{\mu}\gamma^\lambda\gamma_5\mu \Rightarrow \mathcal{H} \supset g_{a\mu}\nabla a \cdot \mathbf{S}$$

- Both lead to **oscillating  $\delta\omega_a$  components perpendicular to  $\omega_a$** .

Spin precession



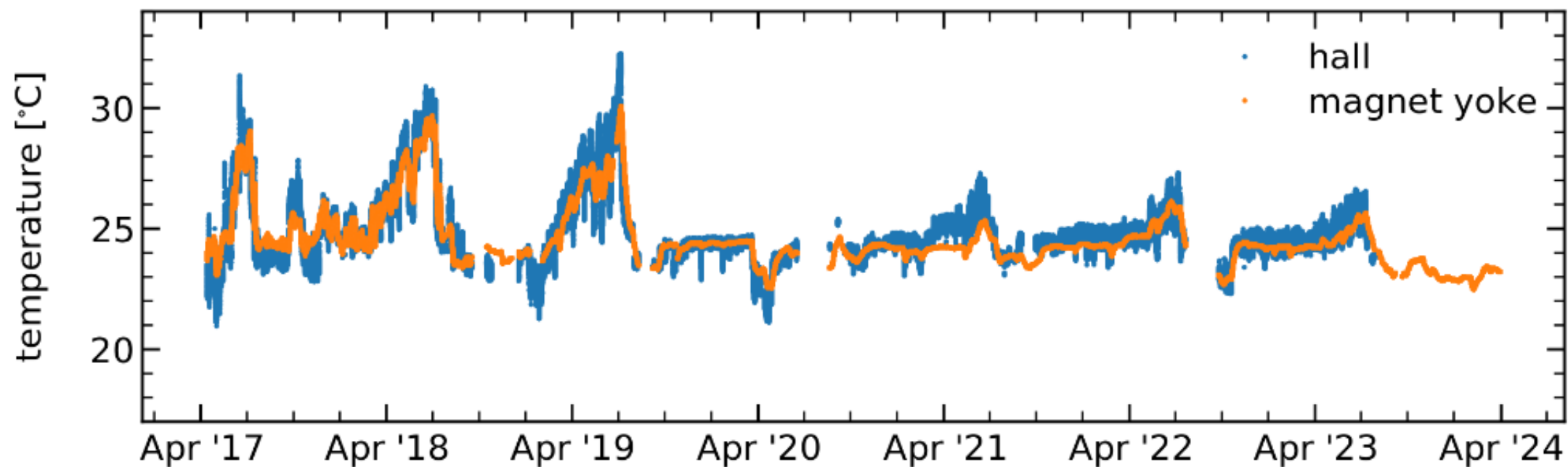
No DM

Gradient coupling (10% of  $\omega_a$ )

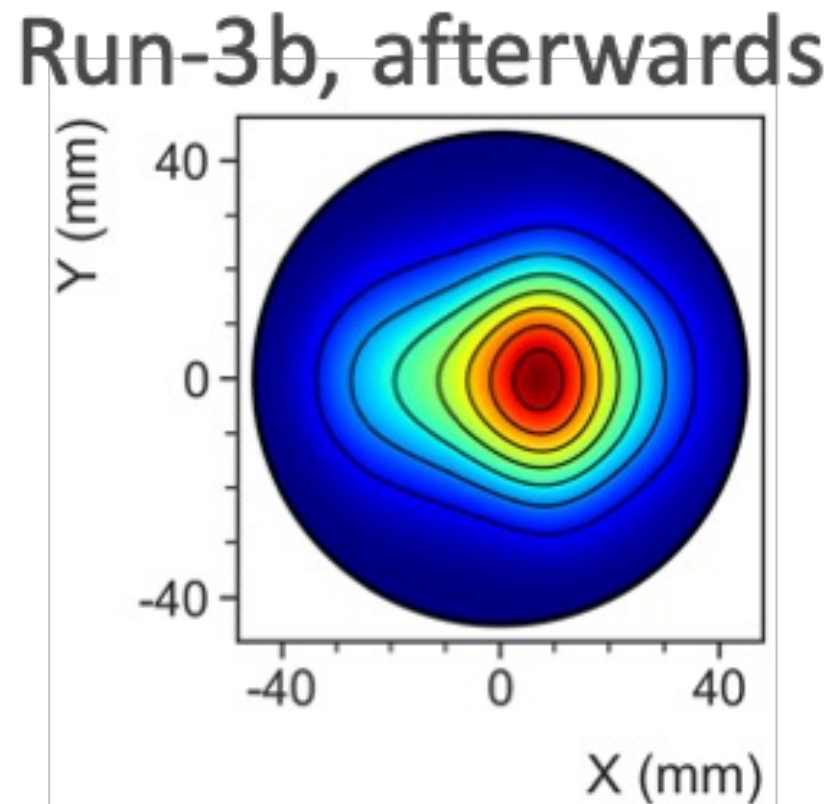
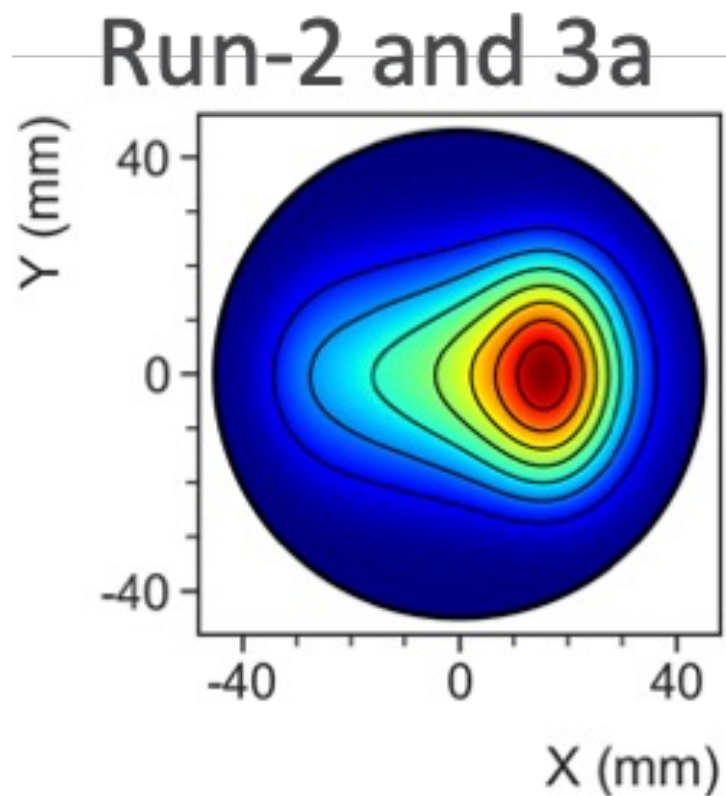
# Detectors



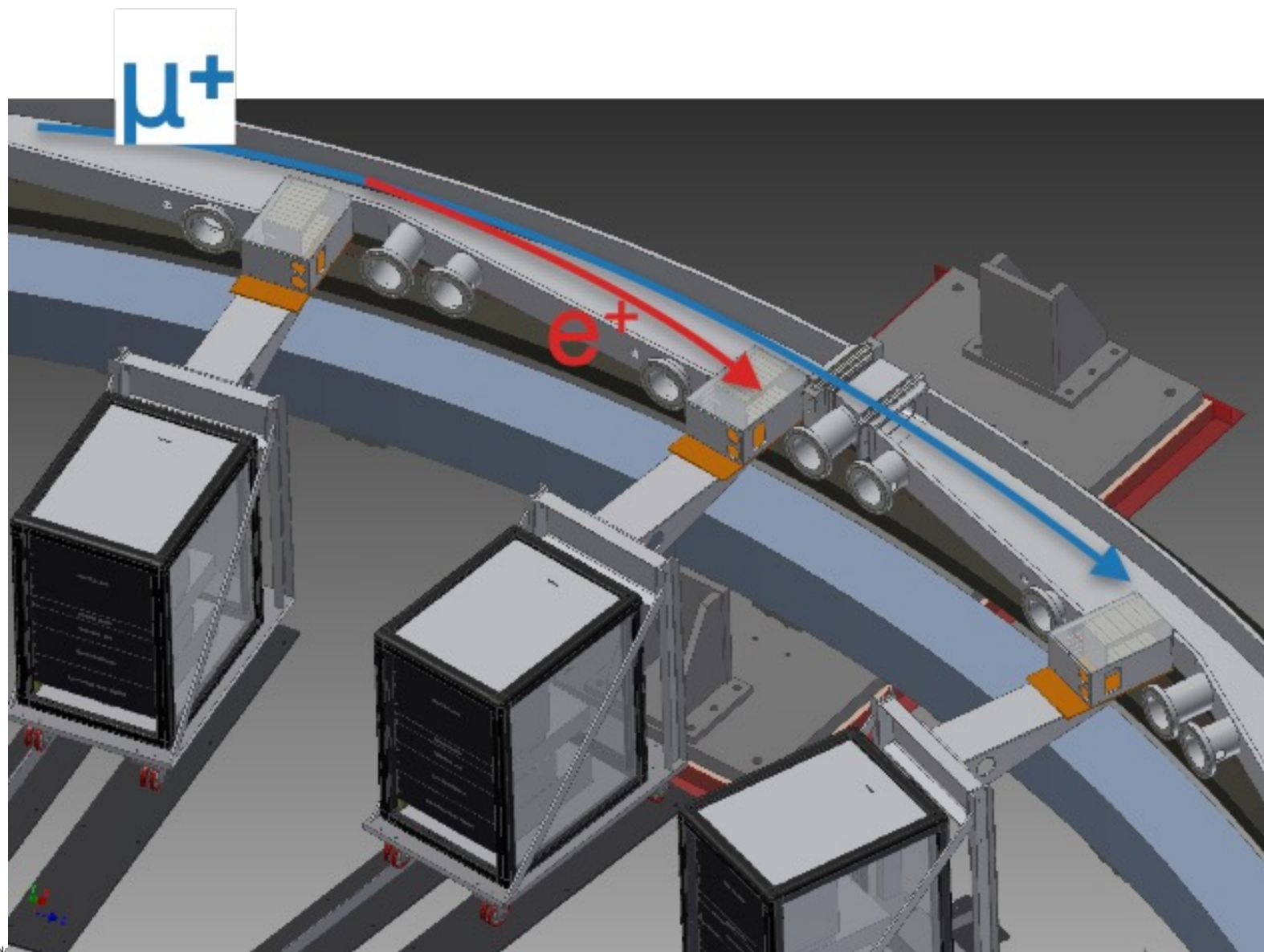
# Temperature



# Kicker Upgrade



# Calorimeters





# Other Experiment

# CERN Experiments – what a difference!

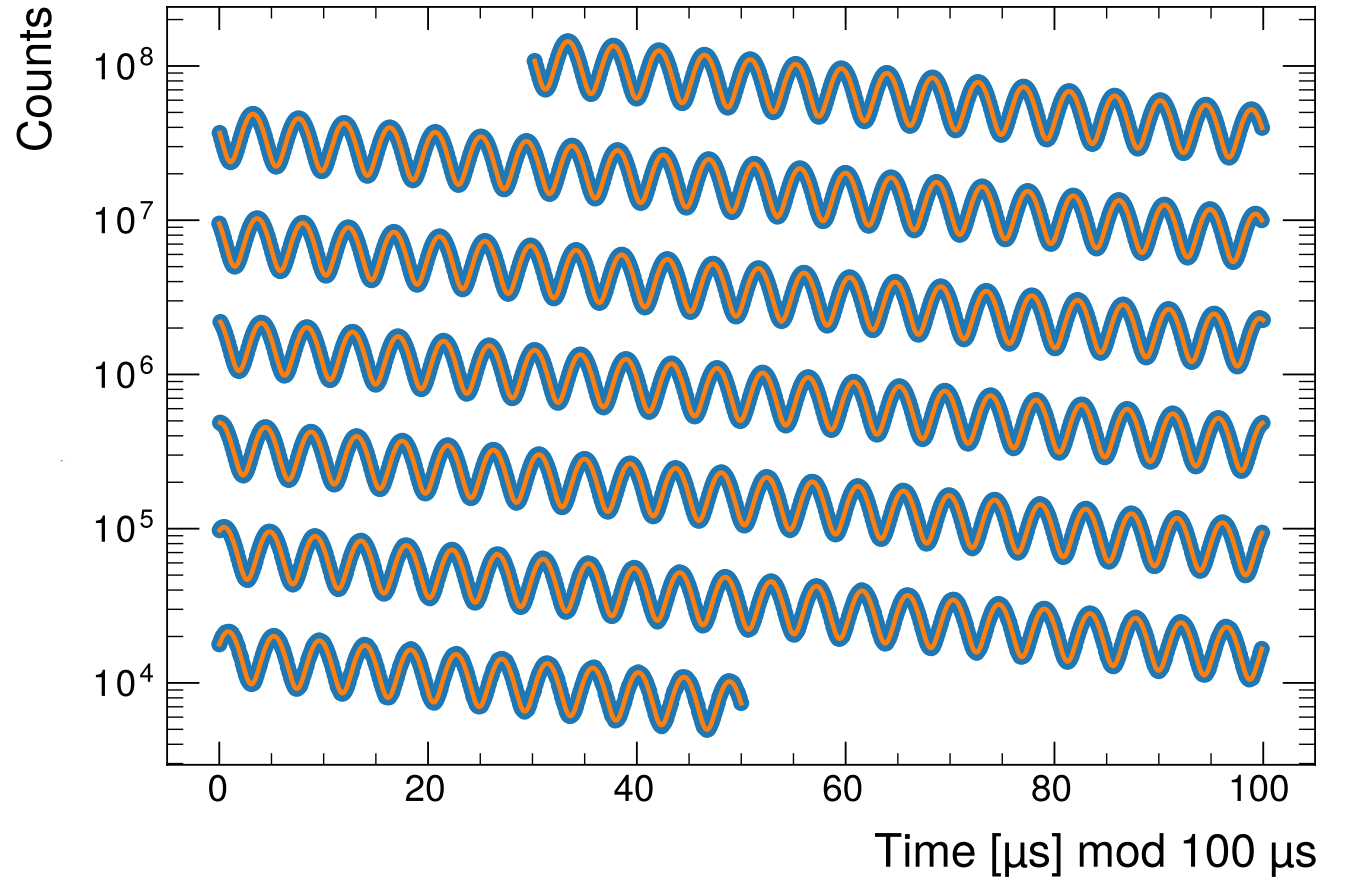
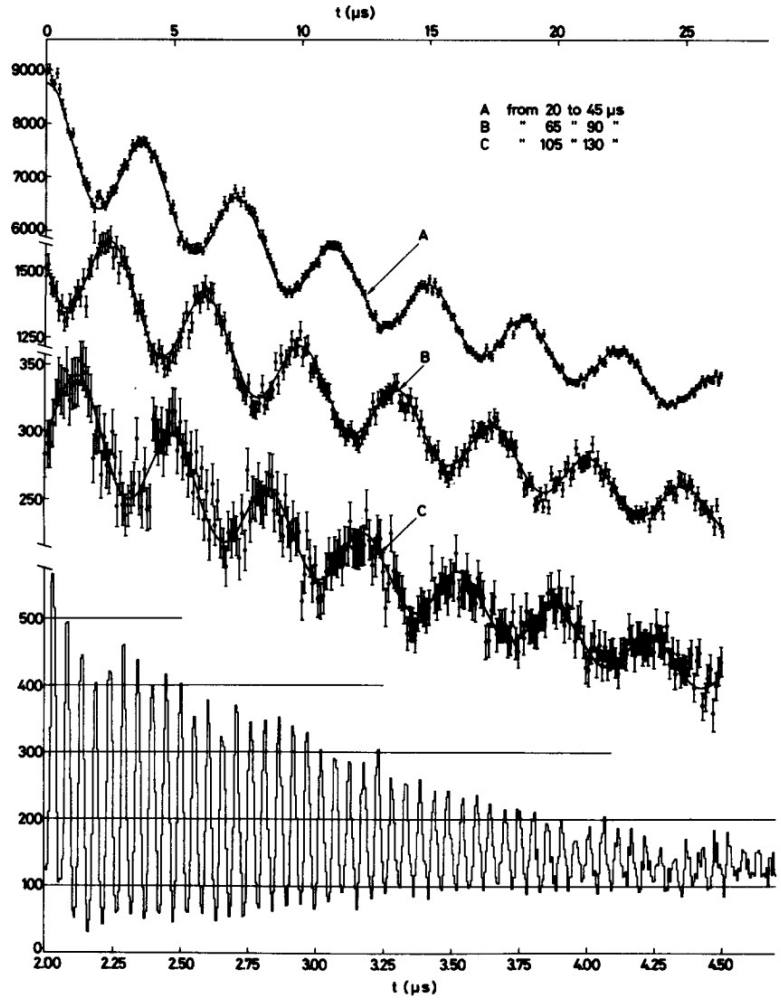


Fig. 2. Distribution of decay-electron events as a function of time. Lower curve shows rotation frequency of muon at early time. A, B, C: late time data, 20–130  $\mu\text{sec}$  showing  $(g-2)$ -precession. Data are fitted from 21 to 190  $\mu\text{sec}$ .

MUonE uses a new, independent evaluation of  $a_{\mu}^{HLO}$

$$a_{\mu}^{HLO} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{had}[t(x)]$$

$\Delta\alpha_{had}$ : hadronic contribution to the running of  $\alpha$  in the space-like region

$\Delta\alpha_{had}(t)$ : can be extracted from the shape of  $\mu e \rightarrow \mu e$  differential cross section

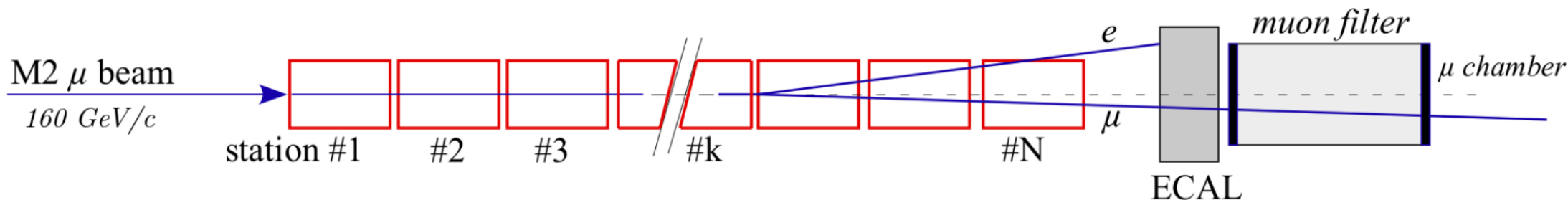
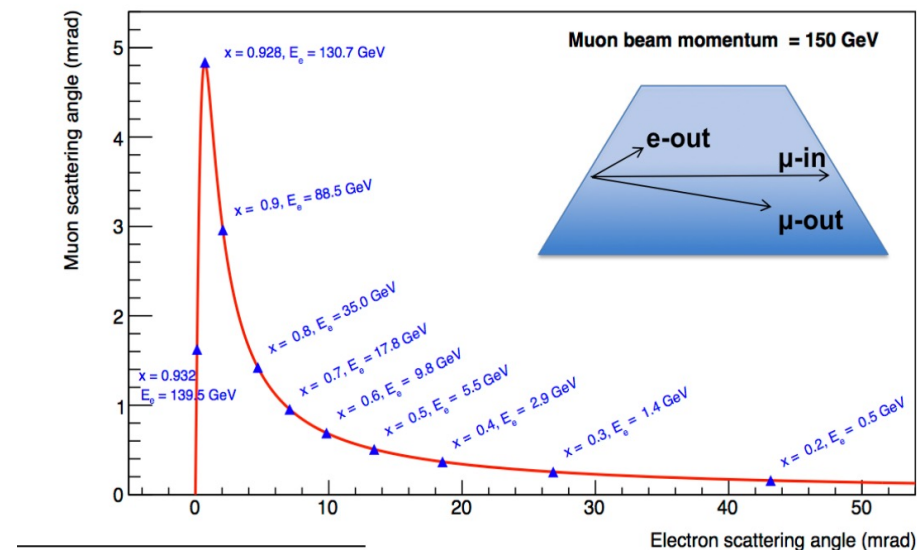
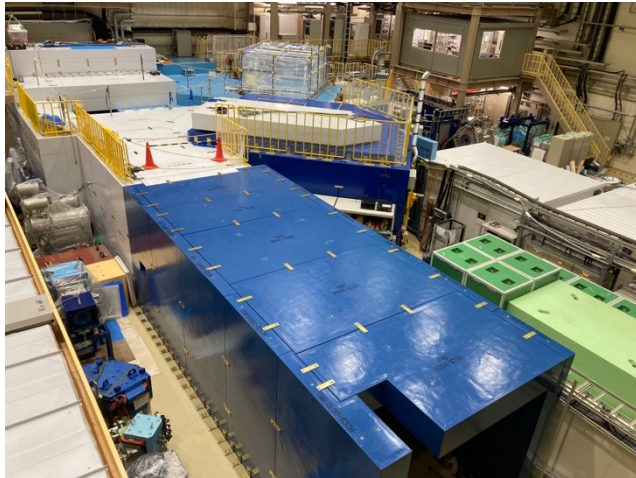
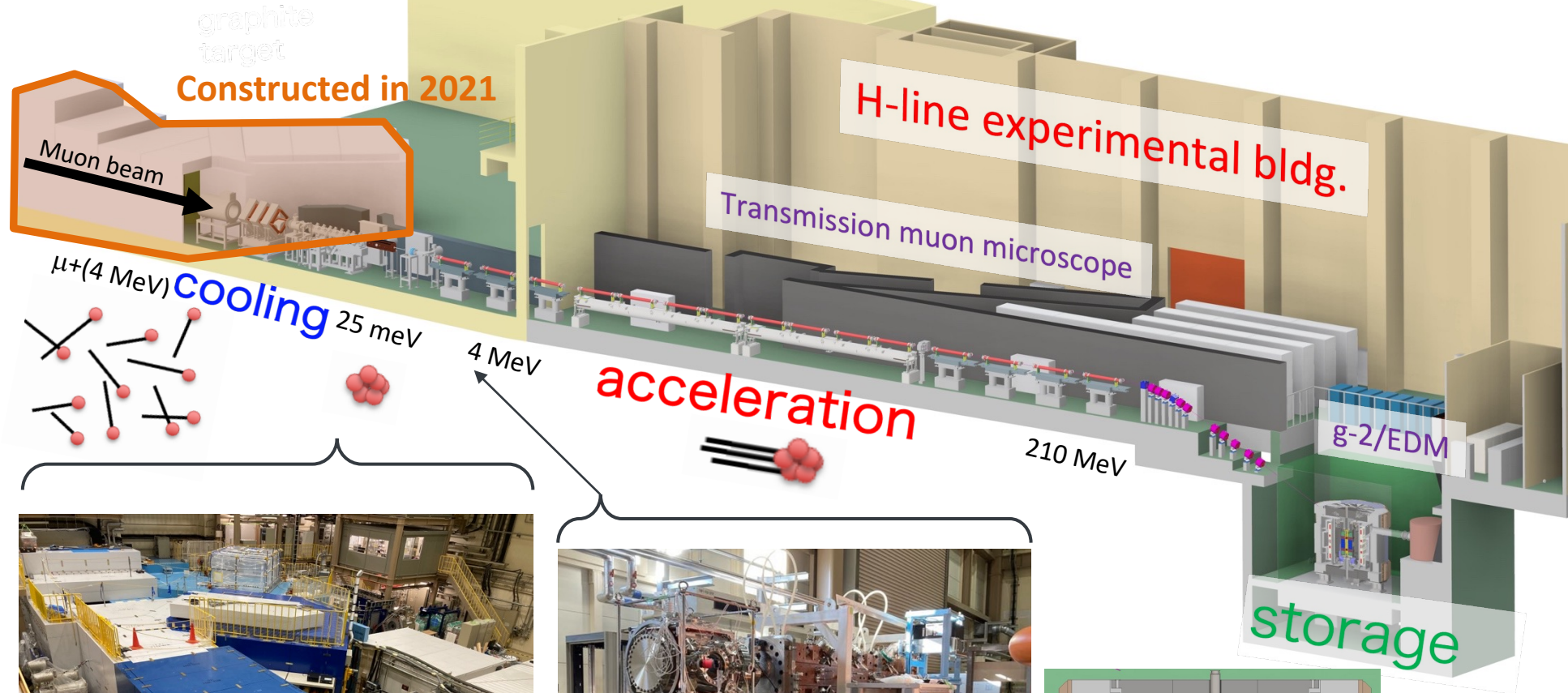


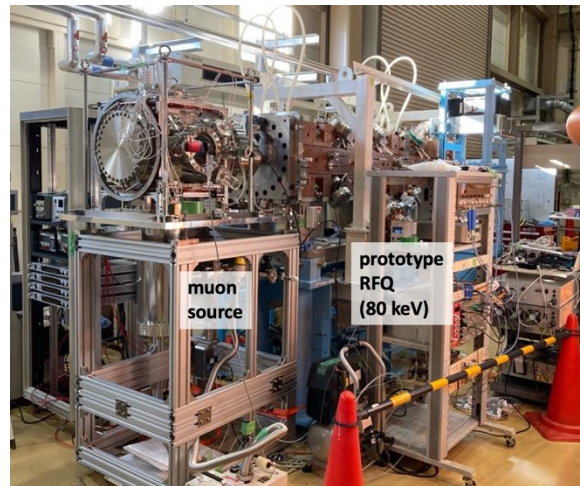
Figure 24: Schematic view of the MUonE experimental apparatus (not to scale).



# J-PARC g-2/EDM



Shields area control (2022)



RF Acc. Test at S2 area (May 2023)

